



UC Berkeley EECS
Lecturer SOE
Dan Garcia

CS10 The Beauty and Joy of Computing

Lecture #7 Algorithmic Complexity

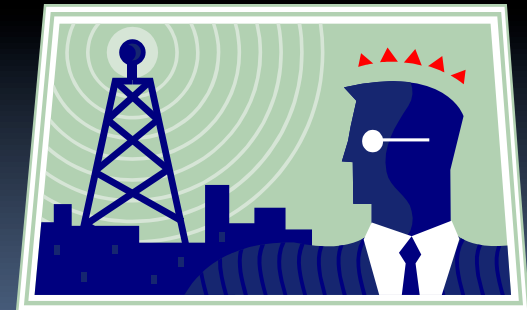
2011-02-09

1 GBPS WI-FI COMING TO A BILLION DEVICES

One million Wi-Fi devices isn't cool.

You know what's cool? A Billion Wi-Fi devices.

...all running the new 802.11ac 1G Wi-Fi standard, which hasn't yet been ratified by the IEEE, but we'll see draft by 2011 and products out there by 2012. It'll use radio spectrum below 6GHz & bond 4- or 8-channels together.



Functional Abstraction (review)

- A **block**, or **function** has inputs & outputs
 - Possibly no inputs
 - Possibly no outputs (if block is a **command**)
 - In this case, it would have a "side effect", i.e., what it does (e.g., move a robot)
- The **contract** describing what that block does is called a **specification** or **spec**



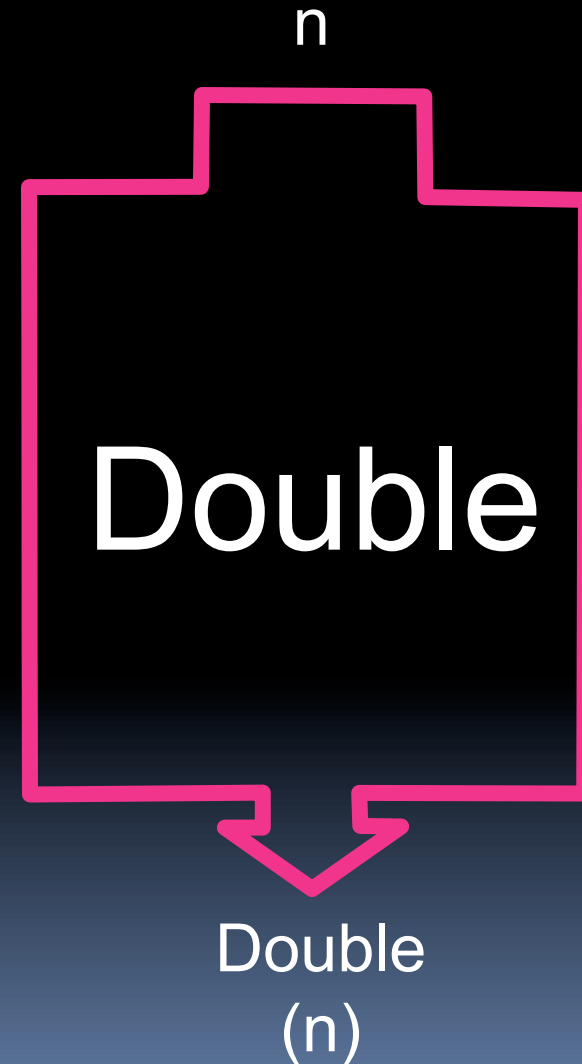
What is IN a spec? (review)

- Typically they all have

- NAME
- INPUT (s)
 - (and types, if appropriate)
 - Requirements
- OUTPUT
 - Can write "none"
- (SIDE-EFFECTS)
- EXAMPLE CALLS

- Example

- NAME : Double
- INPUT : n (a number)
- OUTPUT : n + n



What is NOT in a spec?

- **How!**
 - That's the beauty of a functional abstraction; it doesn't say **how** it will do its job.
- **Example: Double**
 - Could be $n * 2$
 - Could be $n + n$
 - Could be $n+1$ (n times)
 - if n is a positive integer
- **This gives great freedom to author!**
 - You choose Algorithm(s)!



What do YOU think?

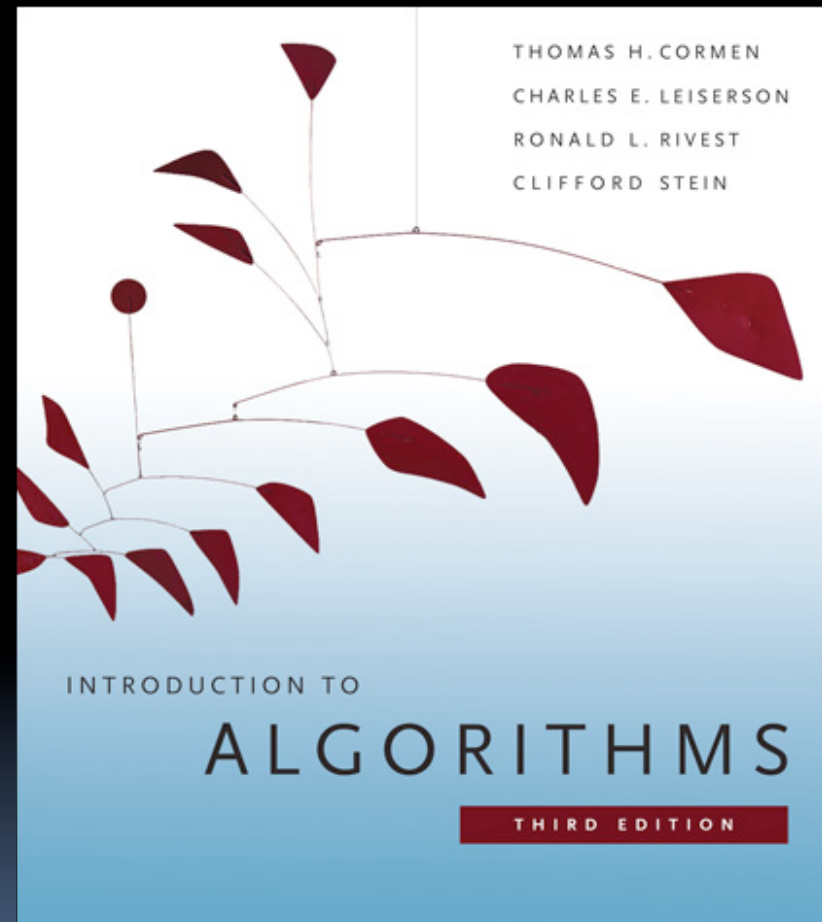
Which factor below is the most important in choosing the algorithm to use?

- A. Simplest?
- B. Easiest to implement?
- C. Takes less time?
- D. Uses up less space (memory)?
- E. Gives a more precise answer?



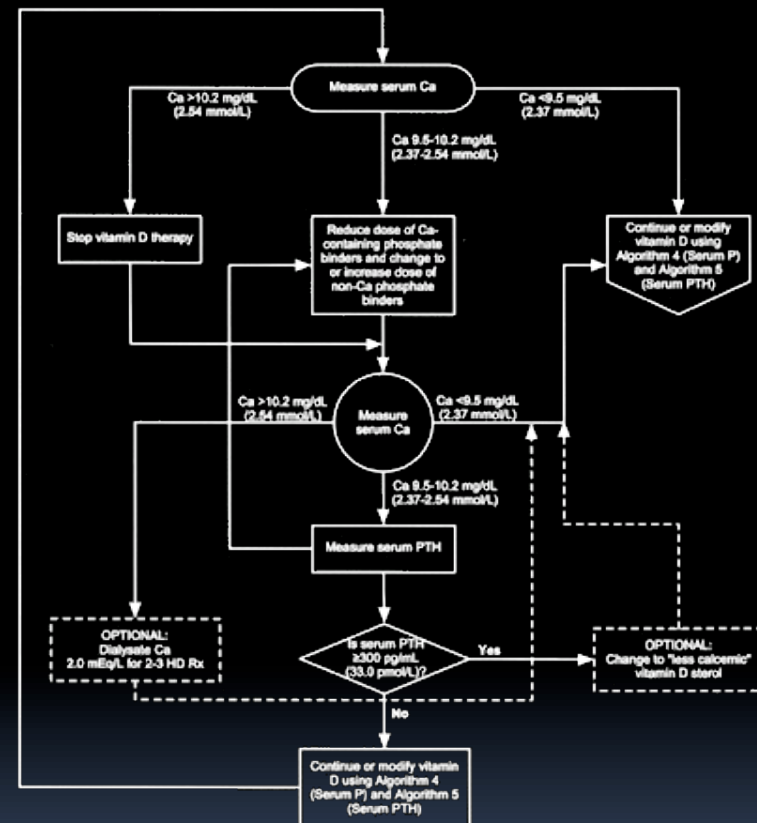
Reference text

- This book launched a generation of CS students into Algorithm Analysis
 - It's on everyone's shelf
 - It might be hard to grok at this point, but if you go on in CS, remember it & own it!
 - ...but get the most recent vers



Algorithm analysis : the basics

- An algorithm is **correct** if, for every input, it reports the correct output and doesn't run forever or cause an error.
 - Incorrect algorithms may run forever, or may crash, or may not return the correct answer.
 - They could still be useful!
 - Consider an approximation...
 - For now, we'll only consider correct algorithms



Algorithm for managing Vitamin D sterols based on serum calcium levels.

www.kidney.org/professionals/kdoqi/guidelines_bone/guide8b.htm



Algorithm analysis : running time

- One commonly used criterion in making a decision is **running time**
 - how long does the algorithm take to run and finish its task?
- How do we measure it?



Runtime analysis problem & solution

- Time w/stopwatch, but...
 - Different computers may have different runtimes. ☹️
 - Same computer may have different runtime on the same input. ☹️
 - Need to implement the algorithm first to run it. ☹️
- **Solution: Count the number of “steps” involved, not time!**
 - Each operation = 1 step
 - *If we say “running time”, we’ll mean # of steps, not time!*



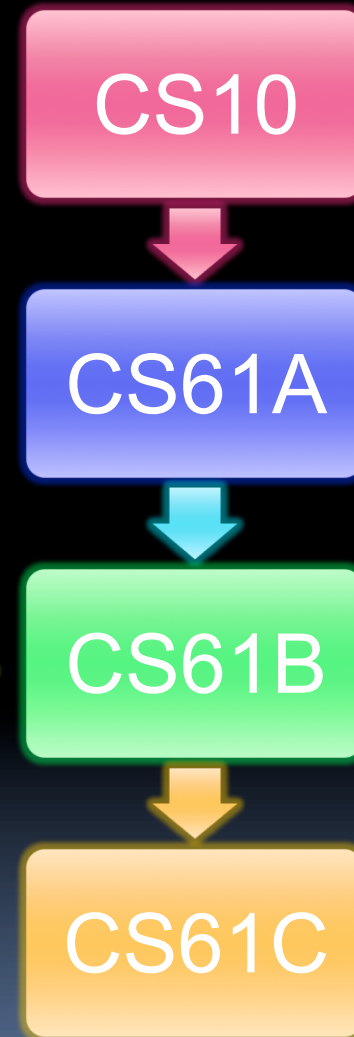
Runtime analysis : input size & efficiency

- **Definition**

- **Input size**: the # of things in the input.
- E.g., # of things in a list
- Running time as a function of input size
- Measures **efficiency**

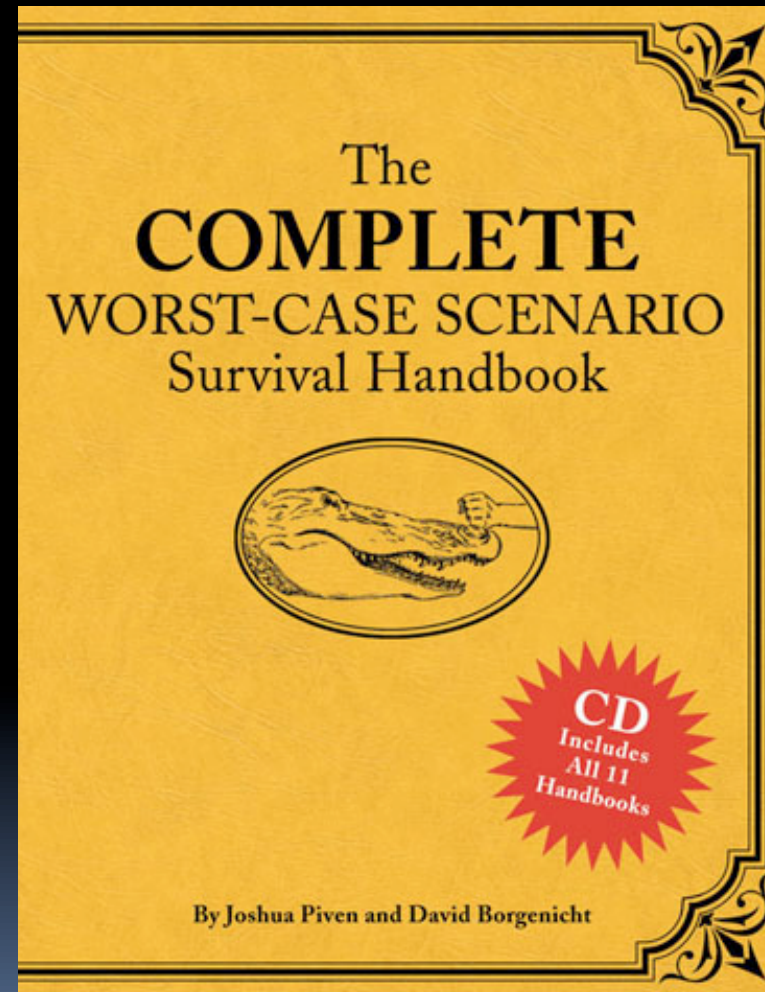
- **Important!**

- In CS10 we won't care about the efficiency of your solutions!
- ...in CS61B we will



Runtime analysis : worst or avg case?

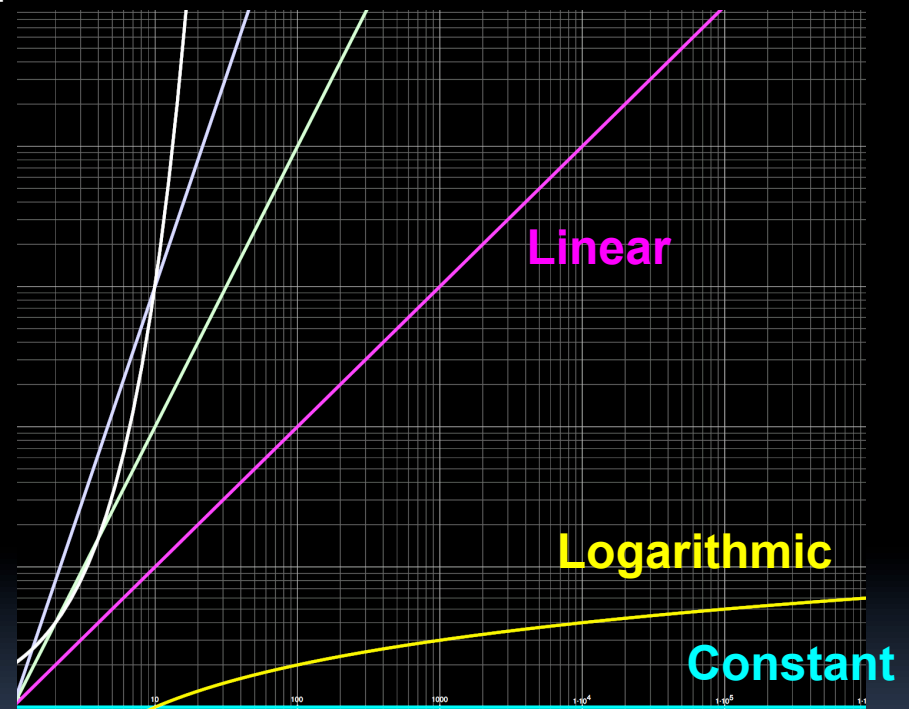
- **Could use avg case**
 - Average running time over a vast # of inputs
- **Instead: use worst case**
 - Consider running time as input grows
- **Why?**
 - Nice to know most time we'd ever spend
 - Worst case happens often
 - Avg is often \sim worst



Runtime analysis: Final abstraction

- Instead of an exact number of operations we'll use abstraction
 - Want **order of growth**, or dominant term
- In CS10 we'll consider
 - Constant
 - Logarithmic
 - Linear
 - Quadratic
 - Cubic
 - Exponential
- E.g. $10n^2 + 4\log n + n$
 - ...is quadratic

Exponential Cubic Quadratic



Graph of order of growth curves on log-log plot



Example: Finding a student (by ID)

- **Input**
 - Unsorted list of students L
 - Particular student S
- **Output**
 - True if S is in L , else False
- **Pseudocode Algorithm**
 - Start one by one, checking for match.
 - If match, true
 - If exhausted L and didn't find S , false



- **Worst-case running time as function of the size of L ?**
 1. Constant
 2. Logarithmic
 3. Linear
 4. Quadratic
 5. Exponential



Example: Finding a student (by ID)

- **Input**
 - Sorted list of students L
 - Particular student S
- **Output : same**
- **Pseudocode Algorithm**
 - Start in middle
 - If match, report true
 - If exhausted, throw away half of L and check again in the middle of remaining part of L
 - If nobody left, report false
- **Worst-case running time as function of the size of L ?**
 1. Constant
 2. Logarithmic
 3. Linear
 4. Quadratic
 5. Exponential



Example: Finding a student (by ID)

- What if L were given to you in advance and you had infinite storage?
 - Could you do any better than logarithmic?



- Worst-case running time as function of the size of L ?
 1. Constant
 2. Logarithmic
 3. Linear
 4. Quadratic
 5. Exponential



Example: Finding a shared birthday

- **Input**

- Unsorted list L (of size n) of birthdays of team

- **Output**

- True if any two people shared birthday, else False

- **What's the worst-case running time?**



- **Worst-case running time as function of the size of L ?**

1. Constant
2. Logarithmic
3. Linear
4. Quadratic
5. Exponential



Example: Finding subsets

- **Input:**
 - Unsorted list L (of size n) of people
- **Output**
 - All the subsets
- **Worst-case running time?**
- **E.g., for 3 people (a,b,c):**
 - 1 empty: $\{\}$
 - 3 1-person: $\{a, b, c\}$
 - 3 2-person: $\{ab, bc, ac\}$
 - 1 3-person: $\{abc\}$



- **Worst-case running time as function of the size of L ?**
 1. Constant
 2. Logarithmic
 3. Linear
 4. Quadratic
 5. Exponential



Summary

- When choosing algorithm, could optimize for
 - Simplest
 - Easiest to implement?
 - **Most efficient**
 - Uses up least resources
 - Gives most precision
 - ...
- In CS10 we'll consider
 - Constant
 - Logarithmic
 - Linear
 - Quadratic
 - Cubic
 - Exponential



How does the goalie choose how to block ball?

