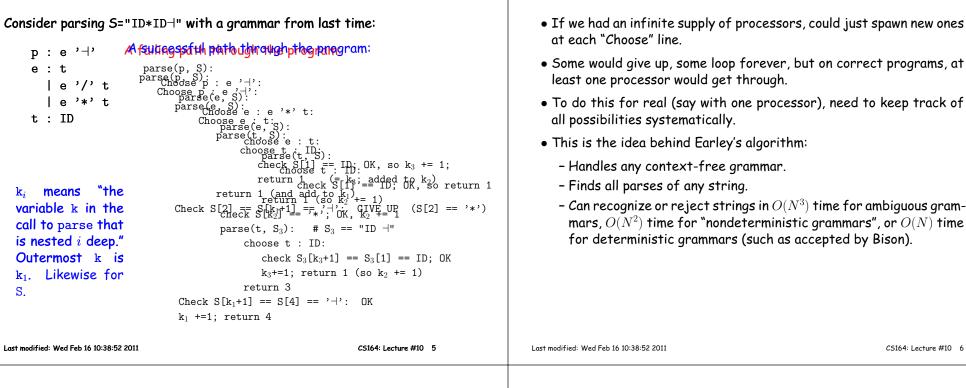
Lecture 10: General and Bottom-Up Parsing A Little Notation Job Opportunity. Professor Keltner of the Psychology Department is Here and in lectures to follow, we'll often have to refer to general looking for a web developer to help with a moodle system (CMS). There productions or derivations. In these, we'll use various alphabets to mean are options for a stipend, and if the project is completed on schedule various thinas: the developer's work will be shown on a TEDx presentation. See Piazzza • Capital roman letters are nonterminals (A, B,...). for more details. • Lower-case roman letters are terminals (or tokens, characters, etc.) • Lower-case greek letters are sequences of zero or more terminal and nonterminal symbols, such as appear in sentential forms or on the right sides of productions (α, β, \ldots) . Subscripts on lower-case greek letters indicate individual symbols within them, so $\alpha = \alpha_1 \alpha_n \dots \alpha_n$ and each α_i is a single terminal or nonterminal. For example, • $A: \alpha$ might describe the production e: e '+' t, • $B \Rightarrow \alpha A \gamma \Rightarrow \alpha \beta \gamma$ might describe the derivation steps e \Rightarrow e '+' t \Rightarrow e '+' ID (α is e '+'; A is t; B is e; and γ is empty.) Last modified: Wed Feb 16 10:38:52 2011 CS164: Lecture #10 1 Last modified: Wed Feb 16 10:38:52 2011 CS164: Lecture #10 2 Abstract body of parse(A,S) **Fixing Recursive Descent** • Can formulate top-down parsing analogously to NFAs. • First, let's define an impractical but simple implementation of a topdown parsing routine. parse (A, S): """Assuming A is a nonterminal and S = $c_1c_2...c_n$ is a string, return • For nonterminal A and string $S=c_1c_2...c_n$, we'll define parse(A, S) to integer k such that A can derive the prefix string $c_1 \dots c_k$ of S.""" return the length of a valid substring derivable from A. Choose production 'A: $\alpha_1 \alpha_2 \cdots \alpha_m$ ' for A (nondeterministically) • That is, parse(A, $c_1c_2...c_n$) = k, where k = 0for x in $\alpha_1, \alpha_2, \cdots, \alpha_m$: if x is a terminal: $\underbrace{\underbrace{c_1c_2\ldots c_k}_{A \xrightarrow{*}} c_{k+1}c_{k+2}\ldots c_n}_{A \xrightarrow{*}}$ if x == c_{k+1} : k += 1 else: GIVE UP else: k += parse (x, $c_{k+1} \cdots c_n$) return k • Assume that the grammar contains one production for the start symbol: p: $\gamma \dashv$. • We'll say that a call to parse returns a value if some set of choices for productions (the blue step) would return a value (just like NFA). • Then if parse(p, S) returns a value, S must be in the language.

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Example



Earley's Algorithm: I

- First, reformulate to use recursion instead of looping. Assume the string $S = c_1 \cdots c_n$ is fixed.
- Redefine parse:

```
parse (A: \alpha \bullet \beta, s, k):

"""Assumes A: \alpha\beta is a production in the grammar,

0 <= s <= k <= n, and \alpha can produce the string c_{s+1}\cdots c_k.

Returns integer j such that \beta can produce c_{k+1}\cdots c_j."""
```

• Or diagrammatically, parse returns an integer j such that:

```
c_1 \cdots c_s \underbrace{c_{s+1} \cdots c_k}_{\alpha \stackrel{*}{\Longrightarrow}} \underbrace{c_{k+1} \cdots c_j}_{\beta \stackrel{*}{\Longrightarrow}} c_{j+1} \cdots c_n
```

Earley's Algorithm: II

Making a Deterministic Algorithm

```
parse (A: \alpha \bullet \beta, s, k):
   """Assumes A: \alpha\beta is a production in the grammar,
       0 <= s <= k <= n, and \alpha can produce the string c_{s+1} \cdots c_k
       Returns integer j such that \beta can produce c_{k+1} \cdots c_i."""
   if \beta is empty:
       return k
   Assume \beta has the form x\delta
   if x is a terminal:
       if x == c_{k+1}:
            return parse(A: \alpha x \bullet \delta, s, k+1)
       else:
             GIVE UP
   else:
       Choose production 'x: \kappa' for x (nondeterministically)
       j = parse(x: \bullet \kappa, k, k)
       return parse (A: \alpha x \bullet \delta, s, j)
```

• Now do all possible choices that result in such a way as to avoid redundant work ("nondeterministic memoization").

Chart Parsing

- Idea is to build up a table (known as a *chart*) of all calls to parse that have been made.
- Only one entry in chart for each distinct triple of arguments (A: $\alpha \bullet \beta$, s, k).
- We'll organize table in columns numbered by the k parameter, so that column k represents all calls that are looking at c_{k+1} in the input.
- Each column contains entries with the other two parameters: [A: $\alpha \bullet \beta$, s], which are called *items*.
- The columns, therefore, are *item sets*.

Example

 Grammar
 Input String

 p : e '⊣'
 - I + I ⊣

 e : s I | e '+' e
 - I + I ⊣

 s : '-' |
 - I + I ⊣

Chart. Headings are values of k and c_{k+1} (raised symbols).

						1 (
	0	-		1 ^I			2	+	· 3 ^I
a.p:	•e '⊢', 0		e. S :	'-'●, 0	<i>g.</i> e:	S	I•, 0		<i>i</i> .e: e '+' ●e, 0
<i>b.</i> e:	●e '+' e,	0	f.e:	s•I, 0	h.e:	е	•'+' e,	0	j.e: •s I, 3
с.е:	•s I, 0								k.s: ●, 3
d. s :	●'-', O								1.e: s •I, 3
	4	4		5					'
m.e:	s I•, 3		р.р:	e '⊣' •	, 0				
n.e:	e '+' e●,	0							
<i>o.</i> p:	e•'⊣', 0								

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Example, completed

• Last slide showed only those items that survive and get used. Algorithm actually computes dead ends as well (unlettered, in red).

0	-	1	I	2	+	3	I
a.p: • e '⊢', () e. S :	· - · • ,	0 g.e:	s I•, O	<i>i.</i> e:	e '+' ● e,	0
b.e: ● e '+' e,	0 f.e:	s• I,	0 h.e:	e ● '+' ∈	e, 0 j.e:	• s I, 3	
c.e: ● s I, O			p:	e•'⊣',	0 k.s:	•, 3	
d.s: • '−', 0					<i>I.</i> e:	s • I, 3	
s: •, 0					s:	• '-', 3	
e: s • I, O					e:	• e '+' e,	3
4	4	5					
m.e: s I∙, 3	<i>p</i> . p :	e '⊣'	•, 0				
n.e: e '+' e●,	0						
o.p: e● '⊣', 0							
e: e • '+' e,	3						

Adding Semantic Actions

- Pretty much like recursive descent. The call parse(A: $\alpha \bullet \beta$, s, k) can return, in addition to j, the semantic value of the A that matches characters $c_{s+1} \cdots c_j$.
- This value is actually computed during calls of the form parse(A: α' •, s, k) (i.e., where the β part is empty).
- Assume that we have attached these values to the nonterminals in α , so that they are available when computing the value for A.

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Ambiguity

- Ambiguity only important here when computing semantic actions.
- Rather than being satisfied with a single path through the chart, we look at *all* paths.
- And we attach the set of possible results of $parse(Y: \bullet \kappa, s, k)$ to the nonterminal Y in the algorithm.

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