# Lecture 17: Types<sup>1</sup>

#### Administrivia

 Autograder trial run: Tuesday night. I will run it only a few times and shut it off before morning. It comes on again at the deadline.

<sup>1</sup>From material by G. Necula and P. Hilfinger Last modified: Mon Feb 28 10:50:47 2011

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## Types and Type Systems

- A type is a set of *values* together with a set of *operations* on those values.
- E.g., fields and methods of a Java class are meant to correspond to values and operations.
- A language's type system specifies which operations are valid for which types.
- Goal of type checking is to ensure that operations are used with the correct types, enforcing intended interpretation of values.
- Notion of "correctness" often depends on what programmer has in mind, rather than what the representation would allow.
- Most operations are legal only for values of some types
  - Doesn't make sense to add a function pointer and an integer in C
  - It does make sense to add two integers
  - But both have the same assembly language implementation:

    mov1 y, %eax; addl x, %eax

## Type Checking Phase

- Determines the type of each expression in the program, (each node in the AST that corresponds to an expression)
- Finds type errors.
  - Examples?
- The *type rules* of a language define each expression's type and the types required of all expressions and subexpressions.

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## Uses of Types

- Detect errors:
  - Memory errors, such as attempting to use an integer as a pointer.
  - Violations of abstraction boundaries, such as using a private field from outside a class.
- Help compilation:
  - When Python sees x+y, its type systems tells it almost nothing about types of x and y, so code must be general.
  - In C, C++, Java, code sequences for x+y are smaller and faster, because representations are known.

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### Review: Dynamic vs. Static Types

- A dynamic type attaches to an object reference or other value. It's a run-time notion, applicable to any language.
- The *static type* of an expression or variable is a constraint on the possible dynamic types of its value, enforced at compile time.
- Language is *statically typed* if it enforces a "significant" set of static type constraints.
  - A matter of degree: assembly language might enforce constraint that "all registers contain 32-bit words," but since this allows just about any operation, not considered static typing.
  - C sort of has static typing, but rather easy to evade in practice.
  - Java's enforcement is pretty strict.
- In early type systems, dynamic\_type( $\mathcal{E}$ ) = static\_type( $\mathcal{E}$ ) for all expressions  $\mathcal{E}$ , so that in all executions,  $\mathcal{E}$  evaluates to exactly type of value deduced by the compiler.
- Gets more complex in advanced type systems.

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## Example

Variables, with static type A can hold values with dynamic type  $\leq A$ , or in general...

### Subtyping

• Define a relation  $X \leq Y$  on classes to say that:

An object (value) of type  $\boldsymbol{X}$  could be used when one of type  $\boldsymbol{Y}$  is acceptable

or equivalently

```
X conforms to Y
```

- In Java this means that X extends Y.
- Properties:
  - $-X \preceq X$
  - $-X \leq Y$  if X inherits from Y.
  - $X \leq Z$  if  $X \leq Y$  and  $Y \leq Z$ .

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## Type Soundness

#### Soundness Theorem on Expressions.

```
\forall E. \ \mathsf{dynamic\_type}(E) \preceq \mathsf{static\_type}(E)
```

- Compiler uses  $static\_type(E)$  (call this type C).
- All operations that are valid on C are also valid on values with types  $\leq C$  (e.g., attribute (field) accesses, method calls).
- Subclasses only add attributes.
- Methods may be overridden, but only with same (or compatible) signature.

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### Typing Options

- Statically typed: almost all type checking occurs at compilation time (C, Java). Static type system is typically rich.
- Dynamically typed: almost all type checking occurs at program execution (Scheme, Python, Javascript, Ruby). Static type system can be trivial.
- Untyped: no type checking. What we might think of as type errors show up either as weird results or as various runtime exceptions.

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### Using Subtypes

- In languages such as Java, can define types (classes) either to
  - Implement a type, or
  - Define the operations on a family of types without (completely) implementing them.
- Hence, relaxes static typing a bit: we may know that something is a Y without knowing precisely which subtype it has.

### "Type Wars"

- Dynamic typing proponents say:
  - Static type systems are restrictive; can require more work to do reasonable things.
  - Rapid prototyping easier in a dynamic type system.
  - Use duck typing: define types of things by what operations they respond to ("if it walks like a duck and quacks like a duck, it's a duck").
- Static typing proponents say:
  - Static checking catches many programming errors at compile time.
  - Avoids overhead of runtime type checks.
  - Use various devices to recover the flexibility lost by "going static:" subtyping, coercions, and type parameterization.
  - Of course, each such wrinkle introduces its own complications.

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## Implicit Coercions

• In Java, can write

```
int x = 'c';
float y = x;
```

- But relationship between **char** and **int**, or **int** and **float** not usually called subtyping, but rather **conversion** (or **coercion**).
- $\bullet$  Such implicit coercions avoid cumbersome casting operations.
- Might cause a change of value or representation,
- But usually, such coercions allowed implicitly only if type coerced to contains all the values of the that coerced from (a widening coercion).
- Inverses of widening coercions, which typically lose information (e.g., int—>char), are known as narrowing coercions. and typically required to be explicit.
- int—float a traditional exception (implicit, but can lose information and is neither a strict widening nor a strict narrowing.)

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### Coercion Examples

Possibility of implicit coercion complicates type-matching rules (see C++).

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ference having the form

that the rules are accurate.

• For type checking, this might become:

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## Prolog: A Declarative Programming Language

- Prolog is the most well-known logic programming language.
- Its statements "declare" facts about the desired solution to a problem. The system then figures out the solution from these facts.
- You saw this in CS61A
- General form:

```
Conclusion: - Hypothesis<sub>1</sub>,..., Hypothesis<sub>k</sub>.
```

for  $k \ge 0$  means Means "may infer Conclusion by first establishing each Hypothesis." (when k = 0, we generally leave off the ':-').

- Each conclusion and hypothesis is a kind of *term*, represent both programs and data. A term is:
  - A constant, such as a, foo, bar12, =, +, '(', 12, 'Foo'.
  - A variable, denoted by an unquoted symbol that starts with a capital letter or underscore: E, Type, \_foo.
  - The nameless variable (\_) stands for a different variable each time it occurs.
- A structure, denoted in prefix form: symbol(term1, ..., term\_k).

  Very general: can represent ASTs, expressions, lists, facts.

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• Constants and structures can also represent conclusions and hypotheses, just as some list structures in Scheme can represent programs.

Type Inference

• Types of expressions and parameters need not be explicit to have

• The appropriate formalism for type checking is logical rules of in-

If  $E_1$  and  $E_2$  have certain types, then  $E_3$  has a certain type.

• Given proper notation, easy to read (with practice), so easy to check

static typing. With the right rules, might infer their types.

If Hypothesis is true, then Conclusion is true

• Can even be mechanically translated into programs.

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## **Prolog Sugaring**

- For convenience, allows structures written in infix notation, such as a + X rather than +(a,X).
- List structures also have special notation:
  - Can write as .(a,(b,(c,[]))) or .(a,(b,(c,X)))
  - But more commonly use [a, b, c] or  $[a, b, c \mid X]$ .

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## Examples: From English to an Inference Rule

- "If e1 has type int and e2 has type int, then e1+e2 has type int:"
   typeof(E1 + E2, int): typeof(E1, int), typeof(E2, int).
- "All integer literals have type int:"

```
typeof(X, int) := integer(X).
```

(integer is a built-in predicate on terms).

• In general, our typeof predicate will take an AST and a type as arguments.

#### Inference Databases

- Can now express ground facts, such as likes(brian, potstickers).
- Universally quantified facts, such as eats(brian, X).

(for all X, brian eats X).

• Rules of inference, such as

eats(brian, X):- isfood(X), likes(brian, X).

(you may infer that brian eats  $\boldsymbol{X}$  if you can establish that  $\boldsymbol{X}$  is a food and brian likes it.)

• A collection (database) of these constitutes a Prolog program.

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#### Soundness

- We'll say that our definition of typeof is sound if
  - Whenever rules show that typeof(e,t), e always evaluates to a value of type t

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- We only want sound rules,
- But some sound rules are better than others; here's one that's not very useful:

```
typeof(X,any) := integer(X).
```

Instead, would be better to be more general, as in

typeof(X,any).

(that is, any expression X is an any.)

#### Example: A Few Rules for Java

- typeof(! X, boolean) :- typeof(X, boolean).
- typeof(while(E, S), void) :- typeof(E, boolean), typeof(S, void).
- typeof(X,void):- typeof(X,Y), valuetype(Y).
- valuetype(int).
- valuetype(double).
- ...
- valuetype(array(X)):- valuetype(X).

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## Defining the Environment in Prolog

- Can define a predicate, say, defn(I,T,E), to mean "I is defined to have type T in environment E."
- We can implement such a defn in Prolog like this:

```
defn(I, T, [def(I,T) | _]).

defn(I, T, [def(I1,_)|R]) := dif(I,I1), defn(I,T,R).
```

(dif is built-in, and means that its arguments differ).

 Now we revise typeof to have a 3-argument predicate: typeof(E, T, Env) means "E is of type T in environment Env," allowing us to say

```
typeof(I, T, Env) :- defn(I, T, Env).
```

#### The Environment

- What is the type of a variable instance? E.g., how do you show that typeof(x, int)?
- Ans: You can't, in general, without more information.
- We need a hypothesis of the form "we are in the scope of a declaration of x with type T.")
- A type environment gives types for free names:
- a mapping from identifiers to types.
- (A variable is *free* in an expression if the expression contains an occurrence of the identifier that refers to a declaration outside the expression.
  - In the expression x, the variable x is free
  - In lambda x: x + y only y is free (Python).
  - In map(lambda x: g(x,y), x), x, y, map, and g are free.

## **Examples Revisited**

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### Example: lambda (Python)

In effect,  $[def(X,any) \mid Env]$  means "Env modified to map x to any and behaving like Env on all other arguments."

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#### Example: Same Idea for 'let' in the Cool Language

- Cool is an object-oriented language sometimes used for the project in this course.
- The statement let x : T0 in e1 creates a variable x with given type T0 that is then defined throughout e1. Value is that of e1.
- Rule (assuming that "let(X,T0,E1)" is the AST for let):

"type of let X: T0 in E1 is T1, assuming that the type of E1 would be T1 if free instances of X were defined to have type T0".

## Example of a Rule That's Too Conservative

• Let with initialization (also from Cool):

```
let x : T0 \leftarrow e0 in e1
```

• What's wrong with this rule?

(Hint: I said Cool was an object-oriented language).

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## Loosening the Rule

- Problem is that we haven't allowed type of initializer to be subtype of TO.
- Here's how to do that:

• Still have to define subtyping (written here as <=), but that depends on other details of the language.

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#### As Usual, Can Always Screw It Up

This allows incorrect programs and disallows legal ones. Examples?

## Function Application

- Consider only the one-argument case (Java).
- AST uses 'call', with function and list of argument types.

```
typeof(call(E1,[E2]), T, Env) :-
     typeof(E1, T1->T, Env), typeof(E2, T1a, Env),
     T1a <= T1.</pre>
```

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## Conditional Expressions

• Consider:

```
e1 if e0 else e2
or (from C) e0 ? e1 : e2.
```

- The result can be value of either e1 or e2.
- The dynamic type is either e1's or e2's.
- Either constrain these to be equal (as in ML):

```
typeof(if(E0,E1,E2), T, Env) :-
    typeof(E0,bool,Env), typeof(E1,T,Env), typeof(E2,T,Env).
```

• Or use the *smallest supertype* at least as large as both of these types—the *least upper bound (lub)* (as in Cool):

```
typeof(if(E0,E1,E2), T, Env) :-
    typeof(E0,bool,Env), typeof(E1,T1,Env), typeof(E2,T2,Env),
    lub(T,T1,T2).
```