#### **Foundations of Computer Graphics** (Fall 2012)

CS 184, Lectures 17, 18:

Nuts and bolts of Ray Tracing

http://inst.eecs.berkeley.edu/~cs184

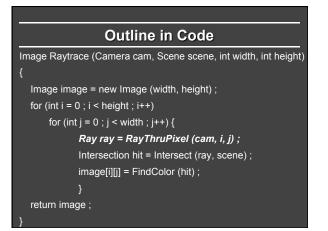
Acknowledgements: Thomas Funkhouser and Greg Humphreys

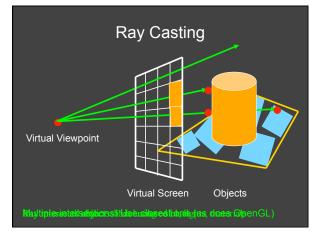
#### Heckbert's Business Card Ray Tracer

typedef struct{double x,y,z}vec;vec U,black,amb={.02,.02,.02};struct sphere{ vec cen,colo double rad,kd,ks,kt,kliji)\*s,'best,sph[]=[0,6...5,1,1,1,...,9,.05,.2,.85,0,1,7,-1,.8,,-5,1,...5,2,1,...7,.3,0,..05,1,2,1,.8,,-5,.1,.8,.8, 1,...3,7,0,0,1,2,3,-6,15,1,...8,1,..7,0,0,0,0,0,1,5,-3,-3,12,... 8,1., 1.,5.0.,0.,0.,.,5,1.5,];yx;double u,b,tmin,sqrt(),tan();double vdot(A,B)vec A ,B;{return A.x \*B.x+A.y\*B.y+A.z\*B.z;}vec vcomb(a,A,B)double a;vec A,B;{B.x+=a\* A.x;B.y+=a\*A.y;B.z+=a\*A.z; return B;)vec vunit(A)vec A;{return vcomb(1./sqrt( vdot(A,A)),A,black);}struct sphere\*intersect (P,D)vec P,D;{best=0;tmin=1e30;s= sph+5;while(s-->sph)b=vdot(D,U=vcomb(-1.,P,s->cen)), u=b\*b-vdot[(J,U)+s->rad\*s ->rad,u=u>0?sqrt(u):1e31,u=b-u>1e-7?b-u:b+u,tmin=u>=1e-7&& u<tmin?best=s,u: tmin;return best;}vec trace(level,P,D)vec P,D;[double d,eta,e;vec N,color; struct sphere's, 'i.if(!level--)return black;if(s=intersect(P,D));else return amb;color=amb;eta= s-sir;d= -vdot(D,N=vunit(vcomb(-1.,P=vcomb(tmin,D,P),s->cen )));if(d<0)N=vcomb(-1.,N,black), eta=1/eta,d= -d;l=sph+5;while(I-->sph)if((e=I ->kI\*vdot(N,U=vunit(vcomb(-1.,P,I->cen))))>0&& intersect(P,U)==I)color=vcomb(e\_l->color,color);U=s->color;color,x\*=U,x;color,y\*=U,y;color z \*=U,z;e=1-eta\* eta\*(1-d\*d);return vcomb(s->kt,e>0?trace(level,P,vcomb(eta,D,vcomb(eta\*dsqrt (e),N,black))):black,vcomb(s->ks,trace(level,P,vcomb(2\*d,N,D)),vcomb(s->kd, color,vcomb (s->kl,Ublack))));)main(){printl(\*%d %din\*,32,32);while(yx<32\*32) U.x=yx%32-32/2,U.z=32/2-yx++/32,U.y=32/2/tan(25/114.5915590261),U=vcomb(255., trace(3,black,vunit(U)),black),printf "%.0f %.0f %.0f\n",U);}/\*minray!\*/

### Outline

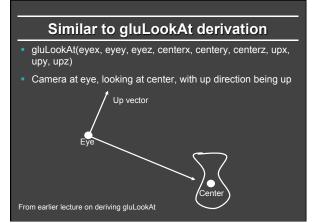
- Camera Ray Casting (choose ray directions)
- Ray-object intersections
- Ray-tracing transformed objects
- Lighting calculations
- Recursive ray tracing

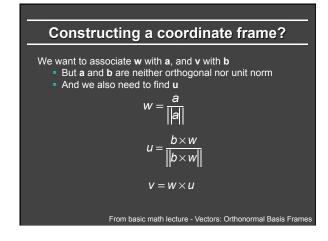


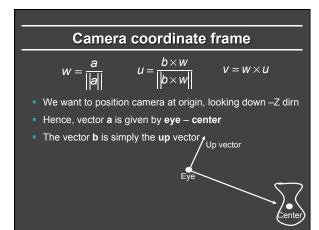


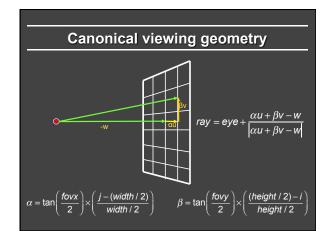
# **Finding Ray Direction**

- Goal is to find ray direction for given pixel i and j
- Many ways to approach problem Objects in world coord, find dirn of each ray (we do this) Camera in canonical frame, transform objects (OpenGL)
- Basic idea
  - Ray has origin (camera center) and direction Find direction given camera params and i and j
- Camera params as in gluLookAt Lookfrom[3], LookAt[3], up[3], fov









### Outline

- Camera Ray Casting (choosing ray directions)
- Ray-object intersections
- Ray-tracing transformed objects
- Lighting calculations
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 Outline in Code

 Image Raytrace (Camera cam, Scene scene, int width, int height) {

 Image image = new Image (width, height) ;

 for (int i = 0 ; i < height ; i++)</td>

 for (int j = 0 ; j < width ; j++) {</td>

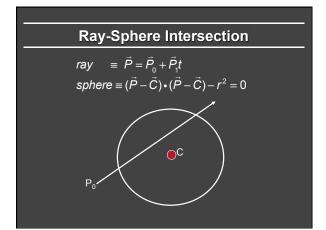
 Ray ray = RayThruPixel (cam, i, j) ;

 Intersection hit = Intersect (ray, scene) ;

 image[i][j] = FindColor (hit) ;

 }

 return image ;



Ray-Sphere Intersection
$ray \equiv \vec{P} = \vec{P}_0 + \vec{P}_1 t$
sphere $\equiv (\vec{P} - \vec{C}) \cdot (\vec{P} - \vec{C}) - r^2 = 0$
Substitute
$ray \equiv \vec{P} = \vec{P}_0 + \vec{P}_1 t$
sphere $\equiv (\vec{P}_{0} + \vec{P}_{1}t - \vec{C}) \cdot (\vec{P}_{0} + \vec{P}_{1}t - \vec{C}) - r^{2} = 0$
Simplify
$t^{2}(\vec{P}_{1} \bullet \vec{P}_{1}) + 2t \vec{P}_{1} \bullet (\vec{P}_{0} - \vec{C}) + (\vec{P}_{0} - \vec{C}) \bullet (\vec{P}_{0} - \vec{C}) - r^{2} = 0$

# **Ray-Sphere Intersection** $t^{2}(\vec{P_{1}} \cdot \vec{P_{1}}) + 2t \vec{P_{1}} \cdot (\vec{P_{0}} - \vec{C}) + (\vec{P_{0}} - \vec{C}) \cdot (\vec{P_{0}} - \vec{C}) - \underline{r}^{2} = 0$

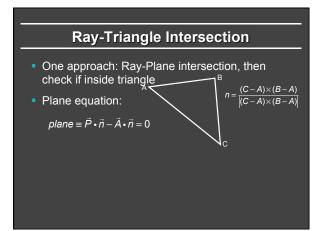
Solve quadratic equations for t

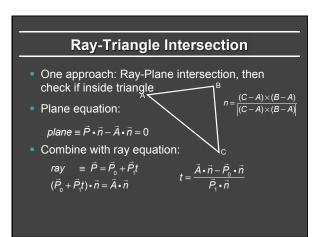
- 2 real positive roots: pick smaller root
- Both roots same: tangent to sphere
- One positive, one negative root: ray origin inside sphere (pick + root)
- Complex roots: no intersection (check discriminant of equation first)

### **Ray-Sphere Intersection**

- Intersection point:  $ray \equiv \vec{P} = \vec{P}_0 + \vec{P}_1 t$
- Normal (for sphere, this is same as coordinates in sphere frame of reference, useful other tasks)

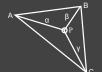
normal = 
$$\frac{\vec{P} - \vec{C}}{|\vec{P} - \vec{C}|}$$



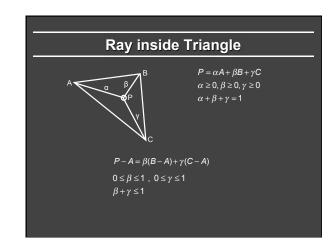


# **Ray inside Triangle**

- Once intersect with plane, still need to find if in triangle
- Many possibilities for triangles, general polygons (point in polygon tests)
- We find parametrically [barycentric coordinates]. Also useful for other applications (texture mapping)

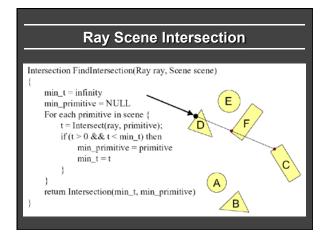


 $P = \alpha A + \beta B + \gamma C$   $\alpha \ge 0, \beta \ge 0, \gamma \ge 0$  $\alpha + \beta + \gamma = 1$ 



### Other primitives

- Much early work in ray tracing focused on rayprimitive intersection tests
- Cones, cylinders, ellipsoids
- Boxes (especially useful for bounding boxes)
- General planar polygons
- Many more
- Consult chapter in Glassner (handed out) for more details and possible extra credit



#### Outline

- Camera Ray Casting (choosing ray directions)
- Ray-object intersections
- Ray-tracing transformed objects
- Lighting calculations
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### **Transformed Objects**

- E.g. transform sphere into ellipsoid
- Could develop routine to trace ellipsoid (compute parameters after transformation)
- May be useful for triangles, since triangle after transformation is still a triangle in any case
- But can also use original optimized routines

### **Ray-Tracing Transformed Objects**

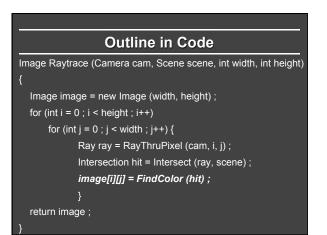
- We have an optimized ray-sphere test But we want to ray trace an ellipsoid...
- Solution: Ellipsoid transforms sphere
  - Apply inverse transform to ray, use ray-sphere
  - Allows for instancing (traffic jam of cars)
    Same idea for other primitives

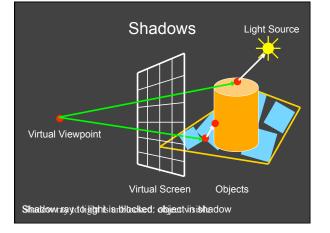
### **Transformed Objects**

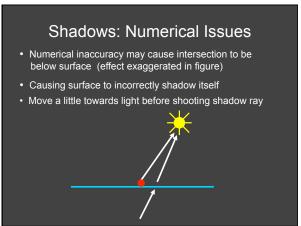
- Consider a general 4x4 transform M Will need to implement matrix stacks like in OpenGL
- Apply inverse transform M<sup>-1</sup> to ray Locations stored and transform in homogeneous coordinates
  - Vectors (ray directions) have homogeneous coordinate set to 0 [so there is no action because of translations]
- Do standard ray-surface intersection as modified
- Transform intersection back to actual coordinates Intersection point p transforms as Mp
  - Distance to intersection if used may need recalculation
     Normals n transform as M<sup>-1</sup>n. Do all this before lighting

### Outline

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# **Lighting Model**

- Similar to OpenGL
- Lighting model parameters (global)
  - Ambient r g b
  - Attenuation const linear quadratic

$$L = \frac{L_0}{const + lin^* d + quad^* d^2}$$

- Per light model parameters
  - Directional light (direction, RGB parameters)
  - Point light (location, RGB parameters)
    Some differences from HW 2 syntax

### **Material Model**

- Diffuse reflectance (r g b)
- Specular reflectance (r g b)
- Shininess s
- Emission (r g b)
- All as in OpenGL

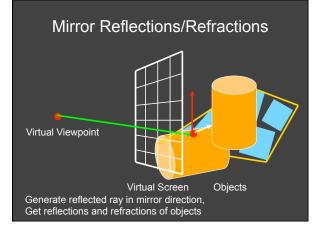
# **Shading Model**

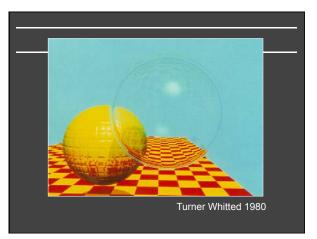
$$I = K_{a} + K_{e} + \sum_{i=1}^{n} V_{i} L_{i} (K_{d} \max (I_{i} \bullet n, 0) + K_{s} (\max(h_{i} \bullet n, 0))^{s})$$

- Global ambient term, emission from material
- For each light, diffuse specular terms
- Note visibility/shadowing for each light (not in OpenGL)
- Evaluated per pixel per light (not per vertex)

# Outline

- Camera Ray Casting (choosing ray directions)
- Ray-object intersections
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#### **Basic idea**

#### For each pixel

- Trace Primary Eye Ray, find intersection
- Trace Secondary Shadow Ray(s) to all light(s)
   Color = Visible ? Illumination Model : 0 ;
- Trace Reflected Ray
   Color += reflectivity \* Color of reflected ray

## **Recursive Shading Model**

$$\mathbf{Y} = \mathbf{K}_{a} + \mathbf{K}_{e} + \sum_{i=1}^{m} \mathbf{V}_{i} L_{i} (\mathbf{K}_{d} \max (I_{i} \cdot \mathbf{n}, 0) + \mathbf{K}_{s} (\max(h_{i} \cdot \mathbf{n}, 0))^{s}) + \mathbf{K}_{s} I_{R} + \mathbf{K}_{T} I_{R}$$

- Highlighted terms are recursive specularities [mirror reflections] and transmission (latter is extra credit)
- Trace secondary rays for mirror reflections and refractions, include contribution in lighting model
- GetColor calls RayTrace recursively (the I values in equation above of secondary rays are obtained by recursive calls)

### Problems with Recursion

- Reflection rays may be traced forever
- Generally, set maximum recursion depth
- Same for transmitted rays (take refraction into account)

# Effects needed for Realism

- (Soft) Shadows
- Reflections (Mirrors and Glossy)
- Transparency (Water, Glass)
- Interreflections (Color Bleeding)
- Complex Illumination (Natural, Area Light)
- Realistic Materials (Velvet, Paints, Glass)

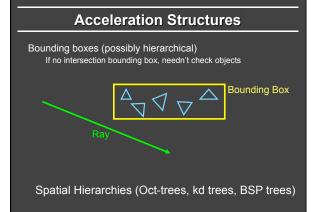
Discussed in this lecture so far Not discussed but possible with distribution ray tracing Hard (but not impossible) with ray tracing; radiosity methods

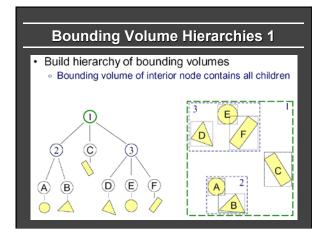
#### Some basic add ons

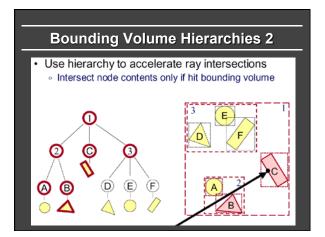
- Area light sources and soft shadows: break into grid of n x n point lights
  - Use jittering: Randomize direction of shadow ray within small box for given light source direction
  - Jittering also useful for antialiasing shadows when shooting primary rays
- More complex reflectance models
  - Simply update shading model
  - But at present, we can handle only mirror global illumination calculations

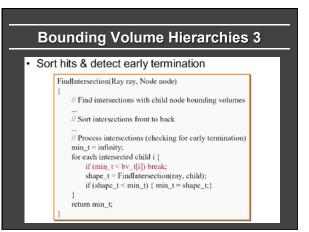
#### Acceleration

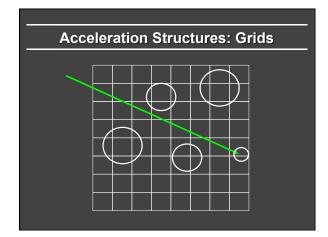
- Testing each object for each ray is slow
  - Fewer Rays Adaptive search
  - Adaptive sampling, depth control Generalized Rays
  - Beam tracing, cone tracing, pencil tracing etc.
  - Faster Intersections \_\_\_\_\_
    - Optimized Ray-Object Intersections
    - Fewer Intersections

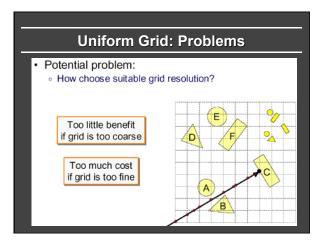


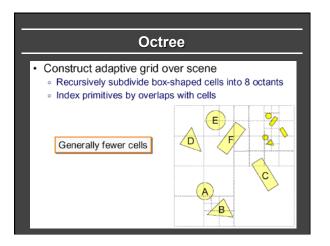


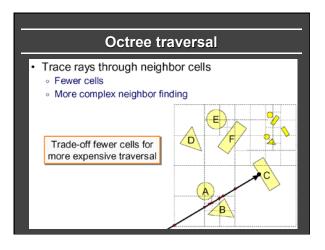


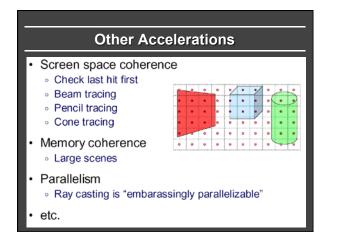






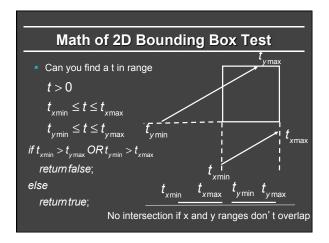


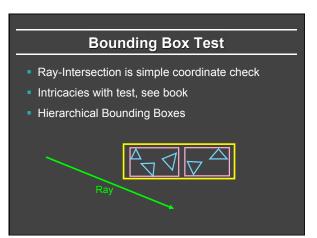




# Ray Tracing Acceleration Structures

- Bounding Volume Hierarchies (BVH)
- Uniform Spatial Subdivision (Grids)
- Binary Space Partitioning (BSP Trees)
   Axis-aligned often for ray tracing: kd-trees
- Conceptually simple, implementation a bit tricky
   Lecture relatively high level: Start early, go to section
   Remember that acceleration a small part of grade
- See 12.3, 12.4 in book





## **Hierarchical Bounding Box Test**

- If ray hits root box
  - Intersect left subtree
  - Intersect right subtree
  - Merge intersections (find closest one)
- Standard hierarchical traversal
  - But caveat, since bounding boxes may overlap
- At leaf nodes, must intersect objects

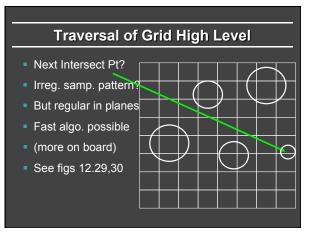
#### **Creating Bounding Volume Hierarchy**

function bvh-node::create (object array A, int AXIS)
 N = A.length();
 if (N == 1) {left = A[0]; right = NULL; bbox = bound(A[0]);}
 else if (N == 2) {
 left = A[0]; right = A[1];
 bbox = combine(bound(A[0]),bound(A[1]));
 else
 Find midpoint m of bounding box of A along AXIS
 Partition A into lists of size k and N-k around m
 left = new bvh-node (A[0...k],(AXIS+1) mod 3);
 right = new bvh-node(A[k+1...N-1],(AXIS+1) mod 3);
 bbox = combine (left -> bbox, right -> bbox);
 }

From page 285 of book

#### **Uniform Spatial Subdivision**

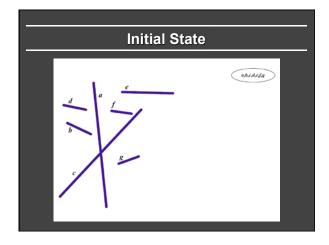
- Different idea: Divide space rather than objects
- In BVH, each object is in one of two sibling nodes
   A point in space may be inside both nodes
- In spatial subdivision, each space point in one node
   But object may lie in multiple spatial nodes
- Simplest is uniform grid (have seen this already)
- Challenge is keeping all objects within cell
- And in traversing the grid

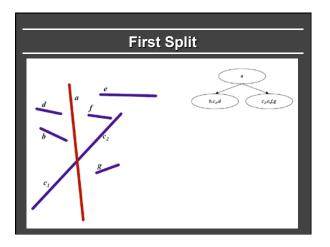


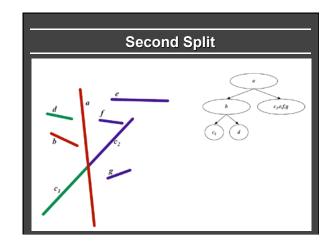
### **BSP Trees**

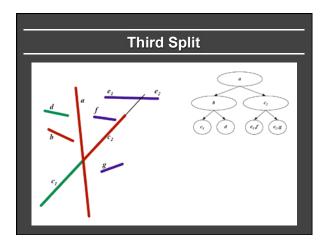
- Used for visibility and ray tracing
   Book considers only axis-aligned splits for ray tracing
   Sometimes called kd-tree for axis aligned
- Split space (binary space partition) along planes
- Fast queries and back-to-front (painter's) traversal
- Construction is conceptually simple
  - Select a plane as root of the sub-tree
  - Split into two children along this root
  - Random polygon for splitting plane (may need to split polygons that intersect it)

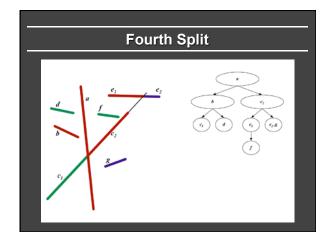
BSP slides courtesy Prof. O' Brien

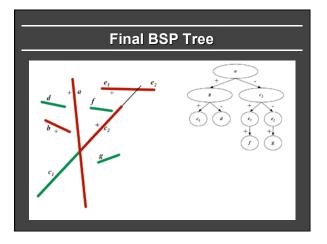












# BSP Trees Cont' d

- Continue splitting until leaf nodes
- Visibility traversal in order
   Child one
   Root

  - Child two
- Child one chosen based on viewpoint
   Same side of sub-tree as viewpoint
- BSP tree built once, used for all viewpoints
   More details in book

# **Interactive Raytracing**

- Ray tracing historically slow
- Now viable alternative for complex scenes
   Key is sublinear complexity with acceleration; need not process all triangles in scene
- Allows many effects hard in hardware
- OpenRT project real-time ray tracing (http:// www.openrt.de)

# **Raytracing on Graphics Hardware**

- Modern Programmable Hardware general streaming architecture
- Can map various elements of ray tracing
- Kernels like eye rays, intersect etc.
- In vertex or fragment programs
- Convergence between hardware, ray tracing
   [Purcell et al. 2002, 2003]

http://graphics.stanford.edu/papers/photongfx

