

Formal Relational Query Languages
Two mathematical Query Languages form the basis for "real" languages (e.g. SQL), and for implementation:
Relational Algebra: More operational, very useful for representing execution plans.

Relational Calculus: Lets users describe what they want, rather than how to compute it. (Non-procedural, declarative.)

- Understanding Algebra \& Calculus is key to understanding SQL, query processing!

Relational Query Languages

- Query languages: Allow manipulation and retrieval of data from a database.
- Relational model supports simple, powerful QLs:
- Strong formal foundation based on logic.
- Allows for much optimization.
- Query Languages != programming languages!
- QLs not expected to be "Turing complete".
- QLs not intended to be used for complex calculations.
- QLs support easy, efficient access to large data sets.


## Preliminaries

- A query is applied to relation instances, and the result of a query is also a relation instance.
- Schemas of input relations for a query are fixed (but query will run over any legal instance)
- The schema for the result of a given query is also fixed. It is determined by the definitions of the query language constructs.
- Positional vs. named-field notation:
- Positional notation easier for formal definitions, named-field notation more readable.
- Both used in SQL
- Though positional notation is not encouraged
- Selection ( $\sigma$ ) Selects a subset of rows from relation (horizontal).
- Projection ( $\pi$ ) Retains only wanted columns from relation (vertical).
- Cross-product $(\times)$ Allows us to combine two relations.
- Set-difference ( - ) Tuples in r1, but not in r2.
- Union ( $\cup$ ) Tuples in r1 or in r2.

Since each operation returns a relation, operations can be composed! (Algebra is "closed".)

Example Instances $R$

| $\underline{\text { sid }}$ | $\underline{\text { bid }}$ | $\underline{\text { day }}$ |
| :--- | :--- | :---: |
| 22 | 101 | $10 / 10 / 96$ |
| 58 | 103 | $11 / 12 / 96$ |

Boats

| bid | bname | color |
| :--- | :--- | :--- |
| 101 | Interlake | blue |
| 102 | Interlake | red |
| 103 | Clipper | green |
| 104 | Marine | red |

S1

| sid | sname | rating | age |
| :--- | :--- | :---: | :--- |
| 22 | dustin | 7 | 45.0 |
| 31 | lubber | 8 | 55.5 |
| 58 | rusty | 10 | 35.0 |

S2

| sid | sname | rating | age |
| :--- | :--- | :--- | :--- |
| 28 | yuppy | 9 | 35.0 |
| 31 | lubber | 8 | 55.5 |
| 44 | guppy | 5 | 35.0 |
| 58 | rusty | 10 | 35.0 |

## Projection ( $\pi$ )

- Examples: $\pi_{\text {age }}(S 2) ; \pi_{\text {sname,rating }}(S 2)$
- Retains only attributes that are in the "projection list".
- Schema of result:
- exactly the fields in the projection list, with the same names that they had in the input relation.
- Projection operator has to eliminate duplicates (How do they arise? Why remove them?)
- Note: real systems typically don't do duplicate elimination unless the user explicitly asks for it. (Why not?)


## Selection ( $\sigma$ )

- Selects rows that satisfy selection condition.
- Result is a relation.

Schema of result is same as that of the input relation.

- Do we need to do duplicate elimination?




## Union and Set-Difference

- Both of these operations take two input relations, which must be union-compatible:
- Same number of fields.
- 'Corresponding' fields have the same type.
- For which, if any, is duplicate elimination required?



## Cross-Product

- S1 $\times$ R1: Each row of S1 paired with each row of R1.
- Q: How many rows in the result?
- Result schema has one field per field of S1 and R1, with field names `inherited' if possible.
- May have a naming conflict: Both S1 and R1 have a field with the same name.
- In this case, can use the renaming operator.

$$
\rho(C(1 \rightarrow \operatorname{sid} 1,5 \rightarrow \operatorname{sid} 2), S 1 \times R 1)
$$

## Compound Operator: Intersection

- In addition to the 5 basic operators, there are several additional "Compound Operators"
- These add no computational power to the language, but are useful shorthands.
- Can be expressed solely with the basic ops.
- Intersection takes two input relations, which must be unioncompatible.
- Q: How to express it using basic operators?

$$
R \cap S=R-(R-S)
$$

## Compound Operator: Join

- Joins are compound operators involving cross product, selection, and (sometimes) projection.
- Most common type of join is a "natural join" (often just called "join"). R $\bowtie S$ conceptually is:
- Compute $\mathrm{R} \times \mathrm{S}$
- Select rows where attributes that appear in both relations
have equal values
- Project all unique atttributes and one copy of each of the common ones.
- Note: Usually done much more efficiently than this.


| Intersection |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| sid | sname | rating | age |  |  |  |  |
| 22 | dustin | 7 | 45.0 |  |  |  |  |
| 31 | lubber | 8 | 55.5 |  |  |  |  |
| 58 | rusty | 10 | 35.0 | sid | sname | rating | age |
| S1 |  |  |  | 31 58 | lubber rusty | $\begin{aligned} & \hline 8 \\ & 10 \end{aligned}$ | $\begin{aligned} & 55.5 \\ & 35.0 \end{aligned}$ |
| sid | sname | rating | age | $S 1 \cap S 2$ |  |  |  |
| 28 | yuppy | 9 | 35.0 |  |  |  |  |
| 31 | lubber | 8 | 55.5 |  |  |  |  |
| 44 | guppy | 5 | 35.0 |  |  |  |  |
| 58 | rusty | 10 | 35.0 |  |  |  |  |
| S2 |  |  |  |  |  |  |  |

Natural Join Example

| sid | $\underline{\text { bid }}$ | $\underline{\text { day }}$ |
| :--- | :--- | :---: |
| 22 | 101 | $10 / 10 / 96$ |
| 58 | 103 | $11 / 12 / 96$ |

R1

| $\underline{\text { sid }}$ | sname | rating | age |
| :--- | :--- | :---: | :--- |
| 22 | dustin | 7 | 45.0 |
| 31 | lubber | 8 | 55.5 |
| 58 | rusty | 10 | 35.0 |

S1
$\mathrm{S} 1 \bowtie \mathbf{R 1}=$

| sid | sname | rating | age | bid | day |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 22 | dustin | 7 | 45.0 | 101 | $10 / 10 / 96$ |
| 58 | rusty | 10 | 35.0 | 103 | $11 / 12 / 96$ |


| O Other Types of Joins |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| - Condition Join (or "theta-join"):$R \bowtie_{c} S=\sigma_{c}(R \times S)$ |  |  |  |  |  |  |
| (sid) | sname | rating | age | (sid) | bid | day |
| 22 | dustin | 7 | 45.0 | 58 | 103 | 11/12/96 |
| 31 | lubber | 8 | 55.5 | 58 | 103 | 11/12/96 |
| $S 1 \bowtie \underbrace{}_{S 1 \text { sid }<R 1 . s i d} R 1$ |  |  |  |  |  |  |
| - Result schema same as that of cross-product. <br> - May have fewer tuples than cross-product. <br> - Equi-Join: Special case: condition c contains only conjunction of equalities. |  |  |  |  |  |  |

Find names of sailors who've reserved boat \#103

- Solution 1: $\pi_{\text {sname }}\left(\left(\sigma_{\text {bid }=103}\right.\right.$ Reserves $) \bowtie$ Sailors $)$
- Solution 2: $\pi_{\text {sname }}\left(\sigma_{b i d=103}(\right.$ Reserves $\bowtie$ Sailors $\left.)\right)$


Find sailors who've reserved a red or a green boat

- Can identify all red or green boats, then find sailors who've reserved one of these boats:
$\rho$ (Tempboats, ( $\sigma_{\text {color }}=$ ' red' v color $=$ ' green' ${ }^{\text {Boats })}$ )
$\pi_{\text {sname }}{ }^{(\text {Tempboats } \bowtie \text { Reserves } \bowtie \text { Sailors })}$

Examples Reserves

| $\underline{\text { sid }}$ | $\underline{\text { bid }}$ | $\underline{\text { day }}$ |
| :---: | :--- | :---: |
| 22 | 101 | $10 / 10 / 96$ |
| 58 | 103 | $11 / 12 / 96$ |

Sailors

| sid | sname | rating | age |
| :--- | :--- | :--- | :--- |
| 22 | dustin | 7 | 45.0 |
| 31 | lubber | 8 | 55.5 |
| 58 | rusty | 10 | 35.0 |

Boats

| bid | bname | color |
| :--- | :--- | :--- |
| 101 | Interlake | Blue |
| 102 | Interlake | Red |
| 103 | Clipper | Green |
| 104 | Marine | Red |

Find names of sailors who've reserved a red boat

- Information about boat color only available in Boats; so need an extra join:
$\pi_{\text {sname }}\left(\left(\sigma_{\text {color }=\text { 'red }}{ }^{\prime}\right.\right.$ Boats $) \bowtie$ Reserves $\bowtie$ Sailors $)$
* A more efficient solution:
$\pi_{\text {sname }}\left(\pi_{\text {sid }}\left(\left(\pi_{\text {bid }} \sigma_{\text {color }=\text { 'red }}{ }^{\prime}\right.\right.\right.$ Boats $\left.) \bowtie \operatorname{Re} s\right) \bowtie$ Sailors $)$
- A query optimizer can find this given the first solution!

Find sailors who've reserved a red and a green boat

- Cut-and-paste previous slide?


Find sailors who've reserved a red and a green boat

- Previous approach won't work! Must identify sailors who've reserved red boats, sailors who've reserved green boats, then find the intersection (note that sid is a key for Sailors):
$\rho$ (Tempred, $\pi_{\text {sid }}\left(\left(\sigma_{\text {color }}=\right.\right.$ 'red ${ }^{\prime}$ Boats $) \bowtie$ Reserves $\left.)\right)$
$\rho$ (Tempgreen, $\pi_{\text {sid }}\left(\left(\sigma_{\text {color }}=\right.\right.$ green' $^{\prime}$ Boats $) \bowtie$ Reserves $\left.)\right)$
$\pi_{\text {sname }}(($ Tempred $\cap$ Tempgreen $) \bowtie$ Sailors $)$

Summary

- Relational Algebra: a small set of operators mapping relations to relations
- Operational, in the sense that you specify the explicit order of operations
- A closed set of operators! Can mix and match.
- Basic ops include: $\sigma, \pi, x, \cup,-$
- Important compound ops: $\cap, \bowtie$

