## Advanced Computer Graphics <br> (Fall 2009)

CS 294-13, Rendering Lecture 1: Introduction and Basic Ray Tracing

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## To Do

- Start working on raytracer assignment (if necessary)
- Start thinking about path tracer, final project

Ray Tracing History


## Outline

- Camera Ray Casting (choosing ray directions)
- Ray-object intersections
- Ray-tracing transformed objects
- Lighting calculations
- Recursive ray tracing


## Outline in Code

Image Raytrace (Camera cam, Scene scene, int width, int height)
\{
Image image = new Image (width, height) ;
for (int $\mathrm{i}=0 ; \mathrm{i}<$ height $; \mathrm{i}++$ )
for (int $\mathrm{j}=0 ; \mathrm{j}<$ width $; \mathrm{j}++$ ) $\{$
Ray ray = RayThruPixel (cam, i, j);
Intersection hit = Intersect (ray, scene) ;
image[i][j] = FindColor (hit) ;
\}
return image ;
\}


## Finding Ray Direction

- Goal is to find ray direction for given pixel i and j
- Many ways to approach problem
- Objects in world coord, find dirn of each ray (we do this)
- Camera in canonical frame, transform objects (OpenGL)
- Basic idea
- Ray has origin (camera center) and direction
- Find direction given camera params and i and j
- Camera params as in gluLookAt
- Lookfrom[3], LookAt[3], up[3], fov


Constructing a coordinate frame?
We want to associate $\mathbf{w}$ with $\mathbf{a}$, and $\mathbf{v}$ with $\mathbf{b}$

- But a and b are neither orthogonal nor unit norm
- And we also need to find $\mathbf{u}$

$$
\begin{aligned}
w & =\frac{a}{\|a\|} \\
u & =\frac{b \times w}{\|b \times w\|}
\end{aligned}
$$

$$
v=w \times u
$$

## Camera coordinate frame

$$
w=\frac{a}{\|a\|} \quad u=\frac{b \times w}{\|b \times w\|} \quad v=w \times u
$$

- We want to position camera at origin, looking down -Z dirn
- Hence, vector a is given by eye - center
- The vector b is simply the up vector Up vector



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## Outline in Code

```
Image Raytrace (Camera cam, Scene scene, int width, int height)
{
    Image image = new Image (width, height);
    for (int i= 0; i < height ; i++)
        for (int j= 0 ; j < width ; j++) {
            Ray ray = RayThruPixel (cam, i, j);
            Intersection hit = Intersect (ray, scene);
            image[i][j] = FindColor (hit) ;
            }
    return image ;
}
```

Ray-Sphere Intersection
ray $\equiv \vec{P}=\vec{P}_{0}+\vec{P}_{1} t$
sphere $\equiv(\vec{P}-\vec{C}) \cdot(\vec{P}-\vec{C})-r^{2}=0$


## Ray-Sphere Intersection

$$
\begin{aligned}
& \text { ray } \equiv \vec{P}=\vec{P}_{0}+\vec{P}_{1} t \\
& \text { sphere } \equiv(\vec{P}-\vec{C}) \cdot(\vec{P}-\vec{C})-r^{2}=0
\end{aligned}
$$

Substitute

$$
\begin{aligned}
& \text { ray } \equiv \vec{P}=\vec{P}_{0}+\vec{P}_{1} t \\
& \text { sphere } \equiv\left(\vec{P}_{0}+\vec{P}_{1} t-\vec{C}\right) \cdot\left(\vec{P}_{0}+\vec{P}_{1} t-\vec{C}\right)-r^{2}=0
\end{aligned}
$$

Simplify

$$
t^{2}\left(\vec{P}_{1} \cdot \vec{P}_{1}\right)+2 t \vec{P}_{1} \bullet\left(\vec{P}_{0}-\vec{C}\right)+\left(\vec{P}_{0}-\vec{C}\right) \cdot\left(\vec{P}_{0}-\vec{C}\right)-r^{2}=0
$$

## Ray-Sphere Intersection

$t^{2}\left(\vec{P}_{1} \cdot \vec{P}_{1}\right)+2 t \vec{P}_{1} \bullet\left(\vec{P}_{0}-\vec{C}\right)+\left(\vec{P}_{0}-\vec{C}\right) \cdot\left(\vec{P}_{0}-\vec{C}\right)-r^{2}=0$
Solve quadratic equations for $t$

- 2 real positive roots: pick smaller root
- Both roots same: tangent to sphere
- One positive, one negative root: ray origin inside sphere (pick + root)
- Complex roots: no intersection (check discriminant of equation first)



## Ray-Triangle Intersection

- One approach: Ray-Plane intersection, then check if inside triangle
- Plane equation:

$$
\text { plane } \equiv \vec{P} \cdot \vec{n}-\vec{A} \cdot \vec{n}=0
$$



## Ray-Triangle Intersection

- One approach: Ray-Plane intersection, then check if inside triangle
- Plane equation:

- Combine with ray equation:

$$
\begin{array}{ll}
\operatorname{ray} \equiv \vec{P}=\vec{P}_{0}+\vec{P}_{1} t \\
\left(\vec{P}_{0}+\vec{P}_{1} t\right) \cdot \vec{n}=\vec{A} \cdot \vec{n} & t=\frac{\vec{A} \cdot \vec{n}-\vec{P}_{0} \cdot \vec{n}}{\vec{P}_{1} \cdot \vec{n}}
\end{array}
$$



## Other primitives

## Ray Scene Intersection

- Much early work in ray tracing focused on rayprimitive intersection tests
- Cones, cylinders, ellipsoides
- Boxes (especially useful for bounding boxes)
- General planar polygons
- Many more
- Many references. For example, chapter in Glassner introduction to ray tracing (see me if interested)



## Transformed Objects

- E.g. transform sphere into ellipsoid
- Could develop routine to trace ellipsoid (compute parameters after transformation)
- May be useful for triangles, since triangle after transformation is still a triangle in any case
- But can also use original optimized routines


## Transformed Objects

- Consider a general $4 \times 4$ transform M
- Will need to implement matrix stacks like in OpenGL
- Apply inverse transform $\mathrm{M}^{-1}$ to ray
" Locations stored and transform in homogeneous coordinates
- Vectors (ray directions) have homogeneous coordinate set to 0 [so there is no action because of translations]
- Do standard ray-surface intersection as modified
- Transform intersection back to actual coordinates
- Intersection point p transforms as Mp
- Distance to intersection if used may need recalculation
" Normals n transform as $\mathrm{M}^{-\mathrm{t}} \mathrm{n}$. Do all this before lighting


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## Shadows: Numerical Issues

- Numerical inaccuracy may cause intersection to be below surface (effect exaggerated in figure)
- Causing surface to incorrectly shadow itself
- Move a little towards light before shooting shadow ray



## Lighting Model

- Similar to OpenGL
- Lighting model parameters (global)
- Ambient r g b (no per-light ambient as in OpenGL)
- Attenuation const linear quadratic (like in OpenGL)

$$
L=\frac{L_{0}}{\text { const }+ \text { lin } d+\text { quad } * d^{2}}
$$

- Per light model parameters
- Directional light (direction, RGB parameters)
- Point light (location, RGB parameters)


## Shading Model

$I=K_{a}+K_{e}+\sum_{i=1}^{n} L_{i}\left(K_{d} \max \left(l_{i} \bullet n, 0\right)+K_{s}\left(\max \left(h_{i} \bullet n, 0\right)\right)^{s}\right)$

- Global ambient term, emission from material
- For each light, diffuse specular terms
- Note visibility/shadowing for each light (not in OpenGL)
- Evaluated per pixel per light (not per vertex)



## Basic idea

## For each pixel

- Trace Primary Eye Ray, find intersection
- Trace Secondary Shadow Ray(s) to all light(s)

$$
\text { - Color }=\text { Visible } ? \text { Illumination Model : } 0
$$

- Trace Reflected Ray
- Color $+=$ reflectivity * Color of reflected ray



## Problems with Recursion

- Reflection rays may be traced forever
- Generally, set maximum recursion depth
- Same for transmitted rays (take refraction into account)


## Effects needed for Realism

- (Soft) Shadows
- Reflections (Mirrors and Glossy)
- Transparency (Water, Glass)
- Interreflections (Color Bleeding)
- Complex Illumination (Natural, Area Light)
- Realistic Materials (Velvet, Paints, Glass)

Discussed in this lecture so far
Not discussed but possible with distribution ray tracing
Hard (but not impossible) with ray tracing; radiosity methods


## Some basic add ons

- Area light sources and soft shadows: break into grid of $n \times n$ point lights
- Use jittering: Randomize direction of shadow ray within small box for given light source direction
- Jittering also useful for antialiasing shadows when shooting primary rays
- More complex reflectance models
- Simply update shading model
- But at present, we can handle only mirror global illumination calculations


Bounding Volume Hierarchies 3

## - Sort hits \& detect early termination

```
FindIntersection(Ray ray, Node node)
    // Find intersections with child node bounding volumes
    // Sort intersections front to back
    // Process intersections (checking for early termination)
    min_t = infinity;
    for each intersected child i;
            if (min_t < bv_t[i]) break;
            shape_t = FindIntersection(ray, child):
            if (shape_t < min_t) { min_t = shape_t;}
    return min_t;
```



## Octree

- Construct adaptive grid over scene
- Recursively subdivide box-shaped cells into 8 octants
- Index primitives by overlaps with cells

Generally fewer cells


## Other Accelerations

- Screen space coherence
- Check last hit first
- Beam tracing
- Pencil tracing
- Cone tracing
- Memory coherence

- Large scenes
- Parallelism
- Ray casting is "embarassingly parallelizable"
- etc.


## Interactive Raytracing

- Ray tracing historically slow
- Now viable alternative for complex scenes
- Key is sublinear complexity with acceleration; need not process all triangles in scene
- Allows many effects hard in hardware
- OpenRT project real-time ray tracing (http://www.openrt.de)



## Raytracing on Graphics Hardware

- Modern Programmable Hardware general streaming architecture
- Can map various elements of ray tracing
- Kernels like eye rays, intersect etc.
- In vertex or fragment programs
- Convergence between hardware, ray tracing - NVIDIA now has CUDA-based raytracing API!
[Purcell et al. 2002, 2003]
http://graphics.stanford.edu/papers/photongfx

