

CS61A Lecture 12

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(calc) review

(scheme-1) has
lambda but NOT
define



Remember calc-apply?

```
STk> (calc-apply '+ '(1 2 3))
6
STk> (calc-apply '* '(2 4 3))
24
STk> (calc-apply '/ '(10 2))
5
STk> (calc-apply '- '(9 2 3 1))
3
```



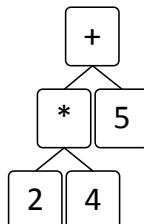
(calc) read-eval-print loop

```
(define (calc)
  (display "calc: ")
  (flush)
  (print (calc-eval (read)))
  (calc))
```



calc-eval

```
STk> (calc)
calc: (+ (* 2 4) 5)
13
(define (calc-eval exp)
  (cond
    ((number? exp) exp)
    ((list? exp)
      (calc-apply
        (car exp)
        (map calc-eval (cdr exp)))))
    (else (error "Calc: bad exp"))))
```



(scheme-1)

DOES NOT HAVE DEFINE!

STk> (scheme-1)

Scheme-1: (lambda (x) (* x x))
(lambda (x) (* x x))

Scheme-1: ((lambda (x) (* x x)) 3)
9



Working with large programs!

- Start with small functions
- Understanding code
 - Read it
 - Recursively figure out any functions it calls
 - Try to call the function to see what it does in different cases
 - Trace the function and try to call it from the functions that call it.

Cal

Approximate hierarchy of calls

scheme-1			
apply-1			eval-1
substitute			
lookup			
maybe-quote			
lambda-exp?	if-exp?	quote-exp?	constant?
exp-checker		number?	boolean?
		string?	procedure?

Cal

lambda-exp?

```
STk> (lambda-exp? '(lambda (x) (+ x 2)))
#t
STk> (lambda-exp? '+)
#f
STk> (lambda-exp? 'lambda)
#f
STk> (lambda-exp? '(lambda (x) (+ x 2)))
#t
```

It isn't as picky as we might hope...

Cal

Write lambda-exp? in terms of exp-checker

```
(define (exp-checker type)
  (lambda (exp)
    (and
      (pair? exp)
      (eq? (car exp) type))))
```

(lambda-exp? '(lambda (x) (+ x 2)))

Did you write it with syntactic sugar? A) Yes B) No

Cal

Some Helpers

```
(define quote-exp?
  (exp-checker 'quote))
(define if-exp?
  (exp-checker 'if))
(define (constant? exp)
  (or (number? exp)
      (boolean? exp)
      (string? exp)
      (procedure? exp)))
```

Cal

What is string?

```
STk> (string? "hello")
#t
STk> (string? 123)
#f
STk> (string? 'hello)
#f
```

Cal

(lookup name params args)

```
STk> (lookup 'x      '(x)      '(3))
3
STk> (lookup 'y      '(x y)    '(2 3))
3
STk> (lookup 'y      '(x)      '(3))
y
STk> (lookup '*      '(x)      '(3))
*
```

Just returns it if it isn't in there

Cal

lookup full functionality

```
STk> (lookup 'fn
              '(x fn)
              '(3 (lambda (y) (* y y))))
(lambda (y) (* y y))
```

```
STk> (lookup 'x '(x) '(cat))
```

(quote cat) cat was already a word, but we want to tell other people this thing IS ACTUALLY a word

This already works

Cal

Full lookup

```
(define (lookup name params args)
  (cond
    ((null? params) name)
    ((eq? name (car params))
     (maybe-quote (car args)))
    (else
      (lookup name
              (cdr params)
              (cdr args)))))
```

Cal

maybe-quote

```
(define (maybe-quote value)
  (cond
    ((lambda-exp? value) value)
    ((constant? value) value)
    ((procedure? value) value)
    (else (list 'quote value))))
```

Cal

Substitution using substitute

(substitute exp params args bound)

```
STk> ((lambda (x) (* x x)) 3)
9
STk> (substitute '(* x x) '(x) '(3) '())
(* 3 3)
STk> ((lambda (x y) (+ x y)) 3 4)
7
STk> (substitute [ ] [ ] [ ] '())
(+ 3 4)
```

Cal

(substitute exp params args bound)

```
STk> ((lambda (x)
              (lambda (y) (* x y)))
        3)
```

What does this return?

```
STk> (substitute
```

[]
[]
[]
'()

Cal

Scheme substitution review

```
STk> ((lambda (x)
    (lambda (x)
        (* x x)) )
4)
#[closure arglist=(x) 7ff1a1f8]
STk> (((lambda (x)
    (lambda (x)
        (* x x)))
4)
3)
```

What does this return? A) 9 B) 16 C)??

(**substitute exp params args bound**)

```
STk> ((lambda (x)
    (lambda (x)
        (* x x)) )
4)
#[closure arglist=(x) 7ff1a1f8]
STk> (substitute
      _____
      _____
      _____
      _____
      '())
      _____
```

Cal

(apply-1 proc args)

```
STk> (apply-1 + '(3 4))
7
STk> (apply-1
      '(lambda (x) (* x x))
      '())
9
```

Unlike calc-apply
apply-1 can be called
with REAL scheme functions

Or lists representing functions
Remember lambda-exp???

apply-1

```
(define (apply-1 proc args)
  (cond
    (procedure? proc)
    (apply proc args))
  ((lambda-exp? proc)
   (eval-1 (substitute
            _____
            _____
            _____
            _____
            '())))
  (else (error "bad proc:" proc)))
  (substitute exp params args bound))
```

scheme-1

```
(define (scheme-1)
  (display "Scheme-1: ")
  (flush)
  (print (eval-1 (read)))
  (scheme-1))
```

eval-1

```
STk> (eval-1 5)
5
      (cond
        ((constant? exp) exp))

STk> (eval-1 '+)
#[closure arglist=exp 7ff53de8]

      (cond
        ((symbol? exp) (eval exp)))
```

eval-1

```
STk> (eval-1 '(if (> 3 4) 5 7))
7
```

```
(cond
  ((if-exp? exp)
   (if (eval-1 (cadr exp))
       (eval-1 (caddr exp))
       (eval-1 (cadddr exp))))
```

*Cal***eval-1**

```
STk> (eval-1 'x)
*** Error:
unbound variable: x
Current eval stack:
```

0	x
1	(eval exp)

Things like + are quoted: '+
when they are passed to
eval-1 so this assumes x
will be a variable not a word.

*Cal***eval-1 with words**

```
STk> (eval-1 '(quote x))
x
```

```
STk> (eval-1 (quote (quote x)))
x (cond
  ((quote-exp? exp) (cadr exp)))
```

```
STk> (eval-1 "'x")
x
```

These are all equivalent!

*Cal***eval-1**

```
STk> (eval-1 '(lambda (x) (* x x)))
(lambda (x) (* x x))
```

```
(cond
  ((lambda-exp? exp) exp))
```

Cal

```
(define (eval-1 exp)
```

```
(cond
  ((constant? exp) exp)
  ((symbol? exp) (eval exp))
  ((quote-exp? exp) (cadr exp))
  ((if-exp? exp)
   (if (eval-1 (cadr exp))
       (eval-1 (caddr exp))
       (eval-1 (cadddr exp))))
  ((lambda-exp? exp) exp)
  ((pair? exp) _____)
  (else (error "?!?" exp))))
```

Cal

(cond ((pair? exp) _____))

```
STk> (eval-1 '(+ 2 3))
5
```

```
STk> (eval-1 '(+ (- 3 1) 5))
7
```

```
STk> (eval-1 '((lambda (x) (* x x)) 3))
9
```

Cal

```
(cond ((pair? exp) _____))
```

```
(cond
  ((pair? exp)
   (apply-1
    (eval-1 (car exp))
    (map eval-1 (cdr exp)))))

STk> (eval-1 '(+ 2 3))
STk> (eval-1 '(+ (- 3 1) 5))
STk> (eval-1 '((lambda (x) (* x x)) 3))
```

Cal

lambda-exp? Solution

```
(define (exp-checker type)
  (lambda (exp)
    (and
      (pair? exp)
      (eq? (car exp) type)))))

(define (lambda-exp? exp)
  ((exp-checker 'lambda) exp))

(define lambda-exp?
  (exp-checker 'lambda))
```

Write lookup (some functionality missing)

```
(define (lookup name params args)
  (cond
    ((null? params) name)
    ((eq? name (car params))
     (car args))
    (else
      (lookup name
              (cdr params)
              (cdr args)))))
```

Cal

Substitution using substitute

(substitute exp params args bound)

```
STk> ((lambda (x) (* x x)) 3)
9
STk> (substitute '(* x x) '(x) '(3) '())
(* 3 3)
STk> ((lambda (x y) (+ x y)) 3 4)
7
STk> (substitute '(+ x y) '(x y) '(3 4) '())
(+ 3 4)
```

Cal

(substitute exp params args bound)

```
STk> ((lambda (x)
            (lambda (y) (* x y)))
       3)

What does this return?
#[closure arglist=(y) 7ff1cc48]

A procedure that takes argument y and adds 3 to it
STk> (substitute
         '(lambda (y) (* x y))
         '(x)
         '(3)
         '())
(lambda (y) (* 3 y))
```

Cal

(substitute exp params args bound)

```
STk> ((lambda (x)
            (lambda (x)
              (* x x)))
       4)

#[closure arglist=(x) 7ff1a1f8]

STk> (substitute
         ' (lambda (x) (* x x))
         '(x)
         '(4)
         '())
(lambda (x) (* x x))
```

A recursive call

will be made

where bound

will be '(x)

'(4)

'()

Cal