

### **Digital Design Basics (1/2)**

- Next 3 weeks: we'll study how a modern processor is built starting with basic logic elements as building blocks.
- Why study logic design?
  - Understand what processors can do fast and what they can't do fast (avoid slow things if you want your code to run fast!)
  - Background for more detailed hardware courses (CS 150, CS 152)



## **Digital Design Basics (2/2)**

- ISA is very important abstraction layer
  - Contract between HW and SW
  - Can you peek across abstraction?
  - Can you depend "across abstraction"?
- Voltages are analog, quantized to 0/1
- Circuit delays are fact of life
- Two types
  - Stateless Combinational Logic (&,|,~)
  - State circuits (e.g., registers)

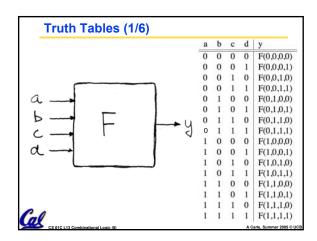
CS 61C L13 Combinational Logic (6

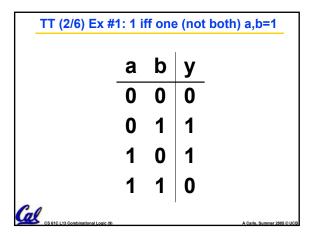
A Carle, Summer 2005 © UCB

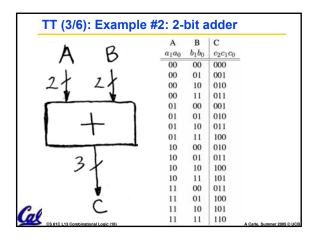


- Truth Tables
- Transistors
- Logic Gates
- Combinational Logic
- Boolean Algebra

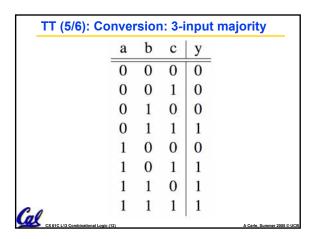


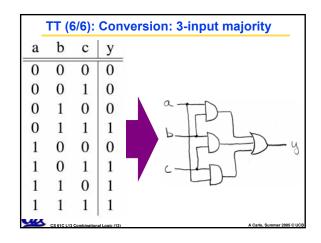


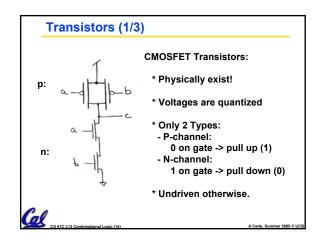


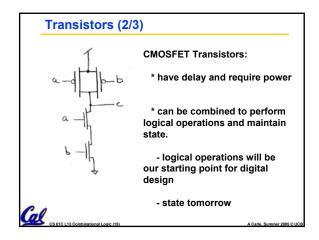


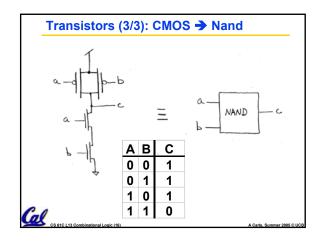
TT (4/6): Ex #3: 32-bit unsigned adder		
A	В	C
000 0	000 0	000 00
000 0	000 1	000 01
	•	į•
•	•	•
	85•3	
111 1	111 1	111 10
Cal CS 84C L13 Combinational Logic (1		A Carla Summer 2008 © HC







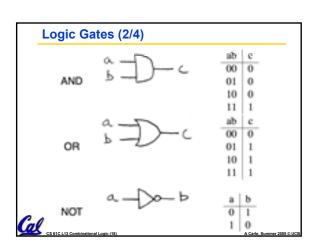


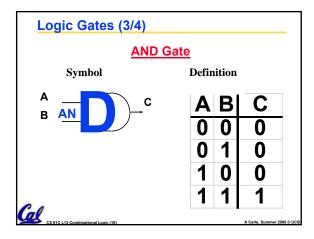


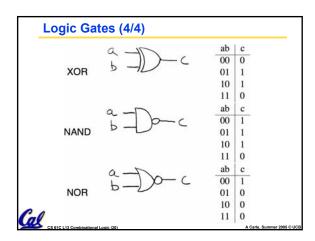
### Logic Gates (1/4)

- Transistors are too low level
  - Good for measuring performance, power.
  - · Bad for logical design / analysis
- Gates are collections of transistors wired in a certain way
  - Can represent and reason about gates with truth tables and Boolean algebra
  - We will mainly review the concepts of truth tables and Boolean algebra in this class. It is assumed that you've seen these before.

• Section B.2 in the textbook has a review

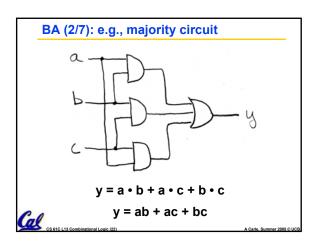


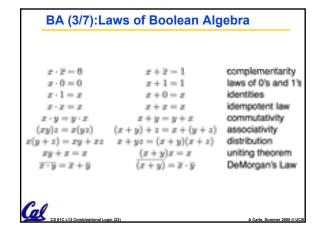


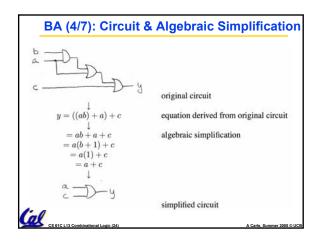


## Boolean Algebra (1/7)

- George Boole, 19<sup>th</sup> Century mathematician
- Developed a mathematical system (algebra) involving logic, later known as "Boolean Algebra"
- Primitive functions: AND, OR and NOT
- The power of BA is there's a one-to-one correspondence between circuits made up of AND, OR and NOT gates and equations in BA
- + means OR,• means AND, x means NOT





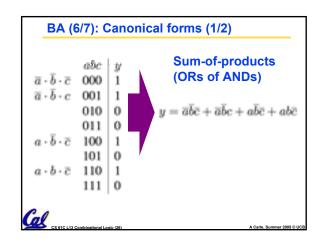


#### **BA (5/7): Simplification Example**

$$y = ab + a + c$$
  
=  $a(b+1) + c$  distribution, identity  
=  $a(1) + c$  law of 1's  
=  $a + c$  identity

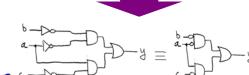


rle, Summer 2005 ©



## BA (7/7): Canonical forms (2/2)

$$\begin{array}{ll} y &= \overline{a}\overline{b}\overline{c} + \overline{a}\overline{b}c + a\overline{b}\overline{c} + ab\overline{c} \\ &= \overline{a}\overline{b}(\overline{c} + c) + a\overline{c}(\overline{b} + b) & \textit{distribution} \\ &= \overline{a}\overline{b}(1) + a\overline{c}(1) & \textit{complementarity} \\ &= \overline{a}\overline{b} + a\overline{c} & \textit{identity} \end{array}$$



Cal CS SICLIS

## Combinational Logic

A combinational logic block is one in which the output is a function only of its current input.

- Combinational logic cannot have memory.
- Everything we've seen so far is CL
- CL will have delay ( f(transistors) )
  - More later.

# Peer Instruction

- A.  $(a+b) \cdot (a+b) = b$
- B. N-input gates can be thought of as cascaded 2-input gates. I.e., (a  $\triangle$  bc  $\triangle$  d  $\triangle$  e) = a  $\triangle$  (bc  $\triangle$  (d  $\triangle$  e)) where  $\triangle$  is one of AND, OR, XOR, NAND
- C. You can use NOR(s) with clever wiring to simulate AND, OR, & NOT



A Carle, Summer 2005 © UC

#### "And In conclusion..."

 Use this table and techniques we learned to transform from 1 to another

