## CS 70

Discrete Mathematics and Probability Theory
Spring 2016 Walrand and Rao

## 1. Markov Chain Terminology Test

For each of the following Markov chains, determine if it is (a) periodic and/or (b) reducible.
(a)

(b)

(c)


## 2. Number of Ones

In this problem, we will revisit dice-rolling, except with conditional expectation.
(a) If we roll a die until we see a 6 , how many ones should we expect to see?
(b) If we roll a die until we see a number greater than 3 , how many ones should we expect to see?
(c) We add $r$ red marbles, $b$ blue marbles and $g$ green marbles to the same bag. If we sample balls, with replacement, until we get 3 red marbles (not necessarily consecutively), how many blue marbles should we expect to see?

