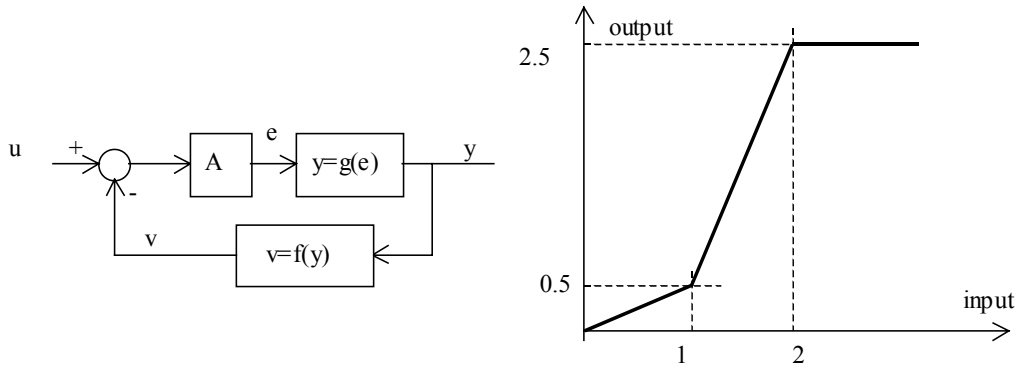


Due on 9/15/04 (before the Wednesday lab session)

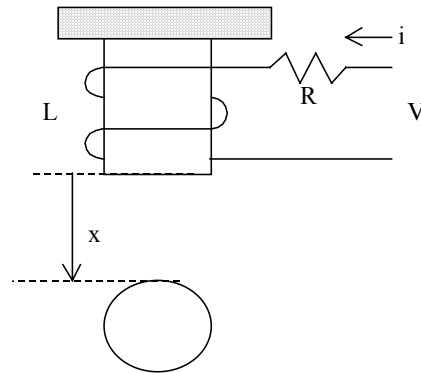
Consider the following feedback system where u is the input and y is the output.

- (1) Assume $v=y$ (i.e., $f(\cdot)$ is the identity function), $A=20$, and the graph of the function g is shown below. Sketchy the y vs. u graph. The y variable in your graph must cover the interval $[0\ 3]$ and you must specify the coordinate of any 'break point' of the graph.
- (2) Assume $y=e$ (i.e., $g(\cdot)$ is the identity function), $A=20$, and the graph of the function f is shown below. Sketchy the y vs. u graph. The y variable in your graph must cover the interval $[0\ 3]$ and you must specify the coordinate of any 'break point' of the graph.
- (3) Repeat the (1) and (2) but assume $A \rightarrow \infty$.
- (4) The function $g(\cdot)$ can be thought of as the 'plant' and $f(\cdot)$ as the sensor. Draw some conclusions from the above analysis on the magnitude of A and the effect of $f(\cdot)$ on the transfer function (i.e., graph) of y vs. u .



- (2) The figure on the right shows a ball suspension system. The steel ball is suspended in the air by the electromagnetic force generated by the electromagnet.

The magnetic force acting on the ball is $F=(k \cdot i^2)/x^2$, the mass of the ball is m . Gravitational constant is g . The inductance of the magnet is L and the resistance of the magnet winding is R (as represented by a resistor in the figure). Using the state vector x defined below, write a nonlinear state equation (V is the input and x is the output variable).



$X=[i, x, v]$ where v is the speed of ball.

- (3) Problem 2.23 in the textbook.
- (4) Draw a block diagram of the motor system in Problem 2.23.
- (5) If the armature circuit of a DC motor is driven by a controlled current source, the effects of armature winding resistance (R_a), armature inductance (L_a), and the back emf (K_e) are completely nullified. In such a case, the armature current i_a should be considered as the input variable. Assume the motor in Problem 2.23 is driven by a controlled current source (i_a). Find the transfer function between i_a and θ_2 . (Hint: This is a 4th order transfer function.)