

**This homework is due November 16, 2017, at noon.**

**1. Interpolation**

Samples from the sinusoid  $f(x) = \sin(0.2\pi x)$  are shown in Figure 1. Draw the results of interpolation using each of the following three methods:

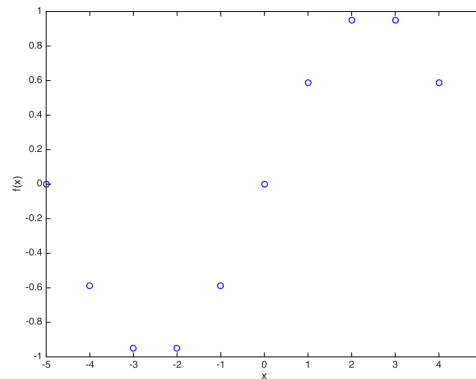


Figure 1: Samples of  $f(x)$ .

- (a) Zero order hold interpolation.
- (b) Linear interpolation.
- (c) Sinc interpolation assuming the Nyquist limit has been satisfied.

**2. Polynomial interpolation and regression**

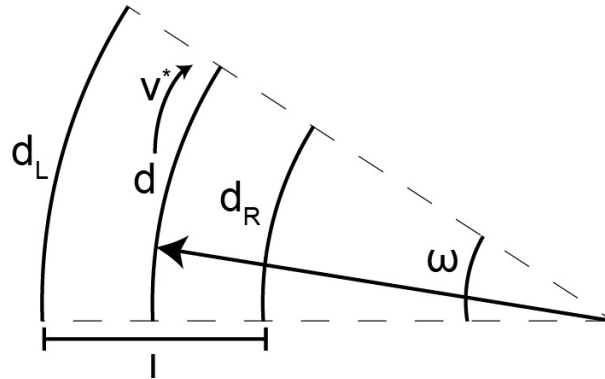
Variometers indicate the rate of climb or descent (vertical velocity) in an aerial vehicle. I have a small variometer sensor that I would like to use on a quadrotor for altitude control. In order to evaluate the sensor's performance, I launch it on a small model rocket and record its measurements. The recorded values are:

Time (s)	Velocity (m/s)
0	3.75
0.5	-1.5
1.5	-8.5

- (a) Perform polynomial interpolation on these points. Show your work (you can use a computer to do a matrix inverse).
- (b) (Optional) The rocket is in freefall, so I expect that it will approximately follow a parabolic trajectory (its flight will not be exactly parabolic due to wind resistance). The velocity profile of a parabolic trajectory is linear. Perform polynomial regression using a first-order polynomial.

### 3. Turning via reference tracking

We would like the car to turn with a specified radius  $r$  and speed  $v^*$ . The controller's unit for distance is encoder ticks, but each tick is approximately 1 cm of wheel circumference. To turn, we want  $\delta$  to change at a particular rate. Without loss of generality, we'll analyze a right turn, corresponding to increasing  $\delta$ . For a left turn, we simply negate  $\delta$ . Our goal is to generate a reference from the desired  $r$  and  $v^*$  for the controller to follow. This reference will be a function of the controller's time-step. Inspect the following diagram:



- $r$  - turn radius in cm where 1 cm = 1 encoder tick
- $\omega$  - angular velocity
- $\theta$  - angle traveled
- $d$  - distance traveled by the center of the car in ticks
- $l$  - distance between the centers of the wheels in cm

From this geometry, can you write  $\delta[k]$  in the following form?

$$\delta[k] = f(r, v^*, l, k)$$

4. Redo problem 1 on the midterm

5. Redo problem 2 on the midterm

6. Redo problem 3 on the midterm

7. Redo problem 4 on the midterm

8. Redo problem 5 on the midterm

#### Contributors:

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