

EECS 151/251A

Discussion 2

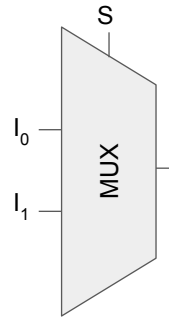
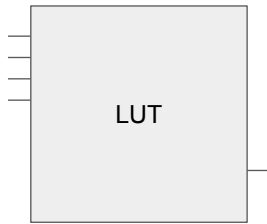
02/02/2018

Agenda

- LUT as a MUX
- Boolean Algebra
- Timing
- FSM

LUT as a MUX

- What is a LUT?
- What is a MUX?
- How can you use a LUT as a MUX?
- Biggest MUX in a 5-LUT? 6-LUT?



Look-up table

				Output
0	0	0	0	
0	0	0	1	
0	0	1	0	
0	0	1	1	
0	1	0	0	
0	1	0	1	
0	1	1	0	
0	1	1	1	

				Output
1	0	0	0	
1	0	0	1	
1	0	1	0	
1	0	1	1	
1	1	0	0	
1	1	0	1	
1	1	1	0	
1	1	1	1	

Outputs:

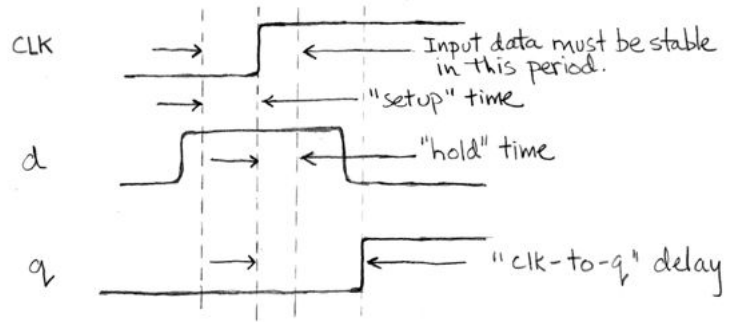
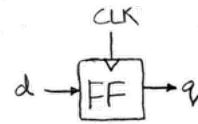
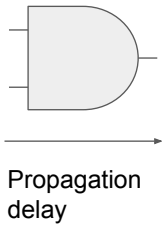
If Isb is sel; output =

0
0
1
0
0
1
1
1

And repeated

Timing

4 things we care about (for now)



Combination logic propagation delay (max) - after this, the output stably represents the function applied to the input

Combination logic contamination delay (min prop delay) - after this, the previous output is no longer valid

Flip flops: set up time: time to keep input stable BEFORE clock edge

Hold time: time to keep input stable AFTER clock edge

Clock-to-Q: time until output of flip flop

Boolean Algebra

Basics

A.B	A AND B	1.1 = ? 1.0 = ?
A + B	A OR B	0 + 0 = ? 1 + 0 = ? 1 + 1 = ?
A + A = ? A + 0 = ?	A.A = ? A.0 = ?	

De Morgan's laws

$$\sim(AB) = \sim A \text{ OR } \sim B$$

$$\sim A.\sim B = ?$$

Not a coincidence that the notation suggests behaviour in the manner we're used to with integers.

$$1.1 = 1$$

$$1 + 0 = 1$$

$$1 + 1 = 2 \text{ but in a}$$

$$\sim(AB) = \sim A \text{ OR } \sim B$$

$$\sim A.\sim B = \sim\sim(\sim A.\sim B) = \sim(A \text{ OR } B)$$

Boolean Algebra

Basics

$A.B$	$A \text{ AND } B$	$1.1 = 1$ $1.0 = 0$
$A + B$	$A \text{ OR } B$	$0 + 0 = 0$ $1 + 0 = 1$ $1 + 1 = 1 \text{ in } F_2/Z_2/GF(2)$
$A + A = A$ $A + 0 = A$	$A.A = A$ $A.0 = 0$	

De Morgan's laws

$$\sim(AB) = \sim A \text{ OR } \sim B$$

$$\sim A.\sim B = \sim(A \text{ OR } B)$$

$$A \text{ NAND } B = (\text{NOT } A) \text{ OR } (\text{NOT } B)$$

$$(\text{NOT } A) \text{ AND } (\text{NOT } B) = A \text{ NOR } B$$

Not a coincidence that the notation suggests behaviour in the manner we're used to with integers.

$$1.1 = 1$$

$$1 + 0 = 1$$

$$1 + 1 = 2 \text{ but in a}$$

$$\sim(AB) = \sim A \text{ OR } \sim B$$

$$\sim A.\sim B = \sim\sim(\sim A.\sim B) = \sim(A \text{ OR } B)$$

Truth Tables

- Quickly prove to you equivalence of expressions
- Canonically describe an expression (exhaustive proof)
- Require discipline and rigour
- Are your friend

If you ever get confused...

Simplification

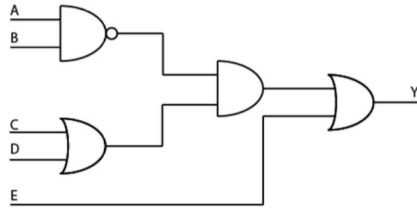
$$X = \sim A \cdot \sim B + \sim A \cdot B + A \cdot B$$

$$\sim(A + \sim B) = \sim A \cdot B$$

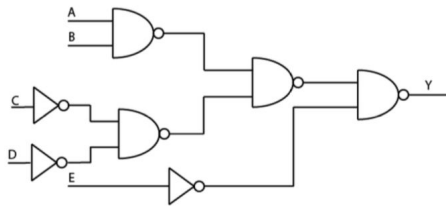
$$X = \sim(\sim(\sim(A + \sim B) + (AB))(A + B));$$

$$\begin{aligned} & \sim A \cdot \sim B + \sim A \cdot B + A \cdot B \\ &= \sim A \cdot \sim B + \sim A \cdot B + A \cdot B + \sim A \cdot B \\ &= \sim A(\sim B + B) + B(A + \sim A) \\ &= \sim A(1) + B(1) \\ &= \sim A + B \end{aligned}$$

A) Convert the circuit below to use only 2-input NAND gates and inverters.



A) Using DeMorgan's Law, the NAND only circuit is:



De morgan's laws:

$$\sim(AB) = \sim A \text{ OR } \sim B$$

$$\sim A. \sim B = \sim\sim(\sim A. \sim B) = \sim(A \text{ OR } B)$$

In this circuit

$$C \text{ OR } D = \sim\sim(C \text{ OR } D) = \sim(\sim C. \sim D) \leftarrow \text{nand with inverters}$$

I (for intermediate) 0 (the top one) AND I1

$$I0.I1 = \sim\sim(I0.I1)$$

$$I3 + E = \sim(\sim(I3 + E)) = \sim(\sim I3. \sim E) \leftarrow \text{nand with inverters on inputs again}$$

But if we do this step last, we see that the output just needs to be inverted anyway, so we can just turn the original and into a nand.

Think of the algebra you're used to. How do you simplify and solve, or expand, or factor, to get it to look like something you want?

Don't get hung up thinking through what it all means intuitively. It'll probably slow you down. Just do it a few times.

B) Configure a 2-to-1 multiplexer in order to implement the following functions:

(a) $F = XY$

(b) $F = X\bar{Y}$

(c) $F = X + Y$

You can only use one multiplexer per function. You are given the input signals X and Y (but NOT their complements) and you may use the supply and ground as inputs (i.e. 1 and 0).

c

B) Assume that the inputs of the multiplexer are $In0$, $In1$, the output is Out and the select signal is S , i.e. the multiplexer is implementing the function $Out = In0 \cdot \bar{S} + In1 \cdot S$. The following table shows how the multiplexer needs to be configured for each function:

Function	$In0$	$In1$	S	Out
(a)	0	X	Y	XY
(b)	X	0	Y	$X\bar{Y}$
(c)	Y	1	X	$X + Y$

^: ✓

Finite State Machines

Moore vs Mealy?

Examples?

Moore= outputs depend only on state

Mealy = outputs depend on state and other inputs

What are simple examples?

Traffic lights

References

- Homework 2, EECS 151/251A Spring 2017
- Wikipedia