

## The Beauty and Joy of Computing

**Lecture #7 Algorithms II**

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*bjc*

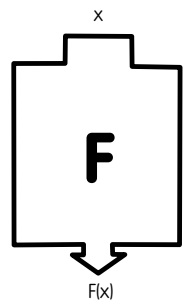
California Law Says All Websites Must Give Minors Option To Delete User Activity

Good: More privacy!  
Bad: How exactly do you delete content from the Internet?

<http://abcnews.go.com/Technology/calif-law-websites-minors-delete-activity/story?id=20361045/>

## Functional Abstraction (review)

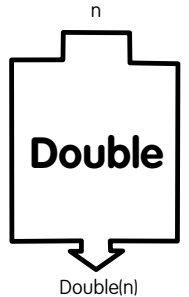
- A block, or function has inputs & outputs
  - Possibly no inputs
  - Possibly no outputs (if block is a command)
    - In this case, it would have a "side effect", i.e., what it does (e.g., move a robot)
- The contract describing what that block does is called a specification or spec



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## What is IN a spec? (review)


- Typically they all have
  - NAME
  - INPUT (s)
    - (and types, if appropriate)
    - Requirements
  - OUTPUT
    - Can write "none"
  - (SIDE-EFFECTS)
  - EXAMPLE CALLS
- Example
  - NAME : Double
  - INPUT : n (a number)
  - OUTPUT : n + n



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## What is NOT in a spec?

- How!
  - That's the beauty of a functional abstraction; it doesn't say how it will do its job.
- Example: Double
  - Could be  $n * 2$
  - Could be  $n + n$
  - Could be  $n+1$  (n times)
    - if n is a positive integer
- This gives great freedom to author!
  - You choose Algorithm(s)!




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## What do YOU think?

Which factor below is the most important in choosing the algorithm to use?

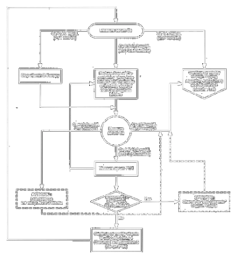
- Simplest?
- Easiest to implement?
- Takes less time?
- Uses up less space (memory)?
- Gives a more precise answer?



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## Algorithm analysis : the basics

- An algorithm is correct if, for every input, it reports the correct output **and** doesn't run forever or cause an error.
  - Incorrect algorithms may run forever, or may not return the correct answer.
    - They could still be useful!
    - Consider an approximation...
  - For now, we'll only consider correct algorithms

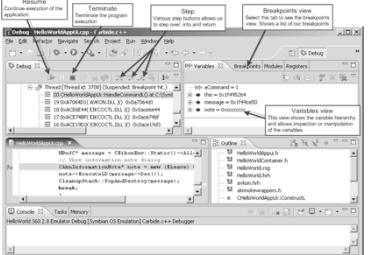


Algorithm for managing Vitamin D sterols based on serum calcium levels.  
www.kidney.org/professionals/kdoqi/guidelines\_bone/guidesB.htm

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**How do you know if "it" is correct?**

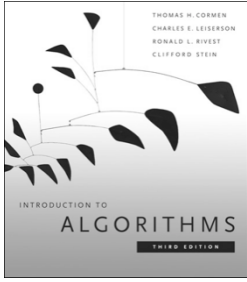
- **Mathematical proof for algorithms**
- **Empirical verification through testing of programs:**
  - Unit Testing
  - Debugging



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**Reference text**

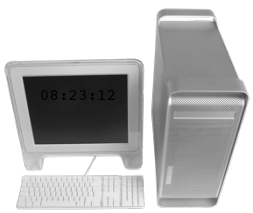
- **This book launched a generation of CS students into Algorithm Analysis**
  - It's on everyone's shelf
  - It might be hard to grok at this point, but if you go on in CS, remember it & own it!
  - ...but get the most recent years



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**Algorithm analysis : running time**


- **One commonly used criterion in making a decision is running time**
  - how long does the algorithm take to run and finish its task?
- **How do we measure it?**



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**Runtime analysis problem & solution**


- **Time w/stopwatch, but...**
  - Different computers may have different runtimes. ☹
  - Same computer may have different runtime on the same input. ☹
  - Need to implement the algorithm first to run it. ☹
- **Solution: Count the number of "steps" involved, not time!**
  - Each operation = 1 step
  - If we say "running time", we'll mean # of steps, not time!



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**Runtime analysis : input size & efficiency**

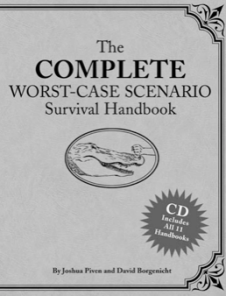
- **Definition**
  - Input size: the # of things in the input.
  - E.g., # of things in a list
  - Running time as a function of input size
  - Measures efficiency
- **Important!**
  - In CS10 we won't care about the efficiency of your solutions!
  - ...in CS61B we will



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**Runtime analysis : worst or avg case?**

- **Could use avg case**
  - Average running time over a vast # of inputs
- **Instead: use worst case**
  - Consider running time as input grows
- **Why?**
  - Nice to know most time we'd ever spend
  - Worst case happens often
  - Avg is often ~ worst



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### Runtime analysis: Final abstraction

- **Instead of an exact number of operations we'll use abstraction**
  - Want order of growth, or dominant term
- **In CS10 we'll consider**
  - Constant
  - Logarithmic
  - Linear
  - Quadratic
  - Cubic
  - Exponential
- **E.g.  $10n^2 + 4 \log n + n$** 
  - ...is quadratic

Graph of order of growth curves on log-log plot

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### Example: Finding a student (by ID)

- **Input**
  - Unsorted list of students L
  - Particular student S
- **Output**
  - True if S is in L, else False
- **Pseudocode Algorithm**
  - Go through one by one, checking for match.
  - If match, true
  - If exhausted L and didn't find S, false
- **Worst-case running time as function of the size of L?**
  1. Constant
  2. Logarithmic
  3. Linear
  4. Quadratic
  5. Exponential

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### Example: Finding a student (by ID)

- **Input**
  - Sorted list of students L
  - Particular student S
- **Output : same**
- **Pseudocode Algorithm**
  - Start in middle
  - If match, report true
  - If exhausted, throw away half of L and check again in the middle of remaining part of L
  - If nobody left, report false
- **Worst-case running time as function of the size of L?**
  1. Constant
  2. Logarithmic
  3. Linear
  4. Quadratic
  5. Exponential

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### Example: Finding a student (by ID)

- **What if L were given to you in advance and you had infinite storage?**
  - Could you do any better than logarithmic?
- **Worst-case running time as function of the size of L?**
  1. Constant
  2. Logarithmic
  3. Linear
  4. Quadratic
  5. Exponential

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### Example: Finding a shared birthday

- **Input**
  - Unsorted list L (of size n) of birthdays of team
- **Output**
  - True if any two people shared birthday, else False
- **What's the worst-case running time?**
- **Worst-case running time as function of the size of L?**
  1. Constant
  2. Logarithmic
  3. Linear
  4. Quadratic
  5. Exponential

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### Example: Finding subsets


- **Input:**
  - Unsorted list L (of size n) of people
- **Output**
  - All the subsets
- **Worst-case running time? (as function of n)**
- **E.g., for 3 people (a,b,c):**
  - 1 empty: {}
  - 3 1-person: {a, b, c}
  - 3 2-person: {ab, bc, ac}
  - 1 3-person: {abc}
- **Worst-case running time as function of the size of L?**
  1. Constant
  2. Logarithmic
  3. Linear
  4. Quadratic
  5. Exponential

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## Limits

- We can prove mathematically that some algorithms are never solveable!
- We can (almost) prove mathematically that some algorithms will never be efficient!
  - Famous problem  $P = NP$  ?
  - Example: Travelling Salesman Problem
  - BUT: Can use heuristics for approximation



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## Summary

- When developing an algorithm, could optimize for
  - Simplest
  - Easiest to implement?
  - Most efficient
  - Uses up least resources
  - Gives most precision
  - ...
- In CS10 we'll consider
  - Constant
  - Logarithmic
  - Linear
  - Quadratic
  - Cubic
  - Exponential
- There are empirical and formal methods to verify efficient and correctness
- Some algorithms cannot be implemented efficiently

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