One million Wi-Fi devices isn’t cool.
You know what’s cool? A Billion Wi-Fi devices.
…all running the new 802.11ac 1G Wi-Fi standard, which hasn’t yet been ratified by the IEEE, but we’ll see draft by 2011 and products out there by 2012. It’ll use radio spectrum below 6GHz & bond 4- or 8-channels together.

hothardware.com/News/1Gbps-WiFi-Soon-Coming-To-a-Billion-Devices
Functional Abstraction (review)

- A **block**, or **function** has inputs & outputs
  - Possibly no inputs
  - Possibly no outputs (if block is a **command**)
    - In this case, it would have a “side effect”, i.e., what it does (e.g., move a robot)

- The **contract** describing what that block does is called a **specification** or **spec**

\[ F(x) \]
What is IN a spec? (review)

- Typically they all have
  - NAME
  - INPUT(s)
    - (and types, if appropriate)
    - Requirements
  - OUTPUT
    - Can write “none”
  - (SIDE-EFFECTS)
  - EXAMPLE CALLS

- Example
  - NAME : Double
  - INPUT : n (a number)
  - OUTPUT : n + n

Double

Double (n)
What is NOT in a spec?

- **How!**
  - That’s the beauty of a functional abstraction; it doesn’t say how it will do its job.

- **Example: Double**
  - Could be $n \times 2$
  - Could be $n + n$
  - Could be $n+1$ ($n$ times)
    - if $n$ is a positive integer

- **This gives great freedom to author!**
  - You choose Algorithm(s)!
What do YOU think?

Which factor below is the most important in choosing the algorithm to use?

A. Simplest?
B. Easiest to implement?
C. Takes less time?
D. Uses up less space (memory)?
E. Gives a more precise answer?
This book launched a generation of CS students into Algorithm Analysis
- It’s on everyone’s shelf
- It might be hard to grok at this point, but if you go on in CS, remember it & own it!
  - …but get the most recent vers
Algorithm analysis: the basics

- An algorithm is **correct** if, for every input, it reports the correct output and doesn’t run forever or cause an error.
  - Incorrect algorithms may run forever, or may crash, or may not return the correct answer.
    - They could still be useful!
    - Consider an approximation…
  - For now, we’ll only consider **correct** algorithms

Algorithm for managing Vitamin D sterols based on serum calcium levels.

www.kidney.org/professionals/kdoqi/guidelines_bone/guide8b.htm
Algorithm analysis: running time

- One commonly used criterion in making a decision is **running time**
  - how long does the algorithm take to run and finish its task?
- How do we measure it?
Runtime analysis problem & solution

- Time w/ stopwatch, but...
  - Different computers may have different runtimes.
  - Same computer may have different runtime on the same input.
  - Need to implement the algorithm first to run it.

- Solution: Count the number of “steps” involved, not time!
  - Each operation = 1 step
  - If we say “running time”, we’ll mean # of steps, not time!
Definition

- **Input size**: the number of things in the input.
- E.g., number of things in a list
- Running time as a function of input size
- Measures **efficiency**

**Important!**

- In CS10 we won’t care about the efficiency of your solutions!
- …in CS61B we will
Runtime analysis: worst or avg case?

- Could use avg case
  - Average running time over a vast # of inputs
- Instead: use worst case
  - Consider running time as input grows
- Why?
  - Nice to know most time we’d ever spend
  - Worst case happens often
  - Avg is often ~ worst
Runtime analysis: Final abstraction

- Instead of an exact number of operations we’ll use abstraction
  - Want order of growth, or dominant term

- In CS10 we’ll consider
  - Constant
  - Logarithmic
  - Linear
  - Quadratic
  - Cubic
  - Exponential

- E.g. $10n^2 + 4\log n + n$
  - ...is quadratic

Graph of order of growth curves on log-log plot
Example: Finding a student (by ID)

- **Input**
  - Unsorted list of students L
  - Particular student S

- **Output**
  - True if S is in L, else False

- **Pseudocode Algorithm**
  - Start one by one, checking for match.
  - If match, true
  - If exhausted L and didn’t find S, false

- **Worst-case running time as function of the size of L?**
  1. Constant
  2. Logarithmic
  3. Linear
  4. Quadratic
  5. Exponential
Example: Finding a student (by ID)

- **Input**
  - Sorted list of students L
  - Particular student S

- **Output**: same

- **Pseudocode Algorithm**
  - Start in middle
  - If match, report true
  - If exhausted, throw away half of L and check again in the middle of remaining part of L
  - If nobody left, report false

- **Worst-case running time as function of the size of L?**
  1. Constant
  2. Logarithmic
  3. Linear
  4. Quadratic
  5. Exponential
Example: Finding a student (by ID)

- What if L were given to you in advance and you had infinite storage?
  - Could you do any better than logarithmic?

- Worst-case running time as function of the size of L?
  1. Constant
  2. Logarithmic
  3. Linear
  4. Quadratic
  5. Exponential
**Example: Finding a shared birthday**

- **Input**
  - Unsorted list \( L \) (of size \( n \)) of birthdays of team

- **Output**
  - True if any two people shared birthday, else False

- **What’s the worst-case running time?**

**Worst-case running time as function of the size of \( L \)?**

1. Constant
2. Logarithmic
3. Linear
4. Quadratic
5. Exponential
Example: Finding subsets

- **Input:**
  - Unsorted list L (of size n) of people

- **Output**
  - All the subsets

- **Worst-case running time?**

- **E.g., for 3 people (a,b,c):**
  - 1 empty: \{\}
  - 3 1-person: \{a, b, c\}
  - 3 2-person: \{ab, bc, ac\}
  - 1 3-person: \{abc\}

- **Worst-case running time as function of the size of L?**
  1. Constant
  2. Logarithmic
  3. Linear
  4. Quadratic
  5. Exponential
Summary

- When choosing algorithm, could optimize for
  - Simplest
  - Easiest to implement?
  - Most efficient
  - Uses up least resources
  - Gives most precision
  - ...

- In CS10 we’ll consider
  - Constant
  - Logarithmic
  - Linear
  - Quadratic
  - Cubic
  - Exponential

How does the goalie choose how to block ball?