CS 188: Artificial Intelligence Spring 2006

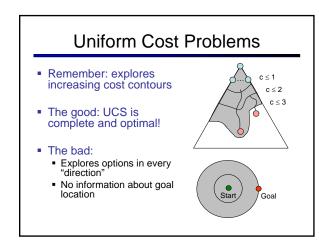
Lecture 4: A* Search (and Friends) 1/26/2006

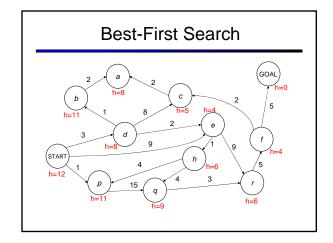
Dan Klein – UC Berkeley

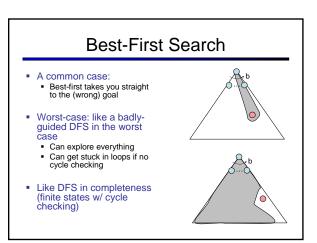
Many slides from either Stuart Russell or Andrew Moore

Today

- A* Search
- Heuristic Design
- Local Search

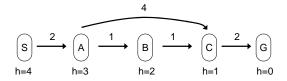






Combining Best-First and UCS

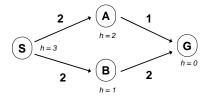
- Uniform-cost orders by path cost, or backward cost g(n)
- Best-first orders by goal proximity, or forward cost h(n)



- What happens with each ordering?
- A* orders by the sum: f(n) = g(n) + h(n)

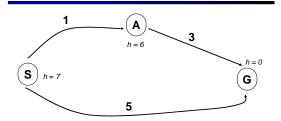
When should A* terminate?

Should we stop when we enqueue a goal?



No: only stop when we dequeue a goal

Is A* Optimal?



- What went wrong?
- Actual bad goal cost > estimated good goal cost
- We need estimates to be less than actual costs!

Admissible Heuristics

• A heuristic is admissible (optimistic) if:

$$h(n) \leq h^*(n)$$

where $h^*(n)$ is the true cost to a nearest goal

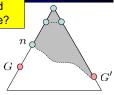
- E.g. Euclidean distance on a map problem
- Coming up with admissible heuristics is most of what's involved in using A* in practice.

Optimality of A*: Blocking

This proof assumed Proof: tree search! Where?

- What can go wrong?
- We'd have to have to pop a suboptimal goal off the fringe queue
- Imagine a suboptimal goal G' is on the queue
- Consider any unexpanded (fringe) node *n* on a shortest path to optimal G

n will be popped before G



 $f(n) \leq g(G)$

g(G) < g(G')

g(G') = f(G')

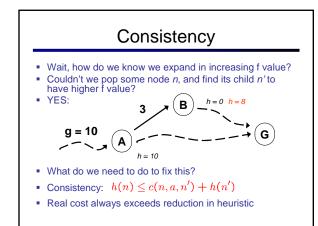
f(n) < f(G')

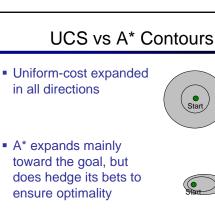
Optimality of A*: Contours

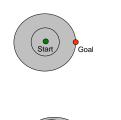
- Consider what A* does:
 - Expands nodes in increasing total f value (f-contours)
 - Optimal goals have lower f value, so get expanded first

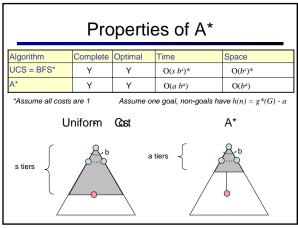


Holds for graph search as well, but we made a different assumption. What?

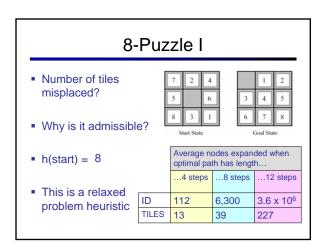








Properties of A*						
Algorithm	Complete	Optimal	Time	Space		
UCS = BFS*	Y	Y	O(s bs)*	O(bs)*		
A*	Y	Y	O(a ba)	$O(b^a)$		
	A .b	2	tiers \	& b		
s tiers	55	a	tiers 1	38		



8	-Puz	zle II		
 What if we had an easier 8-puzzle whe any tile could slide a one direction at any time? Total Manhattan distance Why admissible? 			3 6 odes expan th has lengt	
• h(start) =		4 steps	8 steps	12 steps
3+1+2+	TILES	13	39	227
= 18	MAN- HATTAN	12	25	73

Admissible Heuristics

Good news: usually admissible heuristics

More good news: inadmissible heuristics are often quite effective (especially when

Most of the work is in coming up with

admissible heuristics

are also consistent

you have no choice)

8-Puzzle III

- How about using the actual cost as a heuristic?
 - Would it be admissible?
 - Would we save on nodes?
 - What's wrong with it?
- With A*, trade-off between quality of estimate and work per node!

Trivial Heuristics, Dominance

Dominance:

$$\forall n: h_a(n) \geq h_c(n)$$

- Heuristics form a semi-lattice:
 - Max of admissible heuristics is admissible

$$h(n) = max(h_a(n), h_b(n))$$

- Trivial heuristics
 - Bottom of lattice is the zero heuristic (what does this give us?)
 - Top of lattice is the exact heuristic



Course Scheduling

- From the university's perspective:
 - Set of courses $\{c_1, c_2, \dots c_n\}$
 - Set of room / times {r₁, r₂, ... r_n}
 - Each pairing (c_k, r_m) has a cost w_{km}
 - What's the best assignment of courses to rooms?
- States: list of pairings
- · Actions: add a legal pairing
- Costs: cost of the new pairing
- Admissible heuristics?
- (Who can think of a cs170 answer to this problem?)

Other A* Applications

- Machine translation
- Statistical parsing
- Speech recognition
- Robot motion planning (next class)
- Routing problems (see homework!)
- Planning problems (see homework!)
- •

Summary: A*

- A* uses both backward costs and (estimates of) forward costs
- A* is optimal with admissible heuristics
- Heuristic design is key: often use relaxed problems

Local Search Methods

- Queue-based algorithms keep fallback options (backtracking)
- Local search: improve what you have until you can't make it better
- Generally much more efficient (but incomplete)

Types of Problems

- Planning problems:
 - We want a path to a solution (examples?)
 - Usually want an optimal path
 - Incremental formulations



- Identification problems:
 - We actually just want to know what the goal is (examples?)
 - Usually want an optimal goal
 - Complete-state formulations
 - Iterative improvement algorithms

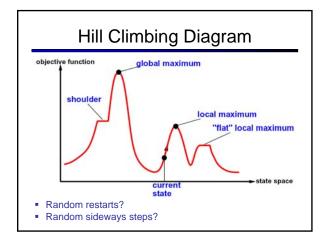


Example: N-Queens h = 0Start wherever, move queens to reduce conflicts

- Almost always solves large n-queens nearly instantly
- How is this different from best-first search?

Hill Climbing

- Simple, general idea:
 - Start wherever
 - Always choose the best neighbor
 - If no neighbors have better scores than current, quit
- Why can this be a terrible idea?
 - Complete?
 - Optimal?
- What's good about it?



Simulated Annealing

- Idea: Escape local maxima by allowing downhill moves
 - But make them rarer as time goes on

function SIMULATED-ANNEALING (problem, schedule) returns a solution state inputs: problem, a problem
schedule, a mapping from time to "temperature" local variables: current, a node next, a node T, a "temperature" controlling prob. of downward steps $mrent \leftarrow Make-Node(Initial-State[problem])$ for $t \leftarrow 1$ to ∞ do $T \leftarrow schedule[t]$ if T = 0 then return current $\begin{array}{l} next \leftarrow \text{a randomly selected successor of } eurrent \\ \Delta E \leftarrow \text{Value}[next] - \text{Value}[eurrent] \end{array}$ if $\Delta E > 0$ then current \leftarrow

else $\mathit{current} \leftarrow \mathit{next}$ only with probability $e^{\Delta - E/T}$

Simulated Annealing

- Theoretical guarantee:
 - ullet Stationary distribution: $p(x) \propto e^{rac{E(x)}{kT}}$
 - If T decreased slowly enough, will converge to optimal state!
- Is this an interesting guarantee?
- Sounds like magic, but reality is reality:
 - The more downhill steps you need to escape, the less likely you are to every make them all in a row
 - People think hard about ridge operators which let you jump around the space in better ways

Beam Search

Like greedy search, but keep K states at all times:

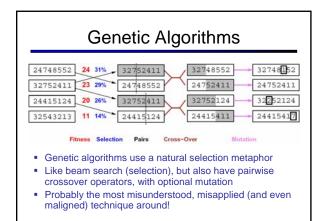




Greedy Search

Beam Search

- Variables: beam size, encourage diversity?
- The best choice in MANY practical settings
- Complete? Optimal?
- Why do we still need optimal methods?



Example: N-Queens Why does crossover make sense here? When wouldn't it make sense? What would mutation be? What would a good fitness function be?

