CS 188: Artificial Intelligence Spring 2006

Lecture 5: Robot Motion Planning 1/31/2006

Dan Klein - UC Berkelev Many slides from either Stuart Russell or Andrew Moore

Robotics Tasks

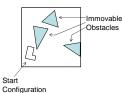
- Motion planning (today)
 - How to move from A to B
 Known obstacles
 Offline planning
- Localization (later)
 - Where exactly am I?
 - Known map
 - Ongoing localization (why?)
- Mapping (much later)What's the world like?

 - Exploration / discovery
 - SLAM: simultaneous localization and mapping



Mobile Robots

- High-level objectives: move robots around obstacles
- · Low-level: fine motor control to achieve motion
- Why is this hard?







Manipulator Robots

- High-level goals: reconfigure environment
- Low-level: move from configuration A to B (point-to-point motion)
 - Why is this already hard?
- Also: compliant motion





Sensors and Effectors

- Sensors vs. Percepts
 - Agent programs receive percepts
 - Agent bodies have sensors
 - Includes proprioceptive sensors
 - Real world: sensors break, give noisy answers, miscalibrate, etc.
- Effectors vs. Actuators
 - Agent programs have actuators (control lines)
 - Agent bodies have effectors (gears and motors)
 - Real-world: wheels slip, motors fail, etc.





Degrees of Freedom

- The degrees of freedom are the numbers required to specify a robot's configuration
- Positional DOFs:
 - (x, y, z) of free-flying robot
 - direction robot is facing
- Effector DOFs
 - Arm angle Wing position
- Static state: robot shape and position
- Dynamic state: derivatives of static DOFs (why have these?)

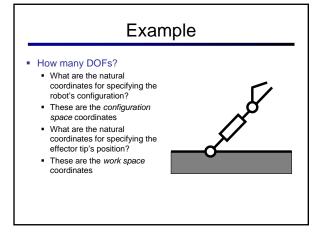


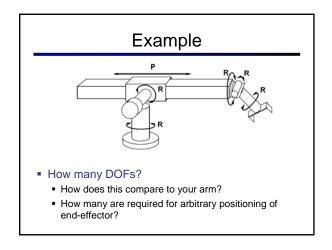
2 DOFs

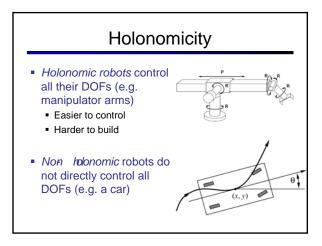


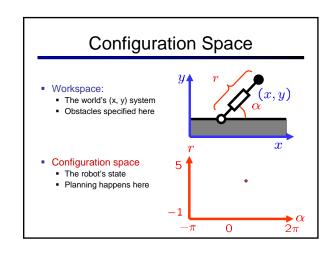
3 DOFs

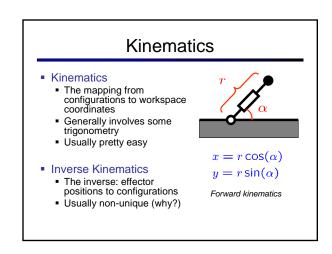
Question: How many DOFs for a polyhedron free-flying in 3D space?

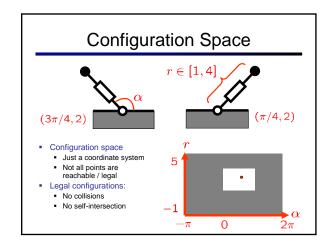


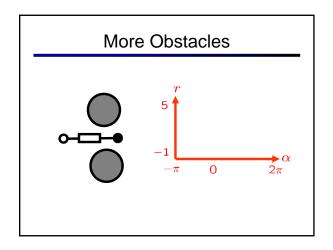


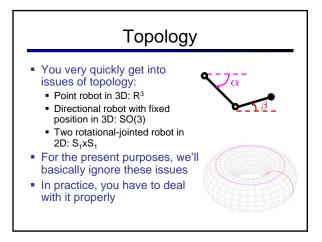


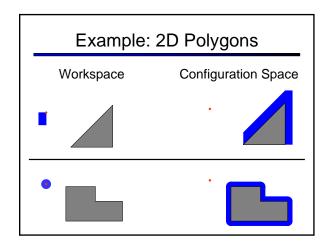


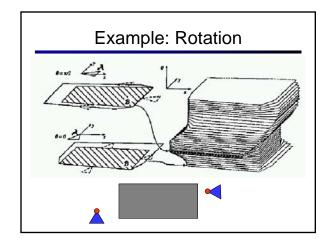


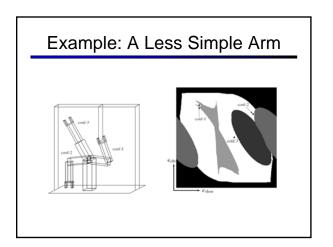










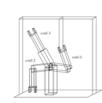


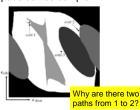
Summary

- Degrees of freedom
- Legal robot configurations form configuration space
- Obstacles have complex images in cspace

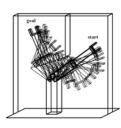
Motion as Search

- Motion planning as path finding problem
 - Problem: configuration space is continuous
 - Problem: under-constrained motion
 - Problem: configuration space can be complex





Decomposition Methods

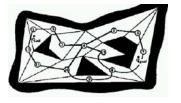




- Break c-space into discrete regions
- Solve as a discrete problem

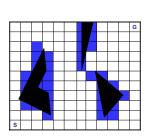
Exact Decomposition?

- With polygon obstacles: decompose exactly
- Problems?
 - Doesn't scale at all
 - Doesn't work with complex, curved obstacles



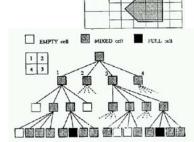
Approximate Decomposition

- Break € space into a grid
 - Search (A*, etc)
 - What can go wrong?
 - If no path found, can subdivide and repeat
- Problems?
 - Still scales poorly
 - Incomplete*
 - Wiggly paths



Hierarchical Decomposition

- Actually used in practical systems
- But:
 - Not optimal
 - Not complete
 - Still hopeless above a small number of



Skeletonization Methods

 Decomposition methods turn configuration space into a grid



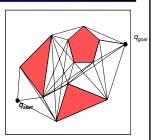
Skeletonization methods turn it into a set of points, with preset linear path between them



Visibility Graphs

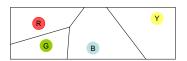
- Shortest paths:
 - No obstacles: straight line
 - Otherwise: will go from vertex to vertex
 - Fairly obvious, but somewhat awkward to prove
- Visibility methods:
 - All free vertex-to-vertex lines (visibility graph)
 Search using, e.g. A*

 - Can be done in O(n³) easily, O(n²log(n)) less easily
- Problems?
 - Bang, screech!
 - Not robust to control errors
 - Wrong kind of optimality?



Voronoi Decomposition

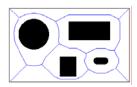
Voronoi regions: points colored by closest obstacle

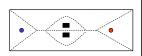


- Voronoi diagram: borders between regions
 - Can be calculated efficiently for points (and polygons) in 2D
 - In higher dimensions, some approximation methods

Voronoi Decomposition

- - Compute the Voronoi diagram of the configuration space
 - of the configuration space
 Compute shortest path (line)
 from start to closest point on
 Voronoi diagram
 Compute shortest path (line)
 from goal to closest point on
 Voronoi diagram.
 Compute shortest path from
 start to goal along Voronoi
 diagram
 replaces:
- Problems:
 - Hard over 2D, hard with complex obstacles
 Can do weird things:





Probabilistic Roadmaps

- Idea: just pick random points as nodes in a visibility graph
- This gives probabilistic roadmaps
 - Very successful in practice
 - Lets you add points where you need them
 - If insufficient points, incomplete, or weird paths



Roadmap Example

Potential Field Methods

- So far: implicit preference for short paths
- Rational agent should balance distance with risk!
- Idea: introduce cost for being close to an obstacle
- Can do this with discrete methods (how?)
- Usually most natural with continuous methods

Potential Fields	ď	
Cost for: Being far from goal Being near an obstacle Go downhill What could go wrong?	q. A	
For For		

Potential Field Methods

Define a function u(q)

u: Configurations $\rightarrow \Re$

Such that

 $u \rightarrow$ huge as you move towards an obstacle $u \rightarrow \text{small}$ as you move towards the goal

Write $d_g(q) = \text{distance from } q \text{ to } q \text{ goal}$

 $d_i(q)$ = distance from q to nearest obstacle

One definition of $u: u(q) = d_i(q) - d_g(q)$

Preferred definition: $u(q) = \frac{1}{2} \sum (d_s(q))^2 + \frac{1}{2} \eta \frac{1}{d_i(q)^2}$

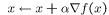
Local Search Methods

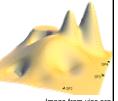
- Queue-based algorithms keep fallback options (backtracking)
- Local search: improve what you have until you can't make it better
- Generally much more efficient (but incomplete)

Gradient Methods

- How to deal with continous (therefore infinite) state spaces?
- Discretization: bucket ranges of values
 - E.g. force integral coordinates
- Continuous optimization
 - E.g. gradient ascent (or descent)

$$\nabla f = \left(\frac{\partial f}{\partial x_1}, \frac{\partial f}{\partial y_1}, \frac{\partial f}{\partial x_2}, \frac{\partial f}{\partial y_2}, \frac{\partial f}{\partial x_3}, \frac{\partial f}{\partial y_3}\right)$$





SIMPLE MOTION PLANNER:

Gradient descent on u

Optimal?

What's good about it?

Hill Climbing

- Simple, general idea:
 - Start wherever
 - Always choose the best neighbor
 - If no neighbors have better scores than current, quit
- Why can this be a terrible idea?
 - Complete?

