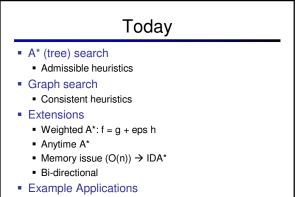
# CS 188: Artificial Intelligence Spring 2011

### Lecture 4: A\* + (beginnings of) Constraint Satisfaction 1/31/2011

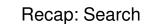
Pieter Abbeel – UC Berkeley Many slides from Dan Klein and Max Likhachev

# Announcements

- Project 1 (Search)
  - If you don't have a class account yet, pick one up after lecture
  - Still looking for project partners? --- Come to front after lecture
- Lecture videos
  - In the works



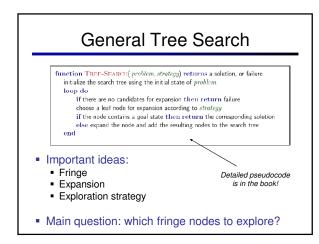
(Beginnings of CSPs)

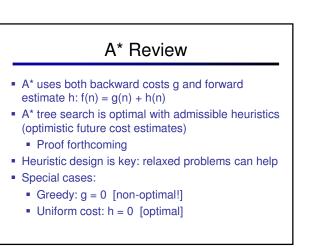


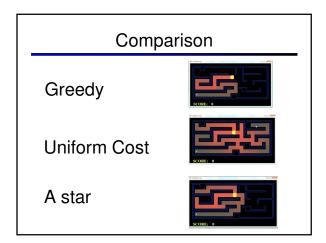
- Search problem:
  - States (configurations of the world)
  - Successor function: a function from states to
  - lists of (state, action, cost) triples; drawn as a graph Start state and goal test
- Search tree:
  - Nodes: represent plans for reaching states
  - Plans have costs (sum of action costs)

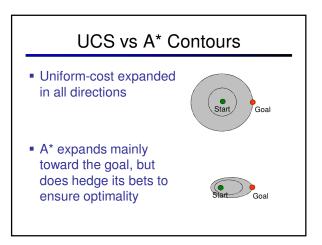
### Search Algorithm:

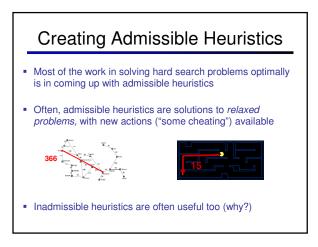
- Systematically builds a search tree
- Chooses an ordering of the fringe (unexplored nodes)

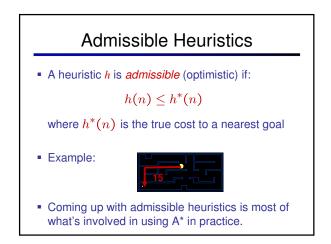


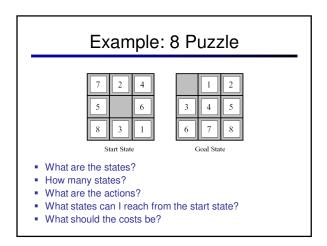


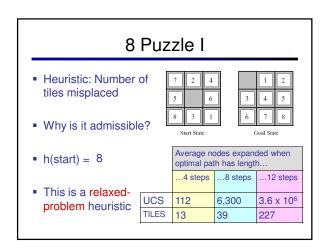


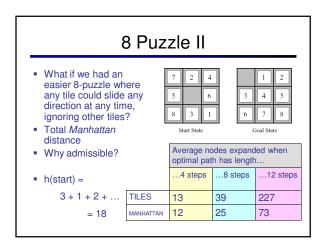


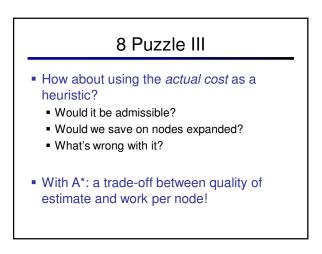


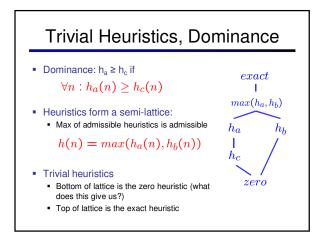


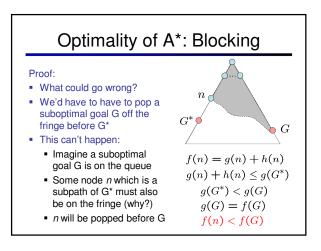


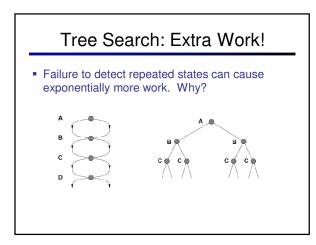


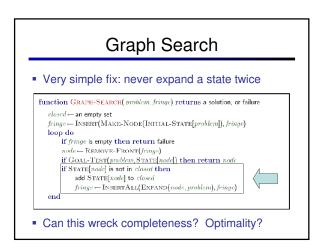


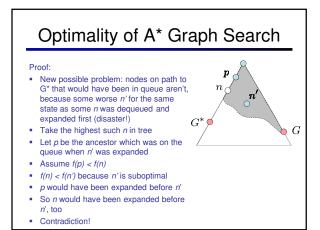


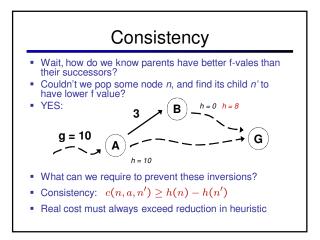


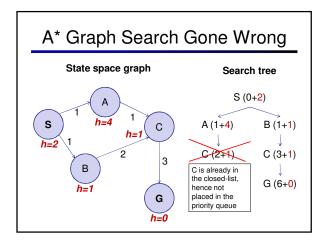


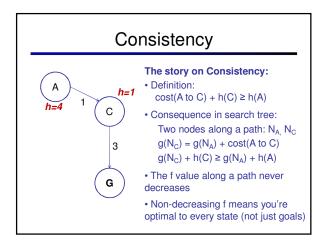






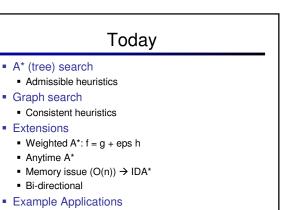




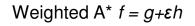


# Optimality Summary Tree search: A\* optimal if heuristic is admissible (and non-negative). Uniform Cost Search is a special case (h = 0) Graph search: A\* optimal if heuristic is consistent UCS optimal (h = 0 is consistent) Consistency implies admissibility Challenge:Try to prove this. Hint: try to prove the equivalent statement not admissible implies not consistent In general, natural admissible heuristics tend to be consistent

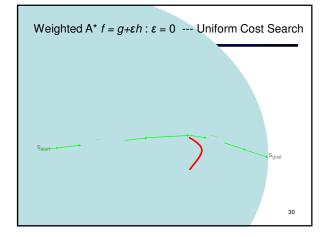
Remember, costs are always positive in search!

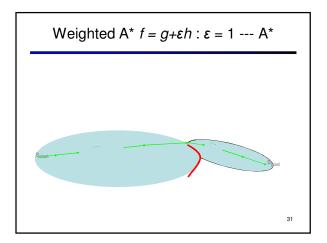


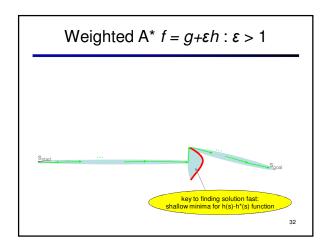
(Beginnings of CSPs)



- Weighted A\*: expands states in the order of f = g+ɛh values,
  - $\varepsilon > 1 = \text{bias}$  towards states that are closer to goal





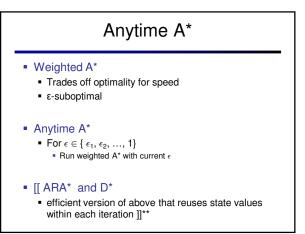


# Weighted A\* $f = g + \varepsilon h$ : $\varepsilon > 1$

- Trades off optimality for speed
- ε-suboptimal:
  - cost(solution) ≤ ε·cost(optimal solution)
  - Test your understanding by trying to prove this!
- In many domains, it has been shown to be orders of magnitude faster than A\*
- Research becomes to develop a heuristic function that has shallow local minima

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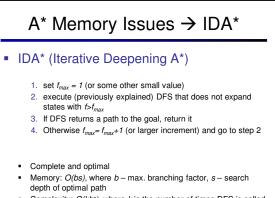
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### A\* Memory Issues

- A\* does provably minimum number of expansions (O(n)) for finding a provably optimal solution
- Memory requirements of A\* (O(n)) can be improved though
- Memory requirements of weighted A\* are often but not always better

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• Complexity: O(kb<sup>s</sup>), where k is the number of times DFS is called

# **Bi-directional search**

### If only 1 goal state:

- Can simultaneously run two searches:
  - Search 1 starts at the START state
  - Search 2 starts at the GOAL state
- → to find path from START to GOAL only requires two searches of depth s/2 rather than one of depth s
- $\rightarrow$  O(b<sup>(s/2)</sup>) vs. O(b<sup>s</sup>)
- Challenge: think about how to run bidirectional A\*

# Robotics Examples

- Urban Challenge
  - Successor function?
  - Heuristic?
- Door Opening
  - Successor function?
  - Heuristic?

# Other A\* Applications

- Pathing / routing problems
- Resource planning problems
- Robot motion planning
- Language analysis
- Machine translation
- Speech recognition
- ....

## Today

- A\* (tree) search
  - Admissible heuristics
- Graph search
  - Consistent heuristics
- Extensions
  - Weighted A\*: f = g + eps h
  - Anytime A\*
  - Memory issue (O(n)) → IDA\*
  - Bi-directional
- Example Applications
- (Beginnings of CSPs)



