The Final Exam

Last name____________________________ First name__________________________
SID Number__________________________ TA’s name ___________________________

(Sorry to ask this next question, but with 100+ students, there may be a wide range of behavior.)
The name of the student to my left is _______________________________________
The name of the student to my right is _______________________________________

I certify that my answers are all my own work. I certify that I shall not discuss the exam with anyone in CS3 who has yet to take it until after the exam time.

Signature ____________________________________________________________

Instructions

• Question 0: Fill in this front page and write your name on the front of every page! The exam is open book and open notes (no computers). Put all answers on these pages; don’t hand in any stray pieces of paper.

• You may NOT write any auxiliary functions for a problem unless they are specifically allowed in the question.

• Feel free to use any Scheme function that was described in sections of the textbook we have read without defining it yourself.

• You do not need to write comments for functions you write unless you think the grader will not understand what you are trying to do otherwise.

• You have three hours, so relax. We estimate 30 minutes per question.

• Feel free to write λ instead of lambda.

• Feel free to write any comments you wish in the margins of this front page. Good skill!

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**Question 1 – This Blanket blank exam... (15 pts, 1 pts each; 30 min)**

Fill in the blanks below. The symbol “⇒” means “evaluates to”.

- If any of the following display an error, write “ERROR” & describe the error.
- If any of the following go into an infinite loop, write “INFINITE LOOP”.
- If any of the following are impossible, write “IMPOSSIBLE”.
- If any of the return values are procedures, write <PROCEDURE name>
  (e.g., cons ⇒ <PROCEDURE cons>)

```scheme
(define (mystery f g) (f (g f)))
(define (call f n) (f n))
(define (double n) (+ n 1))
(define (square n) (* n 2))
```

a) (bf (bl (word 1 (word 2 (word 3 "") )))) ⇒ ____________

b) (bf (bl (se 1 (se 2 (se 3 '() ))))) ⇒ ____________

c) (car (cdr (cons 1 (cons 2 (cons 3 '() ))))) ⇒ ____________

d) (car (cdr (list 1 (list 2 (list 3 '() ))))) ⇒ ____________

e) (car (cdr (append '(1) (append '(2) (append '(3) '() ))))) ⇒ ____________

f) (bf (first _________________________________ )) ⇒ (cal)

g) (cdr (car ____________________________________) ) ⇒ (cal)

h) (aced-cs3-final? 75) ⇒ ____________

i) (if (aced-cs3-final? ___________________________ ) 'a+ 'f) ⇒ f

j) (mystery ________________________________________ ) ⇒ (cal)

k) (reduce call (list ___________________________________) ) ⇒ 65

l) A practical application for the Dragon Curve fractal would be...
  (Hint: How would Dan use them if he were building a new house?)
  ________________________________________________________________.

m) If you’re playing misère “1, 2, ..., 10” against Gamesman, you want to play...

   FIRST / SECOND / DOESN’T-MATTER-GAMESMAN-ALWAYS-WINS (circle one).

n) We want to write a num-arguments to return how many arguments a function call has:

   ```scheme
   (num-arguments (list 'a 'b)) ⇒ 2
   (num-arguments (+ 10 21 40)) ⇒ 3
   (num-arguments (no-arg-fun)) ⇒ 0
   ``

   Now, write num-arguments:

   ```scheme
   (define (num-arguments expression) ________________________________ )
   ```
Question 2 – Cal beat HOFstra with a full-court uncompres... (20 pts; 30 min.)

You’ve probably been annoyed by the fact that every only takes a unary function and a single word/sentence. What if we had a cool binary function \( f \) and two words/sentences and wanted to call \( f \) on every pair of letters or words in them? We’d be stuck! Well, here is every2, which exactly does what we want!

\[
\text{(define (every2 } f \text{ SW1 SW2)} ; ; f \text{ is a binary function; SW1 & SW2 are sents/words}
\begin{align*}
\text{;; if (or (empty? SW1) (empty? SW2))}
\text{('())}
\text{;; else (f (first SW1) (first SW2))}
\text{(every2 } f \text{ (bf SW1) (bf SW2))})
\end{align*}
\]

\(\text{(every2 word}'(\text{gol b})'\text{(den ears)})) \Rightarrow (\text{golden bears})\)
\(\text{(every2 word}'\text{gol 'den}) \Rightarrow (\text{gd oe ln})\)

That was the setup; here’s the cool problem. Compression is the idea that you can save space by shrinking something down, transferring it, and then unshrinking it later. We decide to do the same thing with sentences to eliminate repeat letters. We’ll compress sentences by creating two sentences, which we’ll call cs and cd. cs has the repeated letters (up to 9) removed, and cd tells us (for each letter in each word in cs) how many times to repeat. All we care about is uncompression; assume compression is done for us.

\[
(\text{football win!!!!)} \xrightarrow{\text{compress}} (\text{fotbal win!}) \xrightarrow{\text{uncompress}} (\text{football win!!!!)}
\]

Your job is to write uncompress. You may write any helper functions you wish, but **YOU MAY NOT USE EXPLICIT RECURSION**; instead, use HOFs.

```scheme
;; (uncompress CS CD)
;; INPUTS : CS (A compressed sentence. C stands for "Compressed")
;; : CD (An identical-length sentence with each Digit indicating how
;; : many times the corresponding letter in CS should be repeated.)
;; RETURNS : The original sentence before compression
;; EXAMPLE :
;; (uncompress '(woho goal! i win 10!)
;; '(1213 19111 1 111 142)) \Rightarrow (woohooo goooooooooal! i win 10000!!)
```

\[
\text{(define (uncompress CS CD)} ; ; Helpers might make this problem easier...}
\begin{align*}
\text{;; Don’t use any EXPLICIT RECURSION; instead use HOFs}
\text{;; (even the helpers may not use explicit recursion)}
\end{align*}
\]
Question 3 – Run past the third car and then go deep... (20 pts; 30 min.)

You have probably found list-ref very useful. We’d like to write deep-list-ref which takes a deep list \( L \) and an index \( i \) and finds the \( i \)th atom (starting at 0) in \( L \):

\[
\begin{align*}
(\text{deep-list-ref} \ 'i \ ((\text{love}) \ cs3) \ \text{exams} \ 0) & \rightarrow i \\
(\text{deep-list-ref} \ 'i \ ((\text{love}) \ cs3) \ \text{exams} \ 1) & \rightarrow \text{love} \\
(\text{deep-list-ref} \ 'i \ ((\text{love}) \ cs3) \ \text{exams} \ 2) & \rightarrow \text{cs3} \\
(\text{deep-list-ref} \ 'i \ ((\text{love}) \ cs3) \ \text{exams} \ 3) & \rightarrow \text{exams} \\
(\text{deep-list-ref} \ 'i \ ((\text{love}) \ cs3) \ \text{exams} \ 4) & \rightarrow \text{ERROR: car: wrong type of argument}
\end{align*}
\]

\[
\begin{align*}
(\text{define} \ (\text{deep-list-ref} \ L \ i)) \\
(\text{define} \ (\text{dlr-helper} \ L \ i \ \text{seen}))
\end{align*}
\]

\[
\begin{align*}
(\text{cond} \\
1 & \ ((\text{list?} \ (\text{car} \ L)) \\
2 & \ (\text{dlr-helper} \ (\text{cons} \ (\text{car} \ L) \ (\text{cdr} \ L)) \ i \ \text{seen})) \\
3 & \ ((= \ i \ \text{seen}) \\
4 & \ (\text{car} \ L)) \\
5 & \ (\text{else} \ (\text{dlr-helper} \ (\text{cdr} \ L) \ i \ (+ \ \text{seen} \ 1))))
\end{align*}
\]

a) There is only one buggy line above. The bug affects some (but not all) input. Fill in the blanks below to complete the sentence. All arguments to deep-list-ref should be as short & simple as possible.

“Calling \((\text{deep-list-ref} \ __________________________ 1)\)

doesn’t trigger the bug and correctly returns ________________________.”

b) “However, calling \((\text{deep-list-ref} \ __________________________ 1)\)

causes/returns (fill in description) __________________________

when it should return __________________________.”

c) “Replacing line ____ with __________________________

fixes the bug so that deep-list-ref works as advertised on all input.”

d) After you make the change in (c) your friend asks you an interesting question.

“What if you changed the order of the first two cond statements?” I.e., you swap lines (1 & 2) with lines (3 & 4). What would be the result of the following calls?

\[
\begin{align*}
(\text{deep-list-ref} \ '(i \ ((\text{love}) \ cs3) \ \text{exams}) \ 0) & \rightarrow \____________; \ \text{want} \ i \\
(\text{deep-list-ref} \ '(i \ ((\text{love}) \ cs3) \ \text{exams}) \ 1) & \rightarrow \____________; \ \text{want} \ \text{love} \\
(\text{deep-list-ref} \ '(i \ ((\text{love}) \ cs3) \ \text{exams}) \ 2) & \rightarrow \____________; \ \text{want} \ \text{cs3}
\end{align*}
\]
Put down your pen or pencil, stretch, take a deep breath, and proceed

If you followed our suggested pace, you should have 90 min left and be half done.
Question 4 - fastest-game in the west... (20 pts; 30 min.)

Have you ever played a board game with a friend and wanted to see how fast the game could theoretically end? That is, if the goal for both players were to finish the game as fast as possible (regardless of who won), how many moves would be made? As a reference, here are the brief specs for the big-3 (most important functions):

- `(primitive-position pos)` ➜ `w`, `l` or `t` if `pos` is `primitive` (end of game), else `#f`
- `(do-move pos move)` ➜ A new position, the result of making that move at that `pos`
- `(generate-moves pos)` ➜ A list of all the moves available at position `pos`

For this problem, we will deal only with non-loopy games (i.e., games which never have repeat positions that could cause the game to end in a draw). This is like exactly like the games you’ve seen: `1,2,...,10`, *Tomorrow’s Tic-Tac-Toe*, *Northcott’s game* (except pieces always move towards the middle), *Knight’s Dance* (except you can’t move to a square you’ve already occupied), *Konane*, and *Surround*.

a) Write next-positions that takes a position and returns a list of all the positions which can be reached from that position in exactly one move. Your solution should work for any game in which the big-3 (above) are defined. (7 pts)

```scheme
;; Example for “1,2,...,10” in which a position is represented as (L/R num)
;; & a move is either “1” or “2”. From 0, you can reach 1 or 2.
(next-positions '(L 0)) ➜ ((R 1) (R 2))
```

```scheme
(define (next-positions pos)
  __________________________)
```

b) Write fastest-game which should return the number of moves in the fastest possible game. It should work for any non-loopy game!! You may not write any helper functions; just fill in the blanks below. (13 points)

```scheme
;; INPUTS      : pos (The representation of a position of the game)
;; REQUIRES    : (1) primitive-position, do-move and generate-moves
;;             : already defined for the particular game.
;;             : (2) pos must be a valid position
;;             : (3) The game cannot be loopy
;; EXAMPLES    : The number of moves in the fastest possible game (possibly 0)
;; EXAMPLES    : Assuming primitive-position, do-move & generate-moves for
;;             : the game “1,2,...,10”, which encodes its position as (L/R num)... 
;;             : (fastest-game '(L 0)) ➜ 5    E.g., 0→2→4→6→8→10 (5 moves)
;;             : NOTE: The representation of positions differs with each game.
;;             : Assume fastest-game will be called with a valid position
;;             : for that particular game (don’t do any error-checking).

```scheme
(define (fastest-game pos)
  __________________________)
```

(if ____________________________
  __________________________
  ____________________________
  ____________________________
))
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Question 5 – Magical Mystery Fractal, step right this way...  (10 points; 30 min)

We've seen two remarkable fractals, the C-Curve and the Dragon Curve. They are shown below for the first three generations, 0 through 2. The u label helps us remember which direction “up” is – the curve will “bulge” towards it.

a) Draw the n= 2, 3, 4 and ∞ generations below for the new Mystery Curve. You don’t have to draw the arrowheads – we just draw them to highlight the differences between the fractals. If you do draw the arrowheads, draw them very small. If you’re stuck, it might help to draw another iteration of C-Curve or Dragon Curve.

(Use the area below for scratch; put your answers in the boxes above when you’re done.)

a) Below is the code for the Dragon Curve that you’ve seen before. Change as few lines as possible so that it implements the Mystery Curve. When changing a line, circle the number above and write the new line to the right of it.

(define (fractal P0 P1 n)                        ;; 1
  (if (= level 0)                                ;; 2
    (draw-  line-    P P0 P1)                        ;; 3
    (let ((Pm (coord- P P0 P1 (make- V -½ ½)))))) ;; 4
      (fractal P0 Pm (- n 1))                      ;; 5
      (fractal P1 Pm (- n 1)))) ))))              ;; 6
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**Question 6 – It’s a small world after all (aka MapReduce) (15 points; 30 min)**

For both problems, assume `identity` is defined as usual:  

\[
\text{(define (identity } n) n)
\]

a) Fill in the blanks below. The file "/randoms" has 10 random numbers, and "/shakesp" has the collected works of William Shakespeare.

\[
\begin{align*}
\text{(reduce-map-} & \text{____ } \text{_____________} \text{_____________ } \text{"/randoms")} \\
& \text{;; return largest digit in "/randoms"}
\end{align*}
\]

\[
\begin{align*}
\text{(reduce-map-} & \text{____ } \text{_____________} \text{_____________ } \text{"/randoms")} \\
& \text{;; return } \#t \text{ if 42 (my lucky number) is in "/randoms", } \#f \text{ otherwise}
\end{align*}
\]

\[
\begin{align*}
\text{(reduce-map-} & \text{____ } \text{_____________} \text{_____________ } \text{"/shakesp")} \\
& \text{;; return number of lines Shakespeare wrote}
\end{align*}
\]

We modify `reduce-map-word` so the left-to-right ordering of the inputs is preserved in the map and reduce stage, but the reducing can be paired up any way it wants. There can be many equally possible reductions. How many, though? Let’s see a specific example.

b) How many possible reductions (as a function of `n`) are there for a call to the function `reduce-map-word f identity "numbers"`, if the numbers file contains the numbers 1 through `n` on different lines? You may find `1upto` useful, which returns a sentence of the numberss 1 upto (not including) `n`. E.g., `(1upto 5) ⨆ (1 2 3 4)

\[
\text{(num-reduces 1) } \Rightarrow \text{ 1 } \text{;; 1} \leftarrow \text{(reduce f } '(1)) \text{ doesn’t even call f, so 1 reduction}
\]

\[
\begin{array}{ll}
\text{(num-reduces 2) } & \Rightarrow \text{ 1 } \text{;; (f 1 2)} \\
\text{1 2} & \text{1 2 3}
\end{array}
\]

\[
\begin{array}{ll}
\text{(num-reduces 3) } & \Rightarrow \text{ 2 } \text{;; (f 1 (f 2 3))} \\
\text{1 2 3} & \text{1 2 3}
\end{array}
\]

\[
\begin{array}{ll}
\text{(num-reduces 4) } & \Rightarrow \text{ 5 } \text{;; Below. See the pattern? E.g., (num-reduces 3) is in there...}
\end{array}
\]

\[
\begin{array}{llllll}
\text{(f 1 (f 2 (f 3 4))} & \text{(f 1 (f (f 2 3) 4))} & \text{(f (f 1 2) 4))} & \text{(f (f 1 2) (f 3 4))} & \text{(f (f (f 1 2) 3) 4))} & \text{(f (f (f 1 2) 3) 4)}
\end{array}
\]

\[
\begin{array}{llll}
1 2 3 4 & 1 2 3 4 & 1 2 3 4 & 1 2 3 4 & 1 2 3 4
\end{array}
\]

\[
\text{(num-reduces 5) } \Rightarrow \text{ 14 } \text{;; Too many to print}
\]

\[
\begin{align*}
\text{(define (num-reduces } n) \\
& \text{(if (< } n 3) \text{ 1)}
\end{align*}
\]