

CS61A Notes – Week 10: Vectors, concurrency

Just When You Were Getting Used to Lists

Finally we are now introducing to you what many of you already know – arrays. Roughly, an array is a contiguous block of memory – and this is why you can have “instantaneous”, random access into the array, instead of having to traverse down the many pointers of a list.

Recall the vector operators:

```
(vector [element1] [element2] ...) => works just like (list [element1] ...)
(make-vector [num]) => creates a vector of num elements, all unbound
(make-vector [num] [init-value]) => creates a vector of num elements, all set to init-value
(vector-ref v i) => v[i]; gets the ith element of the vector v
(vector-set! v i val) => v[i] = val; sets the ith element of the vector v to val
(vector-length v) => returns the length of the vector v
```

Beyond using different operators, there are a few big differences between vectors and lists:

Vectors of length N

- a contiguous block of memory cells
- $O(1)$ for accessing any item in the vector
- $O(N)$ for adding an item to the middle of the vector, since you have to move the rest of the vector down
- $O(N)$ for growing a vector; you have to *reallocate* a new, larger block of memory!
- add 1 to index to get next element
- you may have “unbound” elements in the vector; that is, length of vector is not the same as length of valid data

Lists of length N

- many units of two cells linked together by pointers
- $O(N)$ for accessing an item
- $O(1)$ for inserting an item anywhere in the list, assuming we have a pointer to the location
- $O(1)$ for growing a list; just add it at the beginning or the end (if you have a pointer to the end)
- `cdr` down a list
- length of list is exactly the number of elements you've put into the list

Note the last bullet. With lists, you allocate a new piece of memory (using `cons`) when you need to add an element, but with vector, you allocate all the memory you need first, even if you don't have enough data to fill it up.

Also, just as you can have deep lists, where elements of a list may be a list as well, you can also have “deep” vectors, often referred to as n-dimensional arrays, where n refers to how “deep” the deep vector is. For example, a table would be a 2-dimensional array – a vector of vectors. Note that, unlike in, say, C, your each vector in your 2D table does NOT have to have the same size! Instead, you can have variable-length rows inside the same table. In this sense, the vectors of Scheme are more like the arrays of Java than C.

QUESTIONS

1. Write a procedure (`sum-of-vector v`) that adds up the numbers inside the vector. Assume all data fields are valid numbers.

2. Write a procedure (`vector-copy! src src-start dst dst-start length`). After the call, `length` elements in vector `src` starting from index `src-start` should be copied into vector `dst` starting from index `dst-start`.

```
STk> a => #(1 2 3 4 5 6 7 8 9 10)
STk> b => #(a b c d e f g h i j k)
STk> (vector-copy! a 5 b 2 3) => okay
STk> a => #(1 2 3 4 5 6 7 8 9 10)
STk> b => #(a b 6 7 8 f g h i j k)
```


A bit of syntax. To run things concurrently, we use a Scheme primitive called `parallel-execute`, a procedure that takes in any number of “thunks” – procedures that take no arguments – and executes the thunks in parallel. For example,

```
(define x 5)
(parallel-execute (lambda () (set! x (+ x 10)))
                  (lambda () (set! x (+ x 20))))
```

will attempt to set `x` to `(+ x 10)` and set `x` to `(+ x 20)` at the same time. Again, the computer “cheats” by interleaving operation between the different thunks. The answer that we want, of course, is 35 – we want the two thunks executed at the same time, but we still want the result to be *as if they executed consecutively*.

Now, consider this simple Scheme expression:

```
(set! x (+ x 10))
```

What looks like one Scheme operation is actually *three* operations:

1. lookup the value of `x`
2. add the value of `x` to 10
3. store the result into `x`

Thus, consider the above call to `parallel-execute`, and keep in mind that the two thunks can be interleaved arbitrarily:

- lookup value of `x`
- add 10 to the value of `x`
- set `x` to the result
- lookup value of `x`
- add 20 to the value of `x`
- set `x` to the result

If the operations were interleaved in the above manner (not interleaved at all), then the value of `x` at the end is 35.

- lookup value of `x`
- add 10 to the value of `x`
- set `x` to the result
- lookup value of `x`
- add 20 to the value of `x`
- set `x` to the result

In the above interleaving, the value of `x` ends up being 15. This is not what we wanted!

QUESTION: What are the possible values of `x` after the below?

```
(define x 5)
(parallel-execute (lambda () (set! x (* x 2)))
                  (lambda () (if (even? x)
                                (set! x (+ x 1))
                                (set! x (+ x 100))))))
```

Concurrency: The Series

We use something called “serializers” to make sure that certain chunks of code are executed *together*. First, we need a way to create a serializer:

```
(define x-protector (make-serializer))
```

That was easy. A serializer takes in a procedure, and creates a *serialized* version of that procedure. So,

```
(define protected-plus-10 (x-protector (lambda () (set! x (+ x 10)))))  
(define protected-plus-20 (x-protector (lambda () (set! x (+ x 20)))))
```

`protected-plus-10` still does the same thing as the original `thunk` – take in no arguments, and add 10 to `x`. However, because `protected-plus-10` and `protected-plus-20` are created *with the same serializer*, their instructions *will not be interleaved*. Therefore, in doing,

```
(parallel-execute protected-plus-10 protected-plus-20)
```

you can always be sure that `x` will be set to 35 at the end.

There’s also a primitive object called a “mutex” that’s even lower level than serializers (in fact, serializers are implemented with mutexes). You can interact with a mutex this way:

```
(define m (make-mutex))  
(m `acquire) ;; “reserves” the mutex  
(m `release) ;; “releases” the mutex
```

Once one program has acquired a mutex, if another wants to acquire the same mutex, it must wait until the mutex is released. So we can do this to obtain the same result:

```
(define x-mutex (make-mutex))  
(parallel-execute  
  (lambda () (x-mutex `acquire) (set! x (+ x 10)) (x-mutex `release))  
  (lambda () (x-mutex `acquire) (set! x (+ x 20)) (x-mutex `release)))
```

The calls to acquire and release a mutex marks the *critical sections* of the code – sections that should *not* be interleaved with other processes also needing the same mutex.

When working with concurrency, there are four potential kinds of problems:

1. **incorrectness** – like the second interleaving example above, the answer you get might just be wrong
2. **inefficiency** – you could lock up the whole computer and always run only one program at a time, but that’s horribly inefficient
3. **deadlocks** – if two programs are competing for the same two resources, there can be deadlocks
4. **unfairness** – one program may be unfairly favored to do more work than another

QUESTION: The Dining Politicians Problem. Politicians like to congregate once in a while, eat and spew nonsense. One slow Saturday afternoon, three politicians meet to have such wild fun. They sit around a circular table; however, due to the federal deficit (funny that these notes are timeless), they are provided with only three chopsticks, each lying in between two people. A politician will be able to eat only when both chopsticks next to him are not being used. If he cannot eat, he will just spew nonsense.

1. Here is an attempt to simulate this behavior:

```
(define (eat-talk i)
  (define (loop)
    (cond ((can-eat? i)
           (take-chopsticks i)
           (eat-a-while)
           (release-chopsticks i))
          (else (spew-nonsense))))
  (loop)
  (loop))

(parallel-execute (lambda () (eat-talk 0))
                  (lambda () (eat-talk 1))
                  (lambda () (eat-talk 2)))

;; a list of chopstick status, #t if usable, #f if taken
(define chopsticks `(#t #t #t))

;; does person i have both chopsticks?
(define (can-eat? i)
  (and (list-ref chopsticks (right-chopstick i))
       (list-ref chopsticks (left-chopstick i))))

;; let person i take both chopsticks
;; assume (list-set! ls i val) destructively sets the ith element of
;; ls to val
(define (take-chopsticks i)
  (list-set! chopsticks (right-chopstick i) #f)
  (list-set! chopsticks (left-chopstick i) #f))

;; let person i release both chopsticks
(define (release-chopsticks i)
  (list-set! chopsticks (right-chopstick i) #t)
  (list-set! chopsticks (left-chopstick i) #t))

;; some helper procedures
(define (left-chopstick i) (if (= i 2) 0 (+ i 1)))
(define (right-chopstick i) i)
```

Is this correct? If not, what kind of hazard does this create?

2. Here's a proposed fix:

```
(define protector (make-serializer))
(parallel-execute (protector (lambda () (eat-talk 0)))
                  (protector (lambda () (eat-talk 1)))
                  (protector (lambda () (eat-talk 2))))
```

Does this work?

3. Here's another proposed fix: use one mutex per chopstick, and acquire both before doing anything:

```
(define protectors
  (list (make-mutex) (make-mutex) (make-mutex)))

(define (eat-talk i)
  (define (loop)
    ((list-ref protectors (right-chopstick i)) `acquire)
    ((list-ref protectors (left-chopstick i)) `acquire)
    (cond ... ;; as before)
    ((list-ref protectors (right-chopstick i)) `release)
    ((list-ref protectors (left-chopstick i)) `release)
    (loop))
  (loop))
```

Does that work?

4. What about this:

```
(define m (make-mutex))
(define (eat-talk i)
  (define (loop)
    (m `acquire)
    (cond ... ;; as before)
    (m `release)
    (loop))
  (loop))
```

5. So what would be a good solution?

(Note: This problem is commonly referred to as "The Dining Philosophers" problem. However, here at Berkeley, we prefer to look down on politicians rather than philosophers.)