A list is an ordered collection of values. In Python, we can have lists of whatever values we want, be it integers, strings, functions, or even other lists! Furthermore, the types of the list’s contents need not be the same; in other words, the list need not be homogenous. Lists are dynamic, so we can add, change, and remove elements whenever we like. Let’s look at an example:

```python
>>> fantasy_team = []
>>> fantasy_team.append("frank gore")
>>> print(fantasy_team)
['frank gore']
>>> fantasy_team.append("calvin johnson")
>>> print(fantasy_team[1])
calvin johnson
>>> fantasy_team.remove("calvin johnson")
>>> fantasy_team[0] = "aaron rodgers"
>>> print(fantasy_team)
['aaron rodgers']
```

Lists can be created using square braces, and likewise, their elements can be accessed via square braces (we call this indexing). Lists are zero-indexed; to access their first element, we must index at 0, to access their second element, we must index at 1, and to access their $i^{th}$ element, we must index at $i - 1$. Also handy, we can access the last element at index -1. Let’s try out some indexing basics.
1.1 Basics

1. What would Python print?
   >>> a = [1, 5, 4, 2, 3]
   >>> print(a[0], a[-1])
   >>> a
   >>> len(a)
   >>> 4 in a
   >>> a[1] = [a[1], a[0]]
   >>> a

1.2 List methods

In addition to the indexing operator, lists have many mutating methods, some of which are listed here:

1. `append(el)` → Adds `el` to the end of the list
2. `index(el)` → Returns the index of `el` if it occurs in the list, otherwise errors.
3. `insert(i, el)` → Insert `el` at index `i`
4. `remove(el)` → Removes the first occurrence of `el` in list, otherwise errors
5. `sort()` → Sorts elements of list in place

List methods are called via ‘dot notation’, as in:

>>> colts = ['andrew luck', 'reggie wayne']
>>> colts.append('trent richardson')
1. Write a function that removes all instances of an element from a list.

```python
def remove_all(el, lst):
    """Removes all instances of el from lst.
    >>> x = [3, 1, 2, 1, 5, 1, 1, 7]
    >>> remove_all(1, x)
    >>> x
    [3, 2, 5, 7]
    """
```

2. Write a function that takes in two values \( x \) and \( y \), and a list \( l \), and adds as many \( y \)'s to the end of the list as there are \( x \)'s. Do not use the built-in function count.

```python
def add_this_many(x, y, lst):
    """ Adds y to the end of lst the number of times x occurs in lst.
    >>> lst = [1, 2, 4, 2, 1]
    >>> add_this_many(1, 5, lst)
    >>> lst
    [1, 2, 4, 2, 1, 5, 5]
    """
```

### 1.3 Slicing

If we’d like to get back parts of the list, as opposed to single elements, we slice the list. Slicing a list returns us a copy subset of the original list. To slice, we use the following syntax:

\[
\text{lst[start:end:step]}
\]

where start, end, and step are integers. The slice includes every other step elements starting at the start index and up to but not including end index. In other words, it includes elements at indices start, start+1*step, start+2*step, start+3*step, and so on up to end. It
is legal to omit one or more of start, end, and step; they default to 0, \(\text{len}(\text{lst})\), and 1, respectively. Start and end can be negative, meaning you count from the end.

```python
>>> a = [0, 1, 2, 3, 4, 5, 6]
>>> a[1:4]
[1, 2, 3]
>>> a[1:6:2]
[1, 3, 5]
>>> a[:4]
[0, 1, 2, 3]
>>> a[3:]
[3, 4, 5, 6]
>>> a[1:4:]
[1, 2, 3]
>>> a[-1:]
[6]
```

1. What would Python print?

```python
>>> a = [3, 1, 4, 2, 5, 3]
>>> a[:4]

>>> a

>>> a[1::2]

>>> a[:]

>>> a[4:2]

>>> a[1:-2]

>>> a[::-1]
```
1.4 For loops

There are two common methods of looping through lists.

- `for el in lst` → loops through the elements in lst
- `for i in range(len(lst))` → loops through the valid, positive indices of lst

If you do not need indices, looping over elements is usually more clear. Let’s try this out.

1. Reverse a list in place, meaning mutate the passed in list itself, instead of returning a new list.

   ```python
def reverse(lst):
    """ Reverses lst in place.
    >>> x = [3, 2, 4, 5, 1]
    >>> reverse(x)
    >>> x
    [1, 5, 4, 2, 3]
    """
   ```

2. Write a function that rotates the elements of a list to the right by k. Elements should not "fall off"; they should wrap around the beginning of the list. rotate should return a new list. To make a list of n 0’s, you can do this: `[0] * n`

   ```python
def rotate(lst, k):
    """ Return a new list, with the same elements of lst, rotated to the right k.
    >>> x = [1, 2, 3, 4, 5]
    >>> rotate(x, 3)
    [3, 4, 5, 1, 2]
    """
   ```
1.5 Higher order functions and list comprehensions

Many times, we wish an operation to be applied to all elements of a list. Python has methods built-in to help us with these tasks (except reduce which has been hidden in Python3):

- `map(fn, lst)` → applies fn to each element in lst
- `filter(pred, lst)` → keeps those elements in lst that satisfy the predicate
- `reduce(accum, lst, zero_value)` → repeatedly calls the accumulator, which takes in two arguments and returns a single value, on elements of lst.

We can also use higher order functions in list comprehensions. List comprehensions are a compact way to apply some operations to a sequence. They look like this:

```
[expression for value in sequence if predicate]
```

where the if clause is optional.

1. What would Python print?

```python
>>> l_1, l_2 = lambda x: 3*x + 1, lambda x: x % 2 == 0
>>> list(filter(l_2, map(l_1, [1, 2, 3, 4])))

>>> [x*x - x for x in [1, 2, 3, 4] if x > 2]

>>> [[y*2 for y in [x, x+1]] for x in [1, 2, 3, 4]]
```
Recall that dictionaries are data structures that map keys to values. Dictionaries are usually unordered (unlike real-world dictionaries) – in other words, the key-value pairs are not arranged in the dictionary in any particular order. Let’s look at an example:

```python
>>> superbowsls = {'joe montana': 4, 'tom brady':3, 'joe flacco': 0}
>>> superbowsls['tom brady']
3
>>> superbowsls['peyton manning'] = 1
>>> superbowsls
{'peyton manning': 1, 'tom brady': 3, 'joe flacco': 0, 'joe montana': 4}
>>> superbowsls['joe flacco'] = 1
>>> superbowsls
{'peyton manning': 1, 'tom brady': 3, 'joe flacco': 1, 'joe montana': 4}
```

Dictionaries are indexed with similar syntax as sequences, only they use keys, which can be any immutable value, not just numbers. Dictionaries themselves are mutable; we can add, remove, and change entries after creation. There is only one value per key, however, in a dictionary (we call this injective or one-to-one).

1. Continuing from above, what would Python print?

```python
>>> 'colin kaepernick' in superbowsls
False

>>> len(superbowls)
4

>>> superbowsls['peyton manning'] = superbowsls['joe montana']
>>> superbowsls[('eli manning', 'giants')] = 2
>>> superbowsls[3] = 'cat'
>>> superbowsls
```

Dictionaries in general can be arbitrarily deep, meaning their values can be dictionaries themselves. Let’s get practice traversing these deep structures. To do so, we’ll
need to know a couple more things about dictionaries.
To iterate over a dictionary’s keys:

```python
for k in d.keys():
    ...
```

and to remove an entry:

```python
del dictionary[key]
```

2. Given an arbitrarily deep dictionary replace all occurrences of x as a value with y.

```python
def replace_all(d, x, y):
    """Replaces all values of x with y.
    >>> d = {1: {2:3, 3:4}, 2:{4:4, 5:3}}
    >>> replace_all(d,3,1)
    >>> d
    {1: {2: 1, 3: 4}, 2: {4: 4, 5: 1}}
    ""
```

3. Given a (non-nested) dictionary delete all occurrences of a value. You cannot delete items in a dictionary as you are iterating through it.

```python
def rm(d, x):
    """Removes all pairs with value x.
    >>> d = {1:2, 2:3, 3:2, 4:3}
    >>> rm(d,2)
    >>> d
    {2:3, 4:3}
    ""
```