Announcements

• Homework 3 due Wednesday 10/1 @ 11:59pm
  • Homework Party on Monday 9/29, time and place TBD
• Optional Hog Contest due Wednesday 10/1 @ 11:59pm
• Project 2 due Thursday 10/9 @ 11:59pm
Box-and-Pointer Notation
The Closure Property of Data Types

- A method for combining data values satisfies the closure property if:
  - The result of combination can itself be combined using the same method.
  - Closure is the key to power in any means of combination because it permits us to create hierarchical structures.
  - Hierarchical structures are made up of parts, which themselves are made up of parts, and so on.

Lists can contain lists as elements
Box-and-Pointer Notation in Environment Diagrams

Lists are represented as a row of index-labeled adjacent boxes, one per element. Each box either contains a primitive value or points to a compound value.

Interactive Diagram

```
1  pair = [1, 2]
2
3  nested_list = [[1, 2], [],
4     [[3, False, None],
5     [4, lambda: 5]]]
```
Trees
Trees are Nested Sequences

A tree is either a single value called a leaf or a sequence of trees. Typically, some type restriction is placed on the leaves. E.g., a tree of numbers:

```
1  tree = [[1, [2], 3, []],
          [[4], [5, 6]], 7]
```
Tree Processing Uses Recursion

(Demo)

Processing a leaf is often the base case of a tree processing function.

The recursive case often makes a recursive call on each branch and then aggregates.

```python
def count_leaves(tree):
    """Count the leaves of a tree."""
    if is_leaf(tree):
        return 1
    else:
        branch_counts = [count_leaves(b) for b in tree]
        return sum(branch_counts)
```
Discussion Question

Complete the definition of flatten, which takes a tree and returns a list of its leaves

*Hint*: If you `sum` a sequence of lists, you get 1 list containing the elements of those lists

```python
>>> sum([[1], [2, 3], [4]], [])
[1, 2, 3, 4]
>>> sum([[1]], [])
[1]
>>> sum([[1]], [2]), []
[[1], 2]
```

```python
def flatten(tree):
    """Return a list containing the leaves of tree."
    if is_leaf(tree):
        return [tree]
    else:
        return sum([flatten(b) for b in tree], [])

def is_leaf(tree):
    return type(tree) != list
```

```python
>>> tree = [[1, [2], 3, []], [[4], [5, 6]], 7]
>>> flatten(tree)
[1, 2, 3, 4, 5, 6, 7]
```
Sequence Operations
Membership & Slicing

Python sequences have operators for membership and slicing.

Membership.

```python
>>> digits = [1, 8, 2, 8]
>>> 2 in digits
True
>>> 1828 not in digits
True
```

Slicing.

```python
>>> digits[0:2]  # Slicing creates a new object
[1, 8]
>>> digits[1:]
[8, 2, 8]
```
Binary Trees

Trees may also have restrictions on their structure.

A **binary tree** is either a **leaf** or a sequence containing at most two **binary trees**.

The process of transforming a tree into a binary tree is called **binarization**.

```python
def right_binarize(tree):
    """Construct a right-branching binary tree."

    >>> right_binarize([1, 2, 3, 4, 5, 6, 7])
    [1, [2, [3, [4, [5, [6, 7]]]]]]

    if is_leaf(tree):
        return tree
    if len(tree) > 2:
        tree = [tree[0], tree[1:]]
    return [right_binarize(b) for b in tree]
```

All but the first branch are grouped into a new branch.
Strings
Strings are an Abstraction

Representing data:

'200'    '1.2e-5'    'False'    '(1, 2)'

Representing language:

""""""And, as imagination bodies forth
The forms of things to unknown, and the poet's pen
Turns them to shapes, and gives to airy nothing
A local habitation and a name.
"""

Representing programs:

'curry = lambda f: lambda x: lambda y: f(x, y)'

(Demo)
String Literals Have Three Forms

```python
>>> 'I am string!' 'I am string!'

>>> "I've got an apostrophe" "I've got an apostrophe"

>>> '您好' '您好'

>>> """The Zen of Python claims, Readability counts. Read more: import this."""
'The Zen of Python\nclaims, Readability counts.\nRead more: import this.'
```

- Single-quoted and double-quoted strings are equivalent
- A backslash "escapes" the following character
- "Line feed" character represents a new line
Strings are Sequences

Length and element selection are similar to all sequences

```python
>>> city = 'Berkeley'
>>> len(city)
8
>>> city[3]
'k'
```

However, the "in" and "not in" operators match substrings

```python
>>> 'here' in "Where's Waldo?"
True
>>> 234 in [1, 2, 3, 4, 5]
False
>>> [2, 3, 4] in [1, 2, 3, 4, 5]
False
```

When working with strings, we usually care about whole words more than letters
Dictionaries

{"Dem": 0}
Limitations on Dictionaries

Dictionaries are unordered collections of key-value pairs.

Dictionary keys do have two restrictions:

• A key of a dictionary cannot be a list or a dictionary (or any mutable type)

• Two keys cannot be equal; There can be at most one value for a given key

This first restriction is tied to Python's underlying implementation of dictionaries

The second restriction is part of the dictionary abstraction

If you want to associate multiple values with a key, store them all in a sequence value