Outline
- Tuples, List, Dictionaries
- Recursion
- Nonlocal
- Environment Diagrams
- Equality vs. Identity
- Data Abstraction
- OOP
- Rlists

Tuples, Lists, Dictionaries
- Tuples
  - Hold elements in an immutable data structure
- Lists
  - Hold elements in a mutable data structure
- Dictionaries
  - Hold key, value pairs in a mutable data structure
    - Keys must be immutable

What does Python Display?

```python
>>> a = (1,2,3,4)
>>> a[::-1]
(4, 3, 2, 1)
>>> a = a[:0:-1]
>>> a
(4,3,2)
>>> b = [1,2,3,4]
>>> b[3] = a[1:]
[1,2,3,(3,2)]
>>> b[3][0] = a[:-2]
```

Write a function `path_exists` that takes in a dictionary, `friends` mapping every person to the list of their friends, and returns whether it is possible to move from the person `start` to the person `finish` by following friend relationships.

```python
def find_path(friends, start, finish):
    """
    >>> allfriends = {
        "Soumya": ["Julia"],
        "Julia": ["Mark", "Amin", "Soumya"],
        "Keegan": ["Robert", "Sharad"]
    }
    >>> find_path(allfriends, "Soumya", "Mark")
    True
    >>> find_path(allfriends, "Soumya", "Keegan")
    False
    """
```
Find Path - Solution

```python
def find_path(friends, start, finish):
    def find_path2(visited, start):
        if start == finish:
            return True
        if start in friends:
            for vertex in friends[start]:
                if vertex not in visited:
                    visited.append(vertex)
                    if find_path2(visited, vertex):
                        return True
        return False
    return find_path2([], start)
```

Recursion

- Divide a problem into smaller subproblems
  - It's like divide and conquer!
- Figure out the base case(s)
- When calling the recursive function, assume it works

Fibonacci

```python
def fib(n):
    if n == 0:
        return 0
    elif n == 1:
        return 1
    return fib(n - 1) + fib(n - 2)
```

Mutating Map

Define a function `m_map()` that will recursively map a function to each element in a list, mutating the original one. It can be done in place.

```python
def m_map(f, lst):
    """
    Takes in a list and recursively maps a function over each element, mutating the original.
    """
    if lst:
        elem = f(lst.pop())
        m_map(f, lst)
        lst.append(elem)
```

Mutating Map – Solution
Deep Map

Write a function `deep_map(f, lst)` which applies a one-argument function onto every element in the given list. If an element is itself a list, then you should recursively apply the function onto each of its elements. You should NOT return anything—instead, mutate the original list (and any nested lists).

```python
def deep_map(f, lst):
    if lst:
        last = lst.pop()
        if type(last) == list:
            deep_map(f, last)
        else:
            last = f(last)
        deep_map(f, lst)
    lst.append(last)
```

Deep Map – Solution

Nonlocal

- Tells Python that it is allowed to modify the binding for a declared variable in a parent frame
  - does not work for global variables
- Variable should already exist
- Python will **not** create a copy in the local frame

What does this function do?

```python
def make_mystery_sequence():
    n = 0
    x, y = 1, 1
    def mystery():
        nonlocal n, x, y
        if n == 0:
            n += 1
            return x
        elif n == 1:
            n += 1
            return y
        else:
            x, y = y, x + y
            return mystery
    return mystery
```

Fibonacci sequence!

make_delayed_repeater()

Write a function that returns a function that returns the last thing it received (the first time it's called, it returns '...')

```python
>>>slowpoke = make_delayed_repeater()
>>>slowpoke("hi")
...
>>>slowpoke("hello?")
hi
>>>slowpoke("stop repeating what I'm saying")
hello?
```
Solution

```python
def make_delayed_repeater():
    my_phrase = "..."

def repeater(phrase):
    nonlocal my_phrase
    to_return = my_phrase
    my_phrase = phrase
    return to_return
return repeater
```

Environment Diagram

```python
def sillylist(mine, next):
    def cont():
        nonlocal cont
        cont = next
        return mine
    return cont

s = sillylist(1, sillylist(5, None))
s()
s()
```

Another Environment Diagram

```python
def go():
    def foo(a, b, c):
        return foo(a, b, c)
    def bar(a, b, c):
        return a+b+c
    def two():
        nonlocal foo, bar
        foo, bar = bar, foo
        return 2
    return foo(1, two(), 3)
print(go())
```

Equality vs. Identity

- **Equality**
  - checks if two items are equivalent
  - use the `==` operator
    - internally, Python calls `__eq__()`
- **Identity**
  - checks if two items are the same object
  - stronger condition than equality
  - use the `is` operator
    - internally, Python calls `__is__()`
Equality vs. Identity

```python
>>> l1, l2 = list(range(5)), list(range(5))
>>> l1 == l2
True
>>> l1 is l2
False
>>> l2 = l1
>>> l1 is l2
True
>>> d1, d2 = {1: 3, 5: 7}, {5: 7, 1: 3}
>>> d1 == d2
True
>>> d1 is d2
False
```

Data Abstraction

- We want to store data, i.e. numbers, strings, etc. in an organized way that allows us (and others!) to use it easily.

- Two major concerns:
  - How we store the data (lists, tuples, other data structures)
  - How we use the data (constructors, selectors)

How do we represent data types?

- In Python, we have several ways
  - Object oriented programming
  - Data Abstraction with constructors and selectors
  - Dispatch Functions
  - ...

```
Data Abstraction

def make_rlist(first, rest):
    return (first, rest)
def first(rlist):
    return rlist[0]
def rest(rlist):
    return rlist[1]

#make sure you don't violate abstraction!
def popped1(rlist):
    return rlist[1]
def popped2(rlist):
    return rest(rlist)
```

Dispatch Functions

def make_donkey(name):
    weight_carried = 0
    max_carry = 5
def dispatch(msg):
    if msg=='carry':
        nonlocal weight_carried
        weight_carried+=1
    if msg=='talk':
        if dispatch("alive"):
            print("hee-haw, my name is", name)
    if msg=='alive':
        #Dies if you made it carry too much
        return weight_carried<=max_carry
    return dispatch
Object Oriented Programming

The Donkey from Earlier as a Class

```python
class Donkey:
    max_carry = 5
    def __init__(self,name):
        self.weight_carried = 0
        self.name = name
    def carry(self):
        self.weight_carried += 1
    def talk(self):
        if self.alive:
            print("hee-haw, my name is",self.name)
    @property
def alive(self):
        return self.weight_carried <= max_carry
```

Create a new AdultDonkey class that Implements Breeding

```python
>>> d = AdultDonkey("Dopey")
>>> e = AdultDonkey("Jazz")
>>> f = d.breed_with(e)
>>> f.talk()
hee-haw, my name is Dopey Jr.
>>> for _ in range(10):
...     f.carry()
>>> d.talk()
hee-haw, my name is Dopey
>>> f.talk()
```

Name credit: [http://www.wookeyfarm.com/2012/05/99-donkey-names/](http://www.wookeyfarm.com/2012/05/99-donkey-names/)

Solution

```python
class AdultDonkey(Donkey):
    def breed_with(self, other):
        return Donkey(self.name + " Jr.")
```

Let's also make a StrongDonkey that can carry up to 100 things inclusive

```python
>>> s = StrongDonkey("arnold schwarzedonkey")
>>> for _ in range(100):
...     s.carry()
>>> s.alive
True
>>> s.carry()
>>> s.alive
False
>>> s.breed
<bound method ...>
```

Solution

```python
class StrongDonkey(Donkey):
    max_carry=100
    #but we also want strong donkeys to breed
    #into strong donkeys
    def breed_with(self, other):
        return StrongDonkey(self.name + " Jr.")
```
Mutable Rlist Class

```python
class Rlist(object):
    class EmptyList(object):
        def __len__(self):
            return 0
        empty = EmptyList()
        def __init__(self, first, rest=empty):
            self.first = first
            self.rest = rest
        def __len__(self):
            return 1 + len(self.rest)
        def __getitem__(self, i):
            if i == 0:
                return self.first
            return self.rest[i - 1]
```

insert()

Write a function insert that takes in an Rlist, an index, and a value, inserting the value at the index position in the Rlist. It should mutate the original Rlist.

```python
def insert(rlist, index, value):
    """Mutatively insert VALUE at INDEX in the RLIST."""
    for _ in range(index):
        rlist = rlist.rest
    rlist.rest = Rlist(value, rlist.rest)
```

sort_rlist(rlist)

Write a function to sort a given rlist in an increasing order. You may assume that values stored in the rlist are integers.

```python
def sort_rlist(rlist):
    if rlist is Rlist.empty or rlist.rest is Rlist.empty:
        return
    new = Rlist(rlist.first)
    rlist = rlist.rest
    while rlist != Rlist.empty:
        pointer = new
        tmp = rlist.first
        while pointer != Rlist.empty:
            if tmp <= pointer.first:
                tmp_first = pointer.first
                pointer.first = tmp
                pointer.rest = Rlist(tmp_first, pointer.rest)
                break
            if pointer.rest is Rlist.empty:
                pointer.rest = Rlist(tmp, pointer.rest)
                break
            pointer = pointer.rest
        rlist = rlist.rest
    return new
```
```python
def h(x):
    def g(w):
        if w == x:
            return 5
        if x in [2, 3, 4]:
            return 4
        if x[0] == y:
            return 3
        if y == x[0]:
            return 2
    return f(y)

def f(y):
    nonlocal x
    x[0], y[0] = x, z
    return g(y)

z = x[1:]
return f(x[:])

y = [1, 2, 3, 4]
x = 21
h(y)
```

**Extra question! - Env Diagram!**

```python
def h(x):
    def g(w):
        if w == x:
            return 5
        if x in [2, 3, 4]:
            return 4
        if x[0] == y:
            return 3
        if y == x[0]:
            return 2
    return f(y)

def f(y):
    nonlocal x
    x[0], y[0] = x, z
    return g(y)

z = x[1:]
return f(x[:])

y = [1, 2, 3, 4]
x = 21
h(y)
```