CS61A Lecture 31
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Announcements
- HW9 due tonight
- Ants extra credit due tonight
  - See Piazza for submission instructions
- Hog revisions out, due Monday
- HW10 out tonight

Pairs
Scheme has built-in pairs that use weird names:
- **cons:** Two-argument procedure that creates a pair
- **car:** Procedure that returns the first element of a pair
- **cdr:** Procedure that returns the second element of a pair

A pair is represented by a dot between the elements, enclosed in parentheses

```
> (cons 1 2)
(1 . 2)
> (car (cons 1 2))
1
> (cdr (cons 1 2))
2
```

Recursive Lists
A recursive list can be represented as a pair in which the second element is a recursive list or the empty list

Scheme lists are recursive lists:
- **nil** is the empty list
- A non-empty Scheme list is a pair in which the second element is nil or a Scheme list

Scheme lists are written as space-separated combinations

```
> (define x (cons 1 (cons 2 (cons 3 (cons 4 nil)))))
> x
(1 2 3 4)
> (cdr x)
(2 3 4)
> (cons 1 (cons 2 (cons 3 4)))
(1 2 3 4)
```

Symbolic Programming
Symbols are normally evaluated to produce values; how do we refer to symbols?

```
> (define a 1)
> (define b 2)
> (list a b)
(1 2)
```

Quotation prevents something from being evaluated by Lisp

```
> (list 'a 'b)
(a b)
> (list 'a 'b)
(a 2)
```

Quotation can also be applied to combinations to form lists

```
> (car '(a b c))
a
> (cdr '(a b c))
(b c)
```

Scheme Lists and Quotation
Dots can be used in a quoted list to specify the second element of the final pair

```
> (cdr (cdr '(1 2 . 3)))
3
```

However, dots appear in the output only of ill-formed lists

```
> '(1 2 . 3)
(1 2 . 3)
> '(1 2 . (3 4))
(1 2 3 4)
> '(1 2 . nil)
(1 2 3)
```

What is the printed result of evaluating this expression?

```
> (cdr '((1 2 . (3 4 . (5)))))
(3 4 5)
```
The Let Special Form

Let expressions introduce a new frame, with the given bindings

```
(let ([<name> <exp>] ...) <body>)
```

```
(define (filter fn s)
  (if (null? s)
      s
      (let ((first (car s))
            (rest (filter fn (cdr s))))
          (if (fn first)
              (cons first rest)
              rest)))))
> (filter even? '(1 2 3 4 5 6 7))
(2 4 6)
```

Quick Sort

Quick sort algorithm:
1. Choose a pivot (e.g. first element)
2. Partition into three pieces: < pivot, = pivot, > pivot
3. Recurse on first and last piece

```
(define (filter-comp comp pivot s)
  (filter (lambda (x) (comp x pivot)) s))
(define (quick-sort s)
  (if (<= (length s) 1)
      s
      (let ((pivot (car s)))
          (append (quick-sort (filter-comp < pivot s))
                  (filter-comp = pivot s)
                  (quick-sort (filter-comp > pivot s))))))
```

The Begin Special Form

Begin expressions allow sequencing

```
(begin <exp> <exp> ... <exp>)
```

```
(define (repeat k fn)
  (if (> k 0)
      (begin (fn) (repeat (- k 1) fn))
      'done))

(define (tri fn)
  (repeat 3 (lambda () (fn) (lt 120))))

(define (sier d k)
  (tri (lambda () (if (= k 1) (fd d) (leg d k))))))

(define (leg d k)
  (sier (/ d 2) (- k 1)) (penup) (fd d) (pendown))
```