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Lecture 30: User-Defined Special Forms and Streams, Project 4

Defining Syntax

• Scheme provides a powerful (but rather tricky) way to create new special forms: define-synt.
• One of the extensions of our project is a simpler, more traditional form of this: define-macro.
• Macros are like functions, but
  – Do not evaluate their arguments (this is what makes them special forms).
  – Automatically treat the returned value as a Scheme expression and execute it.
• Thus, macros "write" programs that then get executed.

Macro Example

(define-macro (while cond stmt)
  '(begin (define ($loop$) (if ,cond (begin ,stmt ($loop$)))))

• This uses the convenient quasiquote (backquote), another project extension. Quasiquote is like quote, but
  – Everything preceded by a comma is replaced by its value:
  – Everything preceded by ',@' is evaluated and its value spliced in.
    '(a b ,(+ 2 3)) ===> (a b 5)
    '(a b ,@((list (+ 2 3) (- 2 1)) d) ===> (a b 5 1 d)

• So (while (> x y) (set! x (f y))) first yields
  (begin (define ($loop$)
     (if (> x y) (begin (set! x (f y)) ($loop$))));)

• And then this is executed.

A Macro for Streams

• Syntax extension allows us to define a convenient kind of stream in Scheme.
• As we did in Python, a stream in Scheme will consist of a head, and either a function to compute the tail or the tail itself.
  (define-macro (cons-stream head tail)
    '(cons ,head (lambda () ,tail))

• We’ll need a special cdr function that calls the tail computation (if it is a function).
  (define (cdr-stream str)
    (if (procedure? (cdr str))
      ; Compute and memoize tail
      (set-car! str ((cdr str))))
      (cdr str))

• Actually, these are built into our (fully extended) project.
**Streams in Scheme**

```scheme
;; The stream of all 1’s
(define ones (cons-stream 1 ones))
(car ones) ===> 1
(car (cdr-stream ones)) ===> 1

(define (add-streams a b) ; Infinite streams, that is
(cons-stream (+ (car a) (car b))
(add-streams (cdr-stream a) (cdr-stream b))))

;; The stream 1 2 3 ...
(define nums (cons-stream 1 (add-streams ones nums)))

;; The Fibonacci sequence
(define fib (cons-stream 1
(cons-stream 1
(add-streams fib (cdr-stream fib))))))
```

**Major Pieces**

- `read_eval_print` is the main loop of the program, which takes over after initialization. It simply reads Scheme expressions from an input source, evaluates them, and (if required) prints them, catching errors and repeating the process until the input source is exhausted.
- `tokenize_lines` in `scheme_tokens.py` turns streams of characters into tokens. You don’t have to write it, but you should understand it.
- The function `scheme_read` parses streams of tokens into Scheme expressions. It’s a very simple example of a recursive-descent parser.
- The class `Frame` embodies environment frames. You fill in the method that creates local environments.
- The class `Evaluation` is used in the extra-credit part for evaluating expressions in tail contexts.
- A hierarchy of classes represent functions.
- `scheme_primitives.py` defines the basic Scheme expression data structure (aside from functions) and implements the "native" methods (those implemented directly in the host language: Python, or in other compilers, C).

**Dealing With Tail Recursion**

- To handle tail recursion, you’ll actually implement a slightly modified version of `scheme_eval`, one which partially evaluates its argument, performing one "evaluation step."
- Each evaluation step returns either a value (in which case, evaluation of the expression is done), or another expression and the environment in which to evaluate it.
- So now Python can iterate. Conceptually:

  ```python
  while expr is still an unevaluated expression,
  expr, environ = eval_step(expr, expression)
  return expr
  ```

**Function Calls**

- The idea here is a "mutually recursive dance" between two parties (just like the calculator):
  - `scheme_eval`, which evaluates operator and operands, and
  - `scheme_apply`, which applies functions to the resulting values.
- Interestingly, these just happen to be standard functions in the language we are defining: we could in principle (and fact) interpret Scheme in Scheme metacircularly.
- But if we want to do this in Python, we have to deal with proper tail recursion (i.e., its lack in Python vs. its presence in Scheme).
- That is, a purely tail-recursive function must be able to run arbitrarily long (without overflowing any internal stack).
Example

- Consider problem of getting kth item in list:

  \[
  \text{Element \#K of L} \\
  \text{(define (list-ref L k)} \\
  \text{  (if (= k 0) (car L) (list-ref (cdr L) (- k 1))))}
  \]

- We want to evaluate \(\text{list-ref \ '(3 5 7) 2}\).

Let's represent the state of an evaluation as a stack of "evaluation frames" (class \text{Evaluation}), each of which looks like this when partially evaluated:

<table>
<thead>
<tr>
<th>Expression</th>
<th>Value</th>
<th>Environment</th>
</tr>
</thead>
<tbody>
<tr>
<td>(list-ref (cdr L) (- n 1))</td>
<td>L: (3 5 7), k: 2, globals</td>
<td></td>
</tr>
</tbody>
</table>

or like this when fully evaluated:

<table>
<thead>
<tr>
<th>Expression</th>
<th>Value</th>
<th>Environment</th>
</tr>
</thead>
<tbody>
<tr>
<td>7</td>
<td>L: (7), k: 0, globals</td>
<td></td>
</tr>
</tbody>
</table>

Example: list-ref

\[
\text{(define (list-ref L k)} \\
\text{  (if (= k 0) (car L) (list-ref (cdr L) (- k 1))))}
\]

First, the call:

<table>
<thead>
<tr>
<th>Expression</th>
<th>Value</th>
<th>Environment</th>
</tr>
</thead>
<tbody>
<tr>
<td>(list-ref (1 2 3) 2)</td>
<td></td>
<td>globals</td>
</tr>
</tbody>
</table>

After evaluating the quoted expression, we replace the call with the body:

<table>
<thead>
<tr>
<th>Expression</th>
<th>Value</th>
<th>Environment</th>
</tr>
</thead>
<tbody>
<tr>
<td>(if ...)</td>
<td>L: (3 5 7), k: 2, globals</td>
<td></td>
</tr>
</tbody>
</table>

Now evaluate the condition (recursively, in another \text{Evaluation}):

<table>
<thead>
<tr>
<th>Expression</th>
<th>Value</th>
<th>Environment</th>
</tr>
</thead>
<tbody>
<tr>
<td>(= k 0)</td>
<td>L: (3 5 7), k: 2, globals</td>
<td></td>
</tr>
<tr>
<td>(if ...)</td>
<td>L: (3 5 7), k: 2, globals</td>
<td></td>
</tr>
</tbody>
</table>

Example (contd.)

Evaluate the primitive function call \(-\):

<table>
<thead>
<tr>
<th>Expression</th>
<th>Value</th>
<th>Environment</th>
</tr>
</thead>
<tbody>
<tr>
<td>(#f)</td>
<td>L: (3 5 7), k: 2, globals</td>
<td></td>
</tr>
<tr>
<td>(if ...)</td>
<td>L: (3 5 7), k: 2, globals</td>
<td></td>
</tr>
</tbody>
</table>

Which causes us to replace the \text{if} with its "false" branch:

<table>
<thead>
<tr>
<th>Expression</th>
<th>Value</th>
<th>Environment</th>
</tr>
</thead>
<tbody>
<tr>
<td>(list-ref (cdr L) (- k 1)))</td>
<td>L: (3 5 7), k: 2, globals</td>
<td></td>
</tr>
</tbody>
</table>

Example (contd.)

After evaluating \text{list-ref} (to get a function), \text{(cdr L)}, and \text{(- k 1)} (recursively, each in its own \text{Evaluation}), we replace the call on \text{list-ref} with the body:

<table>
<thead>
<tr>
<th>Expression</th>
<th>Value</th>
<th>Environment</th>
</tr>
</thead>
<tbody>
<tr>
<td>(if ...)</td>
<td>L: (5 7), k: 1, globals</td>
<td></td>
</tr>
</tbody>
</table>

and so on. Thus, the stack of evaluations-in-progress does not keep growing.

Handling Special Forms

- The "special" forms (expressions that don't obey the usual evaluate-all-operands-and-call rule) all get handled by eponymous methods in \text{Evaluation} (e.g., \text{do_cond_form}).

- Unlike \text{apply}, they exert explicit control over their operand's evaluation.

- Some special forms can be rewritten into equivalent Scheme expressions that replace the original, but this is up to the implementor.