Recursive Lists (RLists)

Earlier in the course, we worked with the Immutable Recursive List (IRList), which is an abstract data type consisting of a first (some value) and a rest (another IRList). The end of an IRLList was represented by the empty_irlist:

```python
>>> from irlist import *
>>> c_lst = make_irlist('61a',
                      make_irlist('61b',
                                  make_irlist('61c',
                                             empty_irlist)))
>>> irlist_str(c_lst)
<'61a', '61b', '61c'>
```

For instance, the box-and-pointer diagram of courses would be:

This week, we will work with Mutable Recursive Lists (RLists) that are conceptually exactly the same as an IRLList. An RList has a first and a rest, but unlike an IRLList, you can modify the first and rest of an RList.

Here is a shortened class definition of the RList class:

```python
class RList(object):
```

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1The actual class definition of RList is found at: http://inst.eecs.berkeley.edu/cs61a/su12/lib/rlist.py
the_empty_rlist = EmptyRList()

@staticmethod
def empty():
    return RList.the_empty_rlist

def __init__(self, first, rest=the_empty_rlist):
    self.first = first
    self.rest = rest

def __len__(self):
    return 1 + len(self.rest)
def __getitem__(self, i):
    if i == 0:
        return self.first
    return self.rest[i-1]
def __repr__(self):
    # omitted for brevity
def __str__(self):
    # omitted for brevity

class EmptyRList(object):
    def __repr__(self):
        return "RList.empty()"
def __str__(self):
    return "<""def __len__(self):
    return 0
def __getitem__(self, k):
    raise IndexError("out of bounds: {0}".format(k))

1.1 Python “magic methods”

Just like __init__ is the “special” method name that signals the class constructor, there are other method names that Python will handle specially. These include:

__len__(self)
    Returns the length of this object. The len function will call the object’s __len__ method, if it’s defined.
__getitem__(self, i)
    Returns the element at index i. For instance, when you index into an object, like myobj[2], this is converted into the method call: myobj.__getitem__(i).
_repr_(self)

Returns a string representation of this object with the following rule: if you were to evaluate this string, then it would return the object.

_str_(self)

Returns some string representation of this object. This is much more relaxed than _repr_.

There are many other magic methods in Python, which enable your user-defined classes to more-easily integrate with Python's built-in methods and objects.

1.2 Practice with RLists

1. (Warmup) Define a procedure map_rlist that, given an RList rlist and a function fn, returns a new RList with all values in rlist mapped onto by fn. Don't modify the input RList.

```python
def map_rlist(rlist, fn):
```

2 RLLists and Mutation

Because RList instances are mutable objects, we can modify them directly, instead of, say, creating a new RList when operating over them. For instance, we can mutate an RList by doing:

```python
>>> rlist = RList(3, RList(2, RList(1)))
>>> rlist
<3, 2, 1>
>>> rlist.first = 'meow'
>>> rlist
<meow, 2, 1>
>>> rlist.rest.first = 'bark'
>>> rlist
<meow, bark, 1>
>>> rlist.rest.rest = RList(RList('hi'), RList(42))
>>> rlist
```

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2 Aside from the magic methods that we explicitly cover, you will not be responsible for knowing all of the magic methods.
2.1 More Practice with Rlists

1. (Warmup) Define a procedure `map_rlist` that, given an RList `rlist` and a function `fn`, applies `fn` to every element in `rlist`. Your function should mutate the input `rlist`, and should not create any new RLists.
   
   ```python
   def map_rlist(rlist, fn):
   ```

2. Now, define a procedure `map_rlist_alt` that works just like `map_rlist`, but instead only applies the function to every other element, starting from the first.

   ```python
   def map_rlist_alt(rlist, fn):
   ```

3 Environment Model of Evaluation

In this topic, we will formally go over exactly how programs are executed in Python. In fact, it turns out that many other languages use the Environment Model of Evaluation.

The main idea of the environment model is: All evaluation is done with respect to a frame. For instance, when you type expressions into the interpreter prompt, you are evaluating the expressions with respect to the global frame. On the other hand, expressions or statements that are evaluated within a function body is executed with respect to that function’s local frame.

A frame is a construct that contains two things:

1. All variable bindings that were declared in this frame.
2. An arrow to the parent frame that this frame extends.

The global frame is special, in that all built-in functions and constants are defined here, such as `abs`, `True`, and `pow`. By definition, the global frame has no parent frame, and is the parent frame of all other frames.
An environment is a series of frames, starting from the current frame to the global frame. You can generate the current environment by following parent pointers until you reach the global frame – the set of frames that you passed through to get to the global frame consists of your current environment.

Here is a concise list of how the Environment Model evaluates an expression:

**constants (numbers, strings, etc.)**
These are self-evaluating.

**variables**
Look up the variable name in the current frame. If it doesn’t exist in the current frame, look in the parent frame (and the parent frame of that, etc.), and return the first value with the variable name. If you get to the global frame, and still haven’t found the variable name, then signal an unbound variable error (called a NameError in Python).

**function definitions**
Create a new function object, and add the function binding to the current frame.

**function calls**
Evaluate the operands in the current frame. If the function is a primitive (built-in) procedure, then apply the function by “magic”. Otherwise, it’s a user-defined function: create a new frame F. Bind fn’s formal parameters to the evaluated operands’ values within F. Make F extend the current frame. Finally, evaluate fn’s body with respect to the new frame F.

### 3.1 Environment Diagrams

In this course, we use Environment Diagrams to visually represent the Environment model. An environment diagram consists of two main objects:

**Boxes**
These represent your frames. Within each box, you’ll write out all variable bindings. In addition, each box will have an arrow to its parent frame. You will only create a box when you call a user-defined function. At the very least, you will always have the Global frame present.

**Function Bubbles**
These represent user-defined functions. The left-bubble contains a list of its formal parameters, in addition to the body of the function. The right-bubble contains an arrow that points to the environment in which the function was created. You only create function bubbles when a function is created (either via def or lambda).
In each of your environment diagrams, you’ll always start with the global frame, but you need not include variable bindings for all built-in functions. As an example, here’s the environment diagram for the following sequence of expressions:

```python
>>> honey = 'bear'
>>> mylst = [4, 2, 0]
>>> def make_awesome(str1):
...     return 'awesome_' + str1
```

The interesting thing of note is the function bubble - this object represents the `make_awesome` function. In particular, note that the right-bubble points to the global frame - this is because `make_awesome` was defined in the global frame!

Notice that no new frames have been created yet (we haven’t called any user-defined functions yet!). But when we do call `make_awesome`, the following new frame is created:

```python
>>> result = make_awesome(honey)
```

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3 At times, you might find it helpful to include some built-in functions in your diagrams – see the environment diagram exercise 2.f for an example. If you do, instead of creating a lambda bubble for the built-in functions, use some distinguishing object that signals that this is a built-in function object, not a user-defined function object.
3.2 Practice with Environment Diagrams

1. (Warmup) Draw the environment diagram of the following expressions:

   \[
   a = \lambda x: x^2 + 1 \\
   \text{def } b(x):
   \quad \text{return } x \times y \\
   y = 3 \\
   b(y) \quad \# \text{What is the return value?}
   \]

   DRAW DIAGRAM HERE

   \[
   a = \lambda x: x^2 + 1 \\
   b = \lambda x: x \times y \\
   y = 3 \\
   \text{def } c(x):
   \quad y = a(x) \\
   \quad \text{return } b(x) + a(x+y) \\
   c(y) \quad \# \text{What is the return value?}
   \]

   DRAW DIAGRAM HERE

2. Draw the environment diagram at the indicated locations. If an error occurs, write ERROR:

   \[
   \text{def } \text{square}(x):
   \quad \text{return } x \times x \\
   \text{def } \text{call_it}(fn, n):
   \quad \text{return } fn(n) \\
   n = 22 \\
   \text{call_it(square, n-2)} \quad \# \text{What is the return value?}
   \]
def make_adder(x):
    return lambda y: x + y
add_4 = make_adder(4)
add_4(5)  # What is the return value?

mylst = [1, 2, 'yay']
def modify_it_maybe(lst):
    lst = ['this', 'is', 'crazy']
    return lst
result = modify_it_maybe(mylst)
result[2] = 'awesome'
mylst[0] = 'wat'

val = 3
square = lambda x: x * x
def foo(fn, val):
    def doit():

return fn(val)
    return doit
f = foo(square, 4)
f()  # What is the return value?

DRAW DIAGRAM HERE

def f(add, sub):
    return add((lambda sub: sub(3, 5))(sub), 10)
f(sub, add)  # What is the return value?

DRAW DIAGRAM HERE

def hmm(n):
    return lambda x: x + y + n

def uhh(y):
    hmm_y = hmm(y)
    return hmm_y(2)

uhh(42)  # What is the return value?

DRAW DIAGRAM HERE