TODAY

- Review: PyGic
- Unification

DECLARATIVE PROGRAMMING

In declarative programming, we describe what the properties of the required solution are, and the computer discovers how to find the solution. Logic programming is a type of declarative programming that uses mathematical logic and logical inference to solve a problem.

REVIEW: PyGic

Suppose we asserted the following fact:
P>> fact doctor(<christopher, david, matt>)

What would the interpreter print in response to the following queries?
P>> doctor(?who)
P>> doctor(<?who>)
P>> doctor(<?ninth, ?tenth, ?eleventh>)
P>> doctor(<?ninth | ?rest>)
P>> doctor(<christopher, ?tenth | ?eleventh>)
**PyGIC: RULES**

P?\> rule grandfather(?person, ?grandson):
  ...
  father(?person, ?son)
  ...
  father(?son, ?grandson)

The conclusion is true only if the hypotheses are true.

Can variables be replaced with values such that the hypotheses are true? If so, the conclusion is true too.

---

**PyGIC: RULES FOR LISTS**

We can also define rules for lists.

For example, say we want to check if two (flat) lists are equal.

What are some facts we know about equal lists?

---

**PyGIC: RULES FOR LISTS**

Fact 1:
The empty list is only equal to itself.

P?\> fact equal_lists([], [])

A fact, by the way, is equivalent to a rule with True in the body:

P?\> rule equal_lists([], [],):
  ...
  True

---

**PyGIC: RULES FOR LISTS**

Fact 2:
Two lists are equal if their first elements are equal, and if the rest of their elements are equal.

P?\> rule equal_lists([?x | ?rest1], [?x | ?rest2]):
  ...
  equal_lists(?rest1, ?rest2)

---

**PyGIC: RULES FOR LISTS**

We want to append one list to another:

P?\> append([1, 2, 3], [4, 5], [1, 2, 3, 4, 5])

Yes.

P?\> append([1, 2, 3], [4, 5], ?, ?what)

Yes.

?what = [1, 2, 3, 4, 5]

---

**PyGIC: RULES FOR LISTS**

What are some facts we know about the problem?

Fact 1: Appending the empty list to any other list gives us the other list.

Fact 2: Appending one list to another is equivalent to adding the first element of the first list to the result of appending the second list to the rest of the first list.

What facts or rules should we then define?
PyGIC: Rules for Lists

We indicate that the first element of the first list and of the result must be the same.

We can now run append "backwards".

PyGIC: Rules for Lists (Practice)

Write the rule(s) reverse that will match only if the second list has elements in the reverse order as the first.

PyGIC: Rules for Lists (Practice)

Write the rule(s) palindrome that will match only if the list is a palindrome, where the list reads the same forwards and backwards.

PyGIC: Rules for Lists (Practice)
Announcements

• Homework 13 due **Saturday, August 4**.
  – Includes Py, streams, iterators, and generators
  – Also includes the Project 4 contest.
• Project 4 due **Tuesday, August 7**.
  – Partnered project, in two parts.
  – Twelve questions, so please start early!
  – Two extra credit questions.
• De-stress potluck **tonight from 7pm to 10pm** in the Wozniak Lounge (Soda, 4th floor).
  – Food and games.
  – Come and leave when you want.

Final

• Final is **Thursday, August 9**.
  – When? 6PM to 9PM.
  – How much? All of the material in the course, from June 18 to August 8, will be tested.
• Closed book and closed electronic devices.
• One 8.5" x 11" ‘cheat sheet’ allowed.
• No group portion.
• We have emailed you if you have conflicts and have told us.
  If you haven’t told us yet, please let us know by toda.
• Final review sessions on **Monday, August 6** and **Tuesday, August 7**, from 8pm to 9:30pm in the HP Auditorium (306 Soda).

How PyGic Works

Assume that we have asserted these facts:

P??> fact father(james, harry)
  Yes.

P??> fact father(harry, albus_severus)
  Yes.

P??> fact father(harry, james_sirius)
  Yes.

What happens in response to the query:

P??> father(?who, ?child)

PyGic: Rules for Lists (Practice)

P??> rule palindrome(?list):
  ... reverse(?list, ?list_rev)
  ... equal_lists(?list, ?list_rev)
HOW PyGic WORKS

PyGic picks a fact:
father(james, harry)
father(harry, albus_severus)
father(harry, james_sirius)

HOW PyGic WORKS

PyGic prepares an empty frame that extends the global frame.

It makes a new empty frame for every query.

HOW PyGic WORKS

PyGic attempts to unify the query with the fact.

Unification is a generalized form of pattern matching, where either or both of the patterns being matched may contain variables.

HOW PyGic WORKS: UNIFICATION

To match the query
father(?who, ?child)
with the fact
father(james, harry).
PyGic must check if

HOW PyGic WORKS: UNIFICATION

PyGic checks if the variables
?who or ?child
have any values in the current frame.

There are none!
So, PyGic binds the variables to these values in the current frame.

Now, trivially, we know that
?who = james, ?child = harry
is true.
HOW PyGic WORKS: UNIFICATION

PyGic is done with the query, since it successfully matched the query to a fact.

PyGic returns the frame and its bindings to be printed back to the user.

HOW PyGic WORKS: BACKTRACKING

What happens if the user asks for more?

PyGic returns to the last point at which it made a choice (a choice point), and ignores all the frames that it made as a result of that choice.

There, it tries to make another choice, if it can. If not, it goes to the choice point before that, and attempts to make another choice.

HOW PyGic WORKS: BACKTRACKING

In this example, it made a choice when it chose which fact to unify. As a result, a new frame is created with possibly new bindings.

If it cannot choose another fact or rule to unify, and if there are no more choice points, then there are no more ways to satisfy the rules.

This is known as chronological backtracking.

PyGic backtracks to the last point at which it made a choice and attempts to make another one to find another solution.

HOW PyGic WORKS

Now, say that we have the following rule:

\[ P \Rightarrow \text{rule grandfather(?who, ?grandson)} : \]
\[ \ldots \text{father(?who, ?son)} \]
\[ \ldots \text{father(?son, ?grandson)} \]

What happens in response to the query:

\[ P \Rightarrow \text{grandfather(james, ?grandson)} \]

PyGic first searches for the facts that match the query and the rules whose conclusions match the query.

There is only one such rule:

\[ \text{grandfather(?who, ?grandson)} \]

PyGic picks this rule.
HOW PyGic WORKS

PyGic will rename the variables to avoid confusion with other rules that may have the same variable names.

The rule is now:

\[
\text{grandfather}(\text{?who}#1, \text{?grandson}#2):
\text{father}(\text{?who}#1, \text{?son}#3)
\text{father}(\text{?son}#3, \text{?grandson}#2)
\]

HOW PyGic WORKS

PyGic prepares an empty frame, where no variables have yet been bound to any value.

HOW PyGic WORKS: UNIFICATION

To match the query

\[
\text{grandfather}(\text{james}, \text{?grandson})
\]

with the rule conclusion

\[
\text{grandfather}(\text{?who}#1, \text{?grandson}#2),
\]

PyGic must check if

\[
\text{?who}#1 = \text{james},
\text{?grandson}#2 = \text{?grandson}.
\]

HOW PyGic WORKS: HYPOTHESES

However, this is a rule!

PyGic needs to determine if the hypotheses are true to infer that the conclusion is true.

PyGic will consider each hypothesis as a new query, and determine if each hypothesis is true.

HOW PyGic WORKS: UNIFICATION

There are none!

So, PyGic makes the proper bindings in the current frame.

\[
\text{?who}#1 \rightarrow \text{james},
\text{?grandson}#2 \rightarrow \text{?grandson}
\]
HOW PyGic WORKS

The new query is
father(?who#1, ?son#3)

PyGic searches for facts and rule conclusions that match this query. There are three such facts:
father(james, harry)
father(harry, albus_severus)
father(harry, j James_sirius)

HOW PyGic WORKS

PyGic picks a fact:
father(james, harry)
father(harry, albus_severus)
father(harry, j James_sirius)

HOW PyGic WORKS

PyGic prepares an empty frame, which extends the previous frame.

HOW PyGic WORKS: UNIFICATION

To match the query
father(?who#1, ?son#3)
with the fact
father(james, harry),
PyGic must check if
?who#1 = james, ?son#3 = harry.

HOW PyGic WORKS: UNIFICATION

PyGic checks if the variables
?who#1 or ?son#3
have any values in the current frame or its parent.

HOW PyGic WORKS: UNIFICATION

?who#1 has a value, but that value matches james.
There are no bindings for ?son#3.

PyGic binds ?son#3 with harry.
The query has been successfully unified with a fact.
HOW PyGic WORKS

The first hypothesis in the body of the grandfather rule is true. Now, we check the second hypothesis:
father(?son#3, ?grandson#2)

PyGic searches for facts and rule conclusions that match this query. There are three such facts:
father(james, harry)
father(harry, albus_severus)
father(harry, james_sirius)

HOW PyGic WORKS

PyGic picks a fact:
father(james, harry)
father(harry, albus_severus)
father(harry, james_sirius)

HOW PyGic WORKS

PyGic prepares another empty frame, which extends the previous frame.

HOW PyGic WORKS: UNIFICATION

To match the query:
father(?son#3, ?grandson#2)
with the fact:
father(james, harry),
PyGic must check if?
?son#3 = james, ?grandson#2 = harry.

HOW PyGic WORKS: UNIFICATION

?son#3 has a value, which does not match james.
The query is not true, given the existing bindings.
HOW PyGic WORKS

PyGic then backtracks and picks another fact:
father(james, harry)
father(harry, albus_severus)
father(harry, james_sirius)

HOW PyGic WORKS

PyGic prepares another empty frame, which extends the previous frame.

Notice that the “previous frame” is the frame before the last choice point.

HOW PyGic WORKS: UNIFICATION

To match the query
father(?son#3, ?grandson#2)
with the fact
father(harry, albus_severus),
PyGic must check if
?son#3 = harry,
?grandson#2 = albus_severus.

HOW PyGic WORKS: UNIFICATION

PyGic checks if the variables
?son#3 or ?grandson#2
have any values in the current frame or its parents.

HOW PyGic WORKS: UNIFICATION

?son#3 has a value, but that value matches harry.
?grandson#2 has a value ?grandson.

PyGic binds ?grandson with albus_severus.
The query has been unified with the fact.

HOW PyGic WORKS

Both the hypotheses of the grandson rule are true, so the conclusion must also be true.

The values for the variables in the original query (?grandson) are looked up in the environment and printed.
HOW PYGIC WORKS: CODE (SIMPLIFIED)

To prove a query in the given environment and with a given rule database:

```python
def prove_query(query, env, ruledb):
    if is_true_expr(query):
        yield env
    else:
        matching_rules = ruledb.find_rules_matching(query)
        for rule in matching_rules:
            newenv = pygic.environments.Environment(env)
            if unify_expr_lists(query, rule.conclusion, newenv):
                yield result
```

Try to unify the query with the conclusion of the rule, which may extend or prune the frame.

If the hypotheses in the query can be proved, yield the environment that results from the proof.

For every rule that matches... extended or renamed rule.

Try to unify the query with the conclusion of the rule, which may extend or prune the frame.

If the hypotheses in the query can be proved, yield the environment that results from the proof.

HOW PYGIC WORKS: CODE (SIMPLIFIED)

```python
def prove_queries(queries, env, ruledb):
    if len(queries) == 0:
        yield env
    else:
        for new_env in prove_query(queries[0], env, ruledb):
            for result in prove_queries(queries[1:], new_env, ruledb):
                yield result
```

Prove the first query and obtain a resulting new environment.

Prove the rest of the queries in the new environment.

HOW PYGIC WORKS: CODE (SIMPLIFIED)

```python
def prove_query(query, env, ruledb):
    if is_true_expr(query):
        yield env
    else:
        matching_rules = ruledb.find_rules_matching(query)
        for rule in matching_rules:
            rule.rename()
            newenv = pygic.environments.Environment(env)
            if unify_expr_lists(query, rule.conclusion, newenv):
                yield result
```

For every rule that matches... extended or renamed rule.

Try to unify the query with the conclusion of the rule, which may extend or prune the frame.

If the hypotheses in the query can be proved, yield the environment that results from the proof.

For every rule that matches... extended or renamed rule.

Try to unify the query with the conclusion of the rule, which may extend or prune the frame.

If the hypotheses in the query can be proved, yield the environment that results from the proof.
APPLICATIONS

Declarative programming is useful in database applications.

For example, if we have a database of student records, and want to get all the records of sophomore year students, we run the query

```
SELECT * FROM STUDENT_DB WHERE YEAR = 2
```

APPLICATIONS

Notice that in the query

```
SELECT * FROM STUDENT_DB WHERE YEAR = 2
```

all that we have specified are the properties we expect from our output.

We could, of course, iterate through all the records and filter out the ones we need, but it is a common enough operation that it is better to specify what we want from the output, rather than how we want to get it.

CONCLUSION

- Under the hood, PyGic matches the query against all of its rules and facts. It then picks one, and attempts to unify the query with the fact (or rule conclusion) by finding a consistent assignment to the variables in either.
- Declarative programming is useful in situations where we know what we expect of the output.
- Preview: Write your own chat client.