Lecture 10: Linked Lists
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Announcements
• Project 2 is due 7/12 (+1 EC point if submitted 7/12)
  • Run ok --submit to check against hidden tests
  • Check your submission at ok.cs61a.org
  • Invite your partner (watch this video)
• Homework 4 is due 7/7
• Quiz 3 is tomorrow at the beginning of lecture
  • If you have an alternate time or are not enrolled in the class, please arrive at 11:45 am
• Quiz 4 will be released 9 am on 7/11, due 10 am on 7/12
• 61A Potluck on 7/8! 5 – 8 pm (or later) in Wozniak Lounge
  • Bring food and board games!

Roadmap
Introduction
Functions
Data
Mutability
Objects
Interpretation
Paradigms
Applications

Hog Contest
• 76 contestants
  • 20 new challengers on the last day
  • 11 new challengers in the last 6 hours
• The winner:
  1. Edgar Orendain
  2. Going Deep Blue
  3. The best team on the 3rd floor of Davidson (U2)
  4. Going DeepMind
Thank you to all the participants!
Full rankings: cs61a.org/proj/hog_contest

Data Abstraction
• Great programmers use data abstraction to separate:
  • How compound values are used (the unit)
  • How compound values are represented (the parts)
Abstraction Barrier Violations

- Constructors and selectors provide us with abstraction, allowing us to use the data type without having to know its implementation.
- An abstraction barrier violation is when we assume knowledge about the data type implementation, rather than using constructors and selectors.

Never violate the abstraction barrier!

Sequences

The Sequence Abstraction (demo)

The sequence abstraction is a collection of behaviors:

- **Length.** A sequence has a finite length.
- **Element selection.** A sequence has an element corresponding to any non-negative integer index less than its length, starting at 0.

Lists and strings are both examples of sequences.

We can use built-in syntax associated with this behavior. We can also use functions.

Linked Lists

- Another way to implement the sequence abstraction.
- Links have two parts:
  - `first`: the element in the link
  - `rest`: the next link in the list
- This is a recursive definition: the rest of a linked list is another linked list.
- This data structure has many names:
  - Linked list (C, Java)
  - List (Lisp)
  - Forward List (C++)
  - Linky Listys (TAs)

Linked List Abstraction

```python
def link(first, rest):
    """Construct a linked list from its first element and the rest of the linked list."""

def first(s):
    """Return the first element of a linked list S."""

def rest(s):
    """Return the rest of the elements of a linked list S."""
```

If a linked list `s` is constructed from a first element `h` and a linked list `t`, then:

- `first(s)` returns `h`, which is an element of the sequence.
- `rest(s)` returns `t`, which is a linked list.
Implementing Linked Lists (v1)  (demo)

```python
def link(first, rest):
    """Construct a linked list from its first element and the rest of the linked list."""
    return [first, rest]
def first(s):
    """Return the first element of a linked list S."""
    return s[0]
def rest(s):
    """Return the rest of the elements of a linked list S."""
    return s[1]
```

Linked Lists are Sequences  (demo)

```python
def len_link(s):
    """Return the length of the linked list."""
    length = 0
    while s != empty:
        a, length = rest(s), length + 1
    return length
def getitem_link(s, i):
    """Return the element at index i."""
    while i > 0:
        a, i = rest(s), i - 1
    return first(s)
```

Never violate the abstraction barrier!

Linked Lists are Recursive  (demo)

```python
def len_link(s):
    """Return the length of the linked list."""
    if s == empty:
        return 0
    else:
        return 1 + len_link(rest(s))
def getitem_link(s, i):
    """Return the element at index i."""
    if i == 0:
        return first(s)
    else:
        return getitem_link(rest(s), i - 1)
```

Never violate the abstraction barrier!

Sequences as Containers  (demo)

```python
def contains(s, elem):
    """Return whether ELEM is in the sequence S."
    >>> contains([1, 2, 3], 1)
    True
    >>> contains([1, 2, 3], 4)
    False
    >>> for x in s:
    ...     if x == elem:
    ...         return True
    ...     return False
```

Linked List Processing

Break!
**Linked Lists as Containers** (demo)

```python
def contains_link(s, elem):
    """Return whether ELEM is in the sequence S.
    >>> contains_link(link(1, link(2, link(3, empty))), 1)
    True
    >>> contains_link(link(1, link(2, link(3, empty))), 4)
    False
    """
    if s == empty:
        return False
    if first(s) == elem:
        return True
    else:
        return contains(rest(s), elem)
```

**Linked List Examples**

**Counting Partitions**

```python
def count_partitions(n, m):
    if n == 0:
        return 1
    elif n < 0:
        return 0
    elif m == 0:
        return 0
    else:
        with_m = count_partitions(n - m, m)
        without_m = count_partitions(n, m - 1)
        return with_m + without_m
```

**Enumerating Partitions** (demo)

```python
def partitions(n, m):
    if n == 0:
        return link(empty, empty)
    elif n < 0 or m == 0:
        return empty
    else:
        with_m = partitions(n - m, m)
        without_m = partitions(n, m - 1)
        add_m = lambda s: link(m, s)
        with_m = map_link(add_m, with_m)
        return extend(with_m, without_m)
```

**Other Linked List Implementations**

**Implementing Linked Lists (v1)**

```python
def link(first, rest):
    """Construct a linked list from its first element and the rest of the linked list."
    return (first, rest)
def first(s):
    """Return the first element of a linked list S."
    return s[0]
def rest(s):
    """Return the rest of the elements of a linked list S."
    return s[1]
```
def link(first, rest):
    def dispatch(msg):
        if msg == 'first':
            return first
        elif msg == 'rest':
            return rest
    return dispatch

def first(s):
    return s('first')

def rest(s):
    return s('rest')

Implementing Linked Lists (v2) (demo)

def link(first, rest):
    def dispatch(msg):
        if msg == 'first':
            return first
        elif msg == 'rest':
            return rest
    return dispatch

def first(s):
    return s('first')

def rest(s):
    return s('rest')

Implementing Linked Lists (v3)

def link(first, rest):
    def dispatch(msg):
        if msg == 'first':
            return first
        elif msg == 'rest':
            return rest
    return dispatch

def first(s):
    return s('first')

def rest(s):
    return s('rest')

Summary

• Linked lists are one implementation of the sequence abstraction
• Linked lists are composed of two parts:
  • first: the element in the link
  • rest: the next link in the list (may be empty)
• Data abstraction means that the implementation details of the first and rest selectors are unnecessary
• We can use functions to implement linked lists
  • We can use lists to implement dictionaries
  • Therefore, we can use functions to implement dictionaries