

1 Nonlocal

- 1.1 (a) Draw the environment diagram that results from running the code.

```
def what(a, b):  
    x = a  
    def ha(ha):  
        nonlocal x  
        x = ha * 2  
        return x  
    return b(ha(x), x)  
  
what(4, lambda x, y : x)
```

- (b) Write the simplest possible function that does the same thing as what for any input a, b.

- 1.2 Draw the environment diagram that results from running the code.

```
def camp(nile):  
    def ding(ding):  
        nonlocal nile  
        def nile(ring):  
            return ding  
        return nile(ding(1914)) + nile(1917)  
  
ring = camp(lambda nile: 103)
```

- 1.3 The ping-pong sequence counts up starting from 1 and is always either counting up or counting down.

At element k , the direction switches if k is a multiple of 7 or contains the digit 7.

The first 30 elements of the ping-pong sequence are listed below, with direction swaps marked using brackets at the 7th, 14th, 17th, 21st, 27th, and 28th elements.

1 2 3 4 5 6 [7] 6 5 4 3 2 1 [0] 1 2 [3] 2 1 0 [-1] 0 1 2 3 4 [5] [4] 5 6

Implement `make_pingpong_tracker` which returns the next value in the pingpong sequence each time it is called.

```
def has_seven(n):
    """Returns whether a number, n, contains the digit, 7."""
    if n % 10 == 7:
        return True
    elif n < 10:
        return False
    else:
        return has_seven(n // 10)
```

```
def make_pingpong_tracker():
    """
    >>> output = []
    >>> x = make_pingpong_tracker()
    >>> for _ in range(9):
    ... output += [x()]
    >>> output
    [1, 2, 3, 4, 5, 6, 7, 6, 5]
    """
```

```
index, current, add = 1, 0, True
```

```
def pingpong_tracker():
```

```
    -----

    if add:

        -----

    else:

        -----

    if -----:

        add = not add

    -----

    -----
```

```
return pingpong_tracker
```

2 Linked Lists & Trees, Yet Again?

2.1 Consider the following linked list function.

```
def prepend(s, item):
    return link(item, s)
```

- (a) What does this function do?
- (b) Assume s is initially length n , how long does it take to prepend once? prepend twice? prepend n times?

2.2 What does this function do?

```
def append(s, item):
    if s is empty:
        return link(item)
    else:
        return link(first(s), append(rest(s), item))
```

2.3 Say we want to repeatedly insert some numbers to the end of a linked list.

```
def append_many(s, items):
    for item in items:
        append(s, item)
```

- (a) Assuming s is initially length 1. How long will it take to complete the first insertion? The second? The n th?
- (b) Give the total runtime in $\Theta(\cdot)$ notation if s is initially empty and $items$ contains n items.

2.4 Consider the word_finder function below.

```
def word_finder(t, n, word):
    if root(t) == word:
        n -= 1
        if n == 0:
            return True
    for branch in branches(t):
        if word_finder(branch, n, word):
            return True
    return False
```

- (a) What does this function do?
- (b) If a tree has n total nodes, what is the total runtime for all searches in $\Theta(\cdot)$ notation?