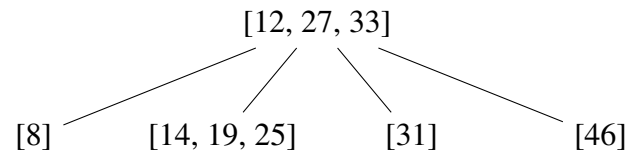
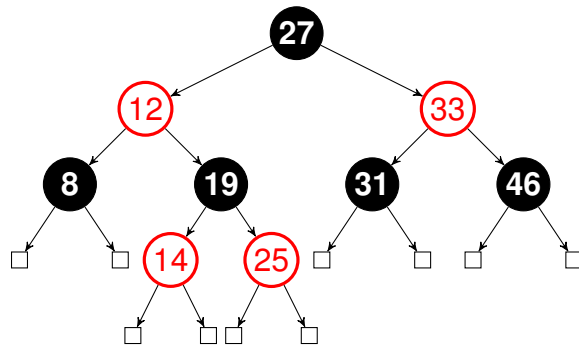
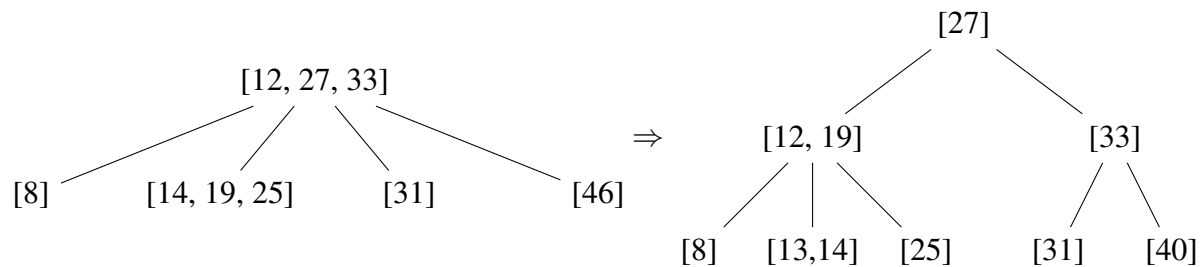


1 Balanced Search Trees

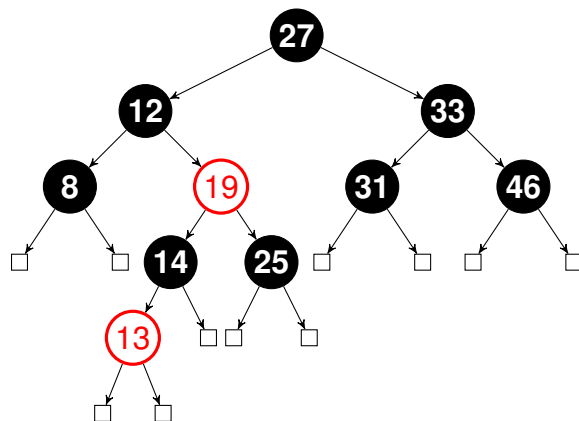
(a) Convert the red-black tree into a 2-4 tree.



(b) Insert 13 into the 2-4 tree.

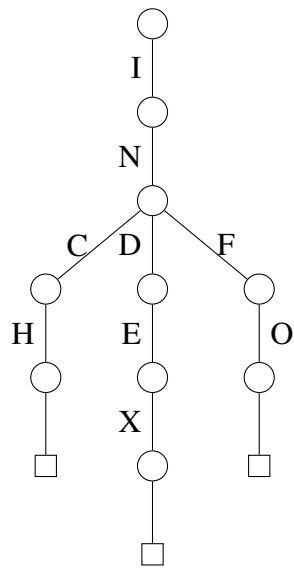


(c) Convert the resulting 2-4 tree into a valid red-black tree.

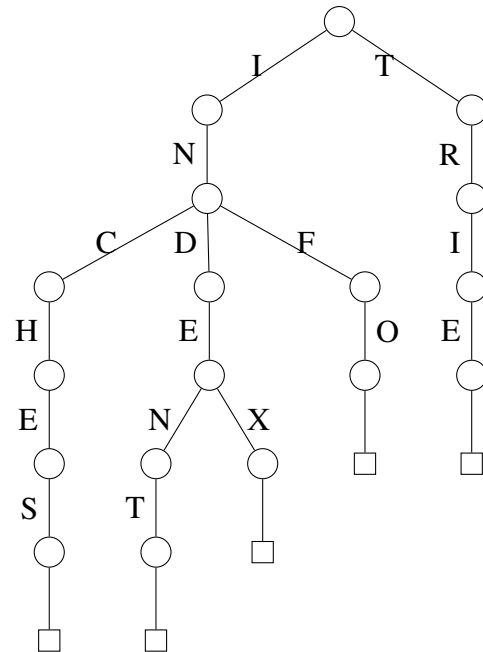


2 Tries

First, list the words encoded by the trie. Then draw the trie after inserting the words *indent*, *inches*, and *trie*. Ignore case.



Encoded words: index, info, inch



3 Runtime Analysis

- (a) Give the best and worst case runtimes for method *A* in $\Theta(\cdot)$.

```
public boolean A(int[] arr, int x) {  
    //Assume arr is sorted; N is arr.length  
    return A(arr, x, 0, arr.length-1);  
}  
  
public boolean A(int[] arr, int x, int low, int high) {  
    if (low > high) return false;  
    int mid = (low + high) / 2;  
    if (arr[mid] == x) return true;  
    return A(arr, x, low, mid-1) || A(arr, x, mid+1, high);  
}
```

This is almost binary search, except that both halves are recursed on.
Best case: $\Theta(1)$. Worst case: $\Theta(N)$.

- (b) Give the best and worst case runtimes for method *B* in $\Theta(\cdot)$.

```
public boolean B(int[] arr) {  
    //N is arr.length  
    int count = arr.length - 1;  
    while(count > 0) {  
        count = count - arr.length / 50;  
    }  
    return count;  
}
```

No matter how big the input array is, the loop will only execute about 50 times.
Best case: $\Theta(1)$. Worst case: $\Theta(1)$.