Recreation

What is the sum of the coefficients of

\[(1 - 3x + 3x^2)^{743}(1 + 3x - 3x^2)^{744}\]

after expanding and collecting terms?
CS61B Lecture #6: Arrays

• An array is a structured container whose components are
  - length, a fixed integer.
  - a sequence of length simple containers of the same type, numbered from 0.
  - (length field usually implicit in diagrams.)

• Arrays are anonymous, like other structured containers.

• Always referred to with pointers.

• For array pointed to by A,
  - Length is A.length
  - Numbered component \( i \) is \( A[i] \) (\( i \) is the index)
  - Important feature: index can be any integer expression.
int[] x, y, z;
String[] a;
x = new int[3];
y = x;
a = new String[3];
x[1] = 2;
y[1] = 3;
a[1] = "Hello";

int[] q;
q = new int[] { 1, 2, 3 };
// Short form for declarations:
int[] r = { 7, 8, 9 };
Example: Accumulate Values

Problem:  Sum up the elements of array $A$.

```java
static int sum(int[] A) {
    int N;
    N = 0;
    for (int i = 0; i < A.length; i += 1)
        N += A[i];
    return N;
}
```

// New (1.5) syntax
```
for (int x : A)
    N += x;
```

// For the hard-core: could have written

```java
int N, i;
for (i=0, N=0; i<A.length; N += A[i], i += 1)
    { }
// or just ;
```

// But please don’t: it’s obscure.

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Example: Insert into an Array

**Problem:** Want a call like `insert(A, 2, "gnu")` to convert (destructively)

```java
/** Insert X at location K in ARR, moving items K, K+1, ... to locations K+1, K+2, .... The last item in ARR is lost. */
static void insert(String[] arr, int k, String x) {
    for (int i = arr.length-1; i > k; i -= 1)  // Why backwards?
        arr[i] = arr[i-1];
    /* Alternative to this loop:
        System.arraycopy(arr, k, arr, k+1, arr.length-k-1);*/
    arr[k] = x;
}
```
(Aside) Java Shortcut

• **Useful tip:** Can write just 'arraycopy' by including at the top of the source file:

```java
import static java.lang.System.arraycopy;
```

• This means “define the simple name arraycopy to be the equivalent of java.lang.System.arraycopy in the current source file.”

• **Can do the same for** `out` **so that you can write**

```java
out.println(...);
```

  in place of

  ```java
  System.out.println(...);
  ```

• **Finally, a declaration like**

```java
import static java.lang.Math.*;
```

  means “take all the (public) static definitions in java.lang.Math and make them available in this source file by their simple names (the name after the last dot).”

• **Useful for functions like** `sin`, `sqrt`, etc.
Growing an Array

Problem: Suppose that we want to change the description above, so that \( A = \text{insert2} \ (A, \ 2, \ "gnu") \) does not shove “skunk” off the end, but instead “grows” the array.

A: bear
gazelle
hartebeest
skunk

A: bear
gazelle
gnu
hartebeest
skunk

/** Return array, r, where r.length = ARR.length+1; r[0..K-1]
* the same as ARR[0..K-1], r[k] = x, r[K+1..] same as ARR[K..]. */
static String[] insert2(String[] arr, int k, String x) {
    String[] result = new String[arr.length + 1];
    arraycopy(arr, 0, result, 0, k);
    arraycopy(arr, k, result, k+1, arr.length-k);
    result[k] = x;
    return result;
}

Why do we need a different return type from insert2??
Example: Merging

Problem: Given two sorted arrays of ints, A and B, produce their merge: a sorted array containing all items from A and B.

A: 0 2 3 6 9 11
B: 1 4 5 7 8

result: 0 1 2 3 4 5 6 7 8 9 11
Example: Merging Program

Problem: Given two sorted arrays of ints, A and B, produce their merge: a sorted array containing all from A and B.

Remark: In order to solve this recursively, it is useful to generalize the original function to allow merging portions of the arrays.

```java
/** Assuming A and B are sorted, returns their merge. */
public static int[] merge(int[] A, int[] B) {
    return mergeTo(A, 0, B, 0);
}

/** The merge of A[L0..] and B[L1..] assuming A and B sorted. */
static int[] mergeTo(int[] A, int L0, int[] B, int L1) {
    int N = A.length - L0 + B.length - L1;
    int[] C = new int[N];
    if (L0 >= A.length) arraycopy(B, L1, C, 0, N);
    else if (L1 >= B.length) arraycopy(A, L0, C, 0, N);
    else if (A[L0] <= B[L1]) {
        C[0] = A[L0];
        arraycopy(mergeTo(A, L0+1, B, L1), 0, C, 1, N-1);
    } else {
        C[0] = B[L1];
        arraycopy(mergeTo(A, L0, B, L1+1), 0, C, 1, N-1);
    }
    return C;
}
```

What is wrong with this implementation?
A Tail-Recursive Strategy

```java
public static int[] merge(int[] A, int[] B) {
    return mergeTo(A, 0, B, 0, new int[A.length+B.length], 0);
}

/** Merge A[L0..] and B[L1..] into C[K..], assuming A and B sorted. */
static int[] mergeTo(int[] A, int L0, int[] B, int L1, int[] C, int k){
    ...
}

This last method merges part of A with part of B into part of C. For example, consider a possible call `mergeTo(A, 3, B, 1, C, 2)`
```
A Tail-Recursive Solution

public static int[] merge(int[] A, int[] B) {
    return mergeTo(A, 0, B, 0, new int[A.length+B.length], 0);
}

/** Merge A[L0..] and B[L1..] into C[K..], assuming A and B sorted. */
static int[] mergeTo(int[] A, int L0, int[] B, int L1, int[] C, int k) {
    if (??) {
        return C;
    } else if (??) {
        C[k] = A[L0];
        return mergeTo(A, ??, B, ??, C, ??)
    } else {
        C[k] = B[L1];
        return mergeTo(A, ??, B, ??, C, ??)
    }
}
A Tail-Recursive Solution

```java
public static int[] merge(int[] A, int[] B) {
    return mergeTo(A, 0, B, 0, new int[A.length+B.length], 0);
}

/** Merge A[L0..] and B[L1..] into C[K..], assuming A and B sorted. */
static int[] mergeTo(int[] A, int L0, int[] B, int L1, int[] C, int k){
    if (L0 >= A.length && L1 >= B.length) {
        return C;
    } else if (??) {
        C[k] = A[L0];
        return mergeTo(A, ??, B, ??, C, ??)
    } else {
        C[k] = B[L1];
        return mergeTo(A, ??, B, ??, C, ??)
    }
}
```
A Tail-Recursive Solution

```java
public static int[] merge(int[] A, int[] B) {
    return mergeTo(A, 0, B, 0, new int[A.length+B.length], 0);
}

/** Merge A[L0..] and B[L1..] into C[K..], assuming A and B sorted. */
static int[] mergeTo(int[] A, int L0, int[] B, int L1, int[] C, int k) {
    if (L0 >= A.length && L1 >= B.length) {
        return C;
    } else if (L1 >= B.length || A[L0] <= B[L1]) {
        C[k] = A[L0];
        return mergeTo(A, ??, B, ??, C, ??)
    } else {
        C[k] = B[L1];
        return mergeTo(A, ??, B, ??, C, ??)
    }
}
```
public static int[] merge(int[] A, int[] B) {
    return mergeTo(A, 0, B, 0, new int[A.length+B.length], 0);
}

/** Merge A[L0..] and B[L1..] into C[K..], assuming A and B sorted. */
static int[] mergeTo(int[] A, int L0, int[] B, int L1, int[] C, int k)
{
    if (L0 >= A.length && L1 >= B.length)
    {
        return C;
    } else if (L1 >= B.length || A[L0] <= B[L1])
    {
        C[k] = A[L0];
        return mergeTo(A, L0 + 1, B, L1, C, k + 1);
    } else
    {
        C[k] = B[L1];
        return mergeTo(A, ??, B, ??, C, ??)
    }
}
public static int[] merge(int[] A, int[] B) {
    return mergeTo(A, 0, B, 0, new int[A.length+B.length], 0);
}

/** Merge A[L0..] and B[L1..] into C[K..], assuming A and B sorted. */
static int[] mergeTo(int[] A, int L0, int[] B, int L1, int[] C, int k){
    if (L0 >= A.length && L1 >= B.length) {
        return C;
    } else if (L1 >= B.length || A[L0] <= B[L1]) {
        C[k] = A[L0];
        return mergeTo(A, L0 + 1, B, L1, C, k + 1);
    } else {
        C[k] = B[L1];
        return mergeTo(A, L0, B, L1 + 1, C, k + 1);
    }
}
**Iterative Solution**

In general, we don't use either of the previous approaches in languages like C and Java. Array manipulation is most often iterative:

```java
public static int[] merge(int[] A, int[] B) {
    int[] C = new int[A.length + B.length];
    // mergeTo(A, 0, B, 0, C, 0)
    int L0, L1, k;
    L0 = L1 = k = 0;

    while (??) {
        if (L1 >= B.length || A[L0] <= B[L1]) {
            C[k] = A[L0];
            ??
        } else {
            C[k] = B[L1];
            ??
        }
    }
}
```
Iterative Solution

In general, we don't use either of the previous approaches in languages like C and Java. Array manipulation is most often iterative:

```java
public static int[] merge(int[] A, int[] B) {
    int[] C = new int[A.length + B.length];
    // mergeTo(A, 0, B, 0, C, 0)
    int L0, L1, k;
    L0 = L1 = k = 0;

    while (L0 < A.length || L1 < B.length) {
        if (L1 >= B.length || A[L0] <= B[L1]) {
            C[k] = A[L0];
            ??
        } else {
            C[k] = B[L1];
            ??
        }
    }
}
```
Iterative Solution

In general, we don't use either of the previous approaches in languages like C and Java. Array manipulation is most often iterative:

```java
public static int[] merge(int[] A, int[] B) {
    int[] C = new int[A.length + B.length];
    // mergeTo(A, 0, B, 0, C, 0)
    int L0, L1, k;
    L0 = L1 = k = 0;

    while (L0 < A.length || L1 < B.length) {
        if (L1 >= B.length || A[L0] <= B[L1]) {
            C[k] = A[L0];
            L0 += 1; k += 1;
        } else {
            C[k] = B[L1];
            L1 += 1; k += 1;
        }
    }
}
```
Iterative Solution II

The same, with a for loop:

```java
public static int[] merge(int[] A, int[] B) {
    int[] C = new int[A.length + B.length];
    int L0, L1;
    L0 = L1 = 0;
    for (int k = 0; k < C.length; k += 1) {
        if (L1 >= B.length || A[L0] <= B[L1]) {
            C[k] = A[L0]; L0 += 1;
        } else {
            C[k] = B[L1]; L1 += 1;
        }
    }
    return C;
}
```
Alternative Solution: Removing k

Claim: An invariant of the loop is that $k=L_0+L_1$.

```java
public static int[] merge(int[] A, int[] B) {
    int[] C = new int[A.length + B.length];
    int L0, L1;
    L0 = L1 = 0;
    while (L0 + L1 < C.length) {
        if {L1 >= B.length || A[L0] < B[L1]) {
            C[L0 + L1] = A[L0]; L0 += 1;
        } else {
            C[L0 + L1] = B[L1]; L1 += 1;
        }
    }
    return C;
}
```
Multidimensional Arrays

What about two- or higher-dimensional layouts, such as

\[
A = \begin{bmatrix}
2 & 3 & 4 & 5 \\
4 & 9 & 16 & 25 \\
8 & 27 & 64 & 125 \\
\end{bmatrix}
\]
Multidimensional Arrays in Java

These are not primitive in Java, but we can build them as arrays of arrays:

```java
int[][] A = new int[3][];
A[0] = new int[] {2, 3, 4, 5};
A[2] = new int[] {8, 27, 64, 125};
// or
int[][] A;
A = new int[][] {
    { 2, 3, 4, 5 },
    { 4, 9, 16, 25 },
    { 8, 27, 64, 125 }
};
// or
int[][] A = {
    { 2, 3, 4, 5 },
    { 4, 9, 16, 25 },
    { 8, 27, 64, 125 }
};
// or
int[][] A = new A[3][4];
for (int i = 0; i < 3; i += 1)
    for (int j = 0; j < 4; j += 1)
        A[i][j] = (int) Math.pow(j + 2, i + 1);
```
Exotic Multidimensional Arrays

- Since every element of an array is independent, there is no single "width" in general:

```java
int[][] A = new int[5][];
A[0] = new int[] {0, 1};
A[1] = new int[] {2, 3, 4, 5};
A[2] = new int[] {6, 7, 8};
```

- What does this print?

```java
int[][] ZERO = new int[3][];
    new int[] {0, 0, 0};
ZERO[0][1] = 1;
System.out.println(ZERO[2][1]);
```
Exotic Multidimensional Arrays

• Since every element of an array is independent, there is no single “width” in general:

```java
int[][] A = new int[5][];
A[0] = new int[] {};
A[1] = new int[] {0, 1};
A[3] = new int[] {6, 7, 8};
```

• What does this print?

```java
int[][] ZERO = new int[3][];
    new int[] {0, 0, 0};
ZERO[0][1] = 1;
System.out.println(ZERO[2][1]);
```