## 1 Javaian Rhapsody

Next to each line, write out what you think the code will do when it is run. Assume the Singer class exists and that the code below compiles.
Comments are above the line they describe.

```
/* Declare a variable of type String and assign it the value "no". In Java,
    all variables must be declared before they are used. */
String disagree = "no";
/* Declare a variable of type int and assign it the value 7. */
int }x=7
/* Declare a variable of type Singer and initialize it using the Singer
    constructor with the argument "Queen" */
Singer queen = new Singer("Queen");
/* Checks if x is greater than 0; if so, subtract l from x, then call queen's
    sing method with argument "no", then go back to the beginning of the loop.
    queen object sings "no" 7 times. */
while (x > 0) {
    x -= 1;
    queen.sing(disagree);
}
/* Declares a variable of type String array and initializes it to hold three
    Strings. */
String[] phrases = {"Oh", "mamma mia", "let me go"};
/* Prints "Oh" to standard output */
System.out.print(phrases[0]);
/* Declares variable i and initialize to 0 and checks if it is less than 3. If
    so, print "mamma mia", then add one to i, then go back to the beginning of
    the loop and re-check that i < 3. "mamma mia" is printed out 3 times. */
for (int i = 0; i < 3; i += 1) {
    System.out.print(" " + phrases[1]);
}
/* Prints "let me go" to standard output. */
System.out.print(" " + phrases[2]);
```


## 2 Mystery

Below is a function (or method) called mystery1. It takes an array of integers called inputArray and an integer $k$ as arguments and returns an integer.

```
public static int mysteryl(int[] inputArray, int k) {
    int x = inputArray[k];
```

```
    int answer = k;
    int index = k + 1;
    while (index < inputArray.length) {
        if (inputArray[index] < x) {
        x = inputArray[index];
        answer = index;
    }
    index = index + 1;
    }
    return answer;
}
```

Write the return value of mystery 1 if inputArray is the array $\{3,0,4,6,3\}$ and $k$ is 2 . Then, describe in English what mystery1 returns.
The mystery1 function returns 4. mystery1 returns the index of the smallest element that occurs at or after index $k$ in the array. If $k$ is greater than or equal to the length of the array or less than 0 , an ArrayIndexOutOfBoundsException will be thrown at runtime.
The variable x keeps track of the smallest element found so far and the variable answer keeps track of the index of this element. The variable index keeps track of the current position in the array. The while loop steps through the elements of the array starting from index $k+1$ and if the current element is less than $\mathrm{x}, \mathrm{x}$ and answer are updated.
Extra: Below is another function called mystery2. It takes an array of integers called inputArray as an argument and returns nothing.

```
public static void mystery2(int[] inputArray) {
    int index = 0;
    while (index < inputArray.length) {
        int targetIndex = mysteryl(inputArray, index);
        int temp = inputArray[targetIndex];
        inputArray[targetIndex] = inputArray[index];
        inputArray[index] = temp;
        index = index + 1;
    }
}
```

Write what mystery 2 will do if inputArray is the array $\{3,0,4,6,3\}$. Then, describe in English what mystery 2 does.
mystery 2 doesn't return anything because its return type is void.
If mystery 2 is called on the array $\{3,0,4,6,3\}$, then after the method runs, the array will be $\{0$, $3,3,4,6\}$. Given any array, the method mystery2 sorts the elements of the array in increasing order.

At the beginning of each iteration of the while loop, the first index elements of the array are in sorted order. Then the method mystery1 is called to find the index of the smallest element of the array occurring at or after index. The element at the index returned by mystery 1 is then swapped with the element at position index so that the first index +1 elements of the array are in sorted order.

## 3 Fibonacci

Implement fib1 recursively. fib1 takes in an integer $N$ and returns an integer representing the Nth Fibonacci number. The Fibonacci sequence is $0,1,1,2,3,5,8,13,21, \ldots$, where 0 is the 0th Fibonacci number.

```
public static int fibl(int N) {
    if (N <= 1) {
        return N;
    } else {
        return fibl(N - 1) + fibl(N - 2);
    }
}
```

Extra: Implement fib2 in 5 lines or fewer that avoids redundant computation. fib2 takes in an integer N and helper arguments $\mathrm{k}, \mathrm{f} 0$, and $f 1$ and returns an integer representing the Nth Fibonacci number. If you're stuck, try implementing fib1 iteratively and then see how you can transform your iterative approach to implement fib2.

```
public static int fib2(int N, int k, int f0, int f1) {
    if (N == k) {
        return f0;
    } else {
        return fib2(N, k + 1, f1, f0 + f1);
    }
}
To compute the \(N\) th fibonacci number using fib2, call \(\ddagger i b 2(N, 0,0,1)\).
```

