1 Law and Order

Write the DFS pre-order, DFS in-order, DFS post-order, and BFS traversals of the following binary search tree. For all traversals, process child nodes left to right.

```
    10
   / \
  3   12
 / \ / \
1  7 13 15
```

2 Is This a BST?

(a) The following code should check if a given binary tree is a BST. However, for some trees, it is returning the wrong answer. Give an example of a binary tree for which the method fails.

```
public static boolean brokenIsBST(TreeNode T) {
    if (T == null) {
        return true;
    } else if (T.left != null && T.left.val > T.val) {
        return false;
    } else if (T.right != null && T.right.val < T.val) {
        return false;
    } else {
        return brokenIsBST(T.left) && brokenIsBST(T.right);
    }
}
```

(b) Now, write `isBST` that fixes the error encountered in part (a).

*Hint:* You will find `Integer.MIN_VALUE` and `Integer.MAX_VALUE` helpful.

```
public static boolean isBST(TreeNode T) {
    return isBSTHelper();
}
```

```
public static boolean isBSTHelper() {
    }
```
3 Sum Paths

Define a root-to-leaf path as a sequence of nodes from the root of a tree to one of its leaves. Write a method `printSumPaths(TreeNode T, int k)` that prints out all root-to-leaf paths whose values sum to `k`. For example, if `T` is the binary tree in the diagram below and `k` is 13, then the program will print out 10 2 1 on one line and 10 4 -1 on another.

```
  10
  /  \
 2   4
  /  \
 5   1  -1
```

(a) Provide your solution by filling in the code below:

```java
public static void printSumPaths(TreeNode T, int k) {
    if (T != null) {
        sumPaths( );
    }
}

public static void sumPaths(TreeNode T, int k, String path) {
    // your code here
}
```

(b) What is the worst case running time of the `printSumPaths` in terms of `N`, the number of nodes in the tree? What is the worst case running time in terms of `h`, the height of the tree?