CS61B Lecture #24

Administrative:
- Midterm graded:
  - Intended average: 20
  - Actual average: 21.2
  - Actual median: 20.5

Today:
- Priority queues (Data Structures §6.4, §6.5)
- Range queries (§6.2)
- Java utilities: SortedSet, Map, etc.

Next topic: Hashing (Data Structures Chapter 7).

Priority Queues, Heaps
- Priority queue: defined by operations “add,” “find largest,” “remove largest.”
- Examples: scheduling long streams of actions to occur at various future times.
- Also useful for sorting (keep removing largest).
- Heap is common implementation.
- Enforces heap property: all labels in both children of node are less (or greater) than node’s label.
- So node at top has largest (or smallest) label.
- Are free to add smaller value to less bushy subtree, thus maintaining bushiness (keeping tree balanced).
- Insertion and deletion always proportional to \( \lg N \) in worst case.

Example: Inserting into a simple heap

Data:
1 17 4 5 9 0 -1 20

Initial Heap:

```
  20
 /   \
17    9
 /     \
5      4
 \      \n 0     -1
```

Add 8: Dashed boxes show where heap property violated

```
  20
 /   \
17    9
 /     \
5      4
 \      \n 0     -1
```

Heap insertion continued

Now insert 18:

```
  20
 /   \
17    9
 /     \
8      4
 \      \n1      5
```

```
  20
 /   \
17    9
 /     \
8      4
 \      \n1      5
```

⇒

```
  20
 /   \
18    9
 /     \
8      4
 /     \
1      5
```

⇒

```
  20
 /   \
18    9
 /     \
8      4
 /     \
1      5
```
Removing Largest from Heap

To remove largest: Move bottommost, rightmost node to top, then re-heapify down as needed (swap offending node with larger child) to re-establish heap property.

Heaps in Arrays

• Since heaps are complete (missing items only at bottom level), can use arrays for compact representation.

• Example of removal from last slide (dashed arrows show children):

Ranges

• So far, have looked for specific items

• But for BSTs, need an ordering anyway, and can also support looking for ranges of values.

• Example: perform some action on all values in a BST that are within some range (in natural order):

  /** Apply WHATTODO to all labels in T that are
   * >= L and < U, in ascending natural order. */
  static void visitRange (BST T, Comparable<Key> L, Comparable<Key> U, 
                       Action whatToDo)
  if (T != null) {
    int compLeft = L.compareTo (T.label ()),
        compRight = U.compareTo (T.label ());
    if (compLeft < 0) /* L < label */
      visitRange (T.left (), L, U, whatToDo);
    if (compLeft <= 0 && compRight > 0) /* L <= label < U */
      whatToDo.action (T);
    if (compRight > 0) /* label <= U */
      visitRange (T.right (), L, U, whatToDo);
  }

Time for Range Queries

• Time for range query ∈ O(h + M), where h is height of tree, and M is number of data items that turn out to be in the range.

• Consider searching the tree below for all values, x, such that 25 ≤ x < 40.

• In this example, the h comes from the starred nodes; the M comes from other non-dashed nodes. Dashed nodes are never looked at.
Ordered Sets and Range Queries in Java

- **Class** SortedSet supports range queries with views of set:
  - `S.headSet(U)`: subset of `S` that is `< U`.
  - `S.tailSet(L)`: subset that is `≥ L`.
  - `S.subSet(L,U)`: subset that is `≥ L`, `< U`.

- Changes to views modify `S`.
- Attempts to, e.g., add to a headSet beyond `U` are disallowed.
- Can iterate through a view to process a range:
  ```java
  SortedSet<String> fauna = new TreeSet<String>(Arrays.asList("axolotl", "elk", "dog", "hartebeest", "duck"));
  for (String item : fauna.subSet("bison", "gnu"))
    System.out.printf("%s, ", item);
  ```
  would print "dog, duck, elk,"

- Java library type TreeSet<T> requires either that `T` be Comparable, or that you provide a Comparator:
  ```java
  SortedSet<String> rev_fauna = new TreeSet<String>(Collections.reverseOrder());
  ```

Example of Representation: BSTSet

- Use binary search tree to represent set. Can use same representation for both BSTSet and its subsets.
- Each set has pointer to BST, plus bounds (if any).
- In this representation, size is rather expensive!

```java
SortedSet<String> fauna = new BSTSet<String>(collection of stuff);
subset = fauna.subSet("bison","gnu");
Iterator<String> i = subset.iterator();
```