

### "What's with all these 1s and 0s?"

1david180lb65haaks to David Jacobs) 1111 1111 1111 1111

































#### **Boolean Equations**

#### **Truth Tables**

- Explicit declaration of a Boolean function for all values of inputs
- Can use to derive a more compact analytical equation
   Sum of Products:
  - Find all rows in which output is a 1
  - Each row will be a term that is ORed with all other row terms
  - For each row term, Input bit i is negated if it is a o in that row, otherwise it appears as normal

	Truth Table to Expression										
	Induit table to Expression										
1	A	B	<u>c</u>	E	i) Find all rows that have a "i" in						
	0	0	0	0	the output						
	0	0	1	1							
	0	1	0	0	2) Incorporate these rows into a						
	0	1	1	1	boolean equation, replacing the						
	1	0	0	1	column heading with its						
	1	0	1	1	negation if the row has a o in						
	1	1	0	1	that cell						
	1	1	1	1							
	First Row: A'B'C				The Whole Equation: A'B'C + A'BC + AB'C + AB'C + ABC' + ABC						

## Question S1 • How many gates are there for a Boolean function of m inputs and n outputs?



#### **Boolean Equation Minimization**

- That equation we just got was gross
  (A'B'C + A'BC + AB'C' + AB'C + ABC' + ABC)
- There's probably a better way to representUse Laws of Boolean Algebra
- Also
  - Can help to verify if two functions are the same (they'll minimize to the same thing)
  - Reduces complexity of hardware (most of the time, there are several factors to this...)

#### Laws of Boolean Algebra

$x \cdot \overline{x} = 0$	$x + \overline{x} = 1$	complementarity
$x \cdot 0 = 0$	x + 1 = 1	laws of 0's and 1's
$x \cdot 1 = x$	x + 0 = x	identities
$x \cdot x = x$	x + x = x	idempotent law
$x \cdot y = y \cdot x$	x + y = y + x	commutativity
(xy)z = x(yz)	(x+y) + z = x + (y+z)	associativity
x(y+z) = xy + xz	x + yz = (x + y)(x + z)	distribution
xy + x = x	(x+y)x = x	uniting theorem
$\overline{x \cdot y} = \overline{x} + \overline{y}$	$\overline{(x+y)} = \overline{x} \cdot \overline{y}$	DeMorgan's Law
		-



































Soo o -> 11 Soo (0/3) # Had two os, another one means we stay here and output #Zl(000)=3Soo 1 -> 10 Soo (1/2) # This is our first 1 in a while, register we've seen a 1 by

# setting I(-i) to I(-i) (i.e., So) and output #ZI(oo)=2 So I(-i) So I(-i) (i.e., So) and output #ZI(oo)=2 So I(-i) (i.e., So) and output #ZI(oo)=2 So I(-i) (i.e., So) and output #ZI(oo)=2 So I(-i) (i.e., So) and output #ZI(oo)=2

S10 0 -> 10 S00 (0/2) # Saw a 1 2 timesteps ago, nothing since. Goto S00,output #ZI(100)=2

 $\begin{array}{l} Sio 1 - > o \ Sio \ (1/i) \ \# \ Saw a \ 1 \ 2 \ timesteps \ ago, a \ 1 \ now. \ Goto \ oi, \ output \ \# ZI(10)=1 \\ Sin \ o - > oi \ Sio \ (o/1) \ \# \ Saw \ 2 \ straight \ is, \ now \ a \ o. \ Goto \ Sio, \ output \ \# ZI(10)=1 \\ \end{array}$ S11 -> 00 S1 (1/0) # Everything is coming up 1s! Stay here (in S11), output #ZI(m)=0





















#### Truth Table

Decode1	Decode2	PS2	PS1	PS0	NS2	NS1	NS0	Open	Error
0	х	0	0	0	1	0	1	0	0
1	х	0	0	0	0	0	1	0	0
х	0	0	0	1	1	1	0	0	0
Х	1	0	0	1	0	1	0	0	0
х	х	0	1	0	0	1	1	1	0
х	х	0	1	1	1	0	0	0	0
х	х	1	0	0	0	1	0	0	0
х	х	1	0	1	1	1	0	0	0
х	х	1	1	0	1	1	0	0	1
х	x	1	1	1	х	х	x	x	х

Enter is a necessary condition for all state transitions Reset will always cause NS to be Init

























Step 5 – Set Control Lines							
Control	Value	Control	Value				
nPC_sel	normal	ExtOp	Sign				
RegDst	Х	MemWr	1				
RegWrite	0	MemToReg	Х				
ALUCtrl	Х	MemDataSrc	1				
ALUSrc	Х	MemAddrSrc	1				
•	Spring 2007 CS6rC Final Re Nguyen, Valerie Ishida, Bria	n Zimmer	8:				











# <section-header><section-header><text><text><text><text>









Infamous Exam	nple	
• addi \$1, \$0, 2	• 1	
<ul> <li>loop: add \$0, \$0, \$0</li> </ul>	• 2,10	
• beq \$1, \$0, done	• 3, 11	
• add \$4, \$3, \$2	• 4, 12	
• add \$5, \$4, \$3	• 5	
• add \$6, \$5, \$4	• 6	
• addi \$1, \$1, -1	• 7	
<ul> <li>beq \$0, \$0, loop</li> </ul>	• 8	
• addi \$1, \$1, -1	• 9	
<ul> <li>done: beq \$0, \$0, exit</li> </ul>	• 13	
• addi \$1, \$0, 3	• 14	
• exit: addi \$1, \$0, 1	<ul> <li>15, 16, 17, 18, 19</li> </ul>	
Spring 2007 CS61C Fina Nguyen, Valerie Ishida,	l Review, David Poll, Brian Brian Zimmer	94









More Pipelining Practice	
• 111	
• 123456789012	
• [1] F D A M R	
• [2] F D A M R	
• [3] F D A M R	
• [4] F D A M R	
• [5] FDAMR	
• [6]     F D A M R	
• [7] F D A M R Spring 2007 Covering to Covering Brian Narven, Valerie Mada Branzimmer	99

## What else? (Caches/VM) Brian Nguyen (Thanks to David Poll)









 What else? (Final

 Dotpourpi)

 Walerie Ishida (Thanks to David Poll)











Conclusion

Questions on the Fa-05 Final?

ring 2007 CS61C Final Review, David Poll, Brian uven. Valerie Ishida. Brian Zimmer