











<b>Representation of Fraction</b>	s with Fixed Pt.		
What about addition and multiplication?			
Addition is straightforward: $\begin{array}{c} 01.100 & 1.5_{10} \\ + & 00.100 & 0.5_{10} \\ 10.000 & 2.0_{10} \end{array}$	01.100 1.5 <sub>10</sub> 00.100 0.5 <sub>10</sub>		
Multiplication a bit more complex:	00 000 000 00 0110 0 0000 0000 0110000		
Where's the answer, 0.11? (need to reme	ember where point is) Garcia, Spring 2014 © UCB		





















Representation for 0	
Represent 0?	
exponent all zeroes	
<ul> <li>significand all zeroes</li> </ul>	
What about sign? Both cases valid	ι.
+0: 0 0000000 0000000000000000000000000	00000
-0: 1 0000000 00000000000000000000000000	00000
Cal	
Cost C Lto Proxing Point (16)	Garcia, spring 2014 © UCB

Exponent	Significand	Object
0	0	0
0	nonzero	???
1-254	anything	+/- fl. pt. #
255	0	+/- ∞
255	nonzero	???





























## Rounding

Cal ...

- When we perform math on real numbers, we have to worry about rounding to fit the result in the significant field.
  The FP hardware carries two extra bits of precision, and then round to get the proper value
- Rounding also occurs when converting: double to a single precision value, or

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floating point number to an integer

IEEE FP Rounding Modes
Examples in decimal (but, of course, IEEE754 in binary)
Round towards + ∞

ALWAYS round "up"; 2.001 ÷ 3, -2.001 ÷ -2

Round towards - ∞

ALWAYS round "down": 1.999 ÷ 1, -1.999 ÷ -2

Journate

Journate
Journation (default mode). Midway? Round to even
Normal rounding, almost: 2.4 ÷ 2, 2.6 ÷ 3, 2.5 ÷ 4
Round like you learned in grade school (nearest int)
Except if the value is right on the borderline, in which case wound to the nearest EVEN number
Ensures fairness on calculation
This way, half the time we round up on tie, the other half time wound both meads to balance out inaccuracies

<ul> <li>More difficult the second secon</li></ul>	han with integers
<ul> <li>Can't just add s</li> </ul>	significands
• How do we do	it?
De-normalize 1	to match exponents
<ul> <li>Add significan</li> </ul>	ids to get resulting one
<ul> <li>Keep the same</li> </ul>	e exponent
Normalize (pos	ssibly changing exponent)
<ul> <li>Note: If signs d subtract instea</li> </ul>	liffer, just perform a d.



















Peer Instruction	
1 1000 0001 111 0000 0000 0000	0000 0000
What is the decimal equivalent	a) -7 * 2^129 b) -3.5 c) -3.75
of the hoating pt # above:	d) -7 e) -7.5
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F	Peer Instruction		
			ABC
1.	produces same float number	1:	FFF
		2:	FFT
2.	same int number	4:	FTT
		5:	TFF
3.	FP add is associative:	6:	TFT
Cal	(x+y)+z = x+(y+z)	8:	TTT
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Peer Ins	struction	
		4
• Let ± (1	(,2) = # of floats between	1 and 2
• Let f (2	2,3) = # of floats between	2 and 3
	1: $f(1,2) < f(2,3)$ 2: $f(1,2) = f(2,3)$	
	3: $f(1,2) > f(2,3)$	
CSSIC L15 Floatik	ig Point I (50)	Garcia, Spring 2014 © UC