Instructions

- This booklet contains 8 pages including this cover page. The back of each page is blank and can be used for scratch work, but will not be graded (i.e. not even scanned into Gradescope).
- Please turn off all cell phones, smartwatches, and other mobile devices. Remove all hats, headphones, and watches. Place everything except your writing utensil(s), cheat sheet, and beverage underneath your seat.
- You have 80 minutes to complete this exam. The exam is closed book: no computers, tablets, cell phones, wearable devices, or calculators. You are allowed one page (US Letter, double-sided) of handwritten notes.
- There may be partial credit for incomplete answers; write as much of the solution as you can.
- Please write your answers within the boxes and blanks provided within each problem!

<table>
<thead>
<tr>
<th>Question</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>Possible Points</td>
<td>15</td>
<td>12</td>
<td>19</td>
<td>16</td>
<td>12</td>
<td>9</td>
<td>83</td>
</tr>
</tbody>
</table>

If you have the time, feel free to doodle on this front page!
**Question 1: Number Representation (15 pts)**

**a) Complete the tables below: (6 pts)**

<table>
<thead>
<tr>
<th>Base 8</th>
<th>Hexadecimal</th>
<th>Convert unsigned integers: (4 pts)</th>
<th>Convert to and from IEC prefixes: (2 pts)</th>
</tr>
</thead>
<tbody>
<tr>
<td>115(_8)</td>
<td>0x4D</td>
<td></td>
<td>2(^{54}) bits</td>
</tr>
<tr>
<td>32(_8)</td>
<td>0x1A</td>
<td></td>
<td>16 Pebi-bits</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Standard</th>
<th>IEC Prefixes</th>
</tr>
</thead>
<tbody>
<tr>
<td>2048 students</td>
<td>2 Kibi students</td>
</tr>
</tbody>
</table>

**b) Due to limitations in storage space, we are using only 4 bits to represent integers.**

1) What is the *most negative* 2’s complement signed integer (decimal) we can represent? (1 pt)

\[-2^{n-1} = -2^3 = -8\]

2) What is the value (decimal) of the 2’s complement number 0b1010? (1 pt)

\[-6\]

3) Write a number (binary) that, when added to 0b0100, will cause signed overflow. (2 pts)

0b0100 > ANS > 0b0111

**c) An amino acid is defined by a set of 3 consecutive nucleotides (A, C, G, or T). For example, ATG is Methionine. All combinations are unique (e.g. ATG ≠ AGT ≠ GTA).**

1) How many total possible amino acids are there? (1 pt)

\[4^3 = 64\] amino acids

2) In reality, there are 21 amino acids found in the human body. How many bits would it take to encode these amino acids in binary? (1 pt)

\[\text{ceil}(\log_2(21)) = 5\] bits

3) Scientists also use single-digit encodings for amino acids (e.g. ‘A’ for Alanine). In a single sentence, explain why it is okay that we use A for the amino acid Alanine, the nucleotide adanine, and the hex representation of the decimal number 10. (1 pt)

They are different representation systems. We need to know the appropriate interpretation to distinguish the values for our application.

4) We wish to encode the 21 amino acids in base 2, 3, or 5. Which of these choices allows for the MOST new amino acids discoveries before needing to increase the number of digits and how many new discoveries are allowed in this choice? (2 pts)

Base: 2  Possible New Discoveries: 32 – 21 = 11
Question 2: C Potpourri (12 pts)

a) Given the library function `rand()` that returns a random number between 0 and \((2^{32})-1\) when called, write a valid C expression that uses bit operations (`^`, `~`, `|`, `&`) to initialize the variable `r` with a random integer between 0 and `n`, which is some power of 2 less than \((2^{32})-1\). (3 pts)

```c
int n = 8; // In this case, we want r to contain one of \{0,1,2,3,4,5,6,7\}.
int r = rand() & (n - 1);
```

b) Sally Stanfurd tells you that using a random number generator function is silly in C. She claims that since local variables are not automatically initialized we can use the garbage contained in them as random values. Does Sally’s function produce truly random values (circle one)? **Yes // No** (2 pts)

*Briefly explain why or why not.*

The garbage contained in local variables is not truly random and is somewhat predictable given knowledge of prior functions and their associated stack frames.

c) Complete the implementation of the integer array shuffle function below, which randomizes the ordering of the first `n` entries of a given integer array. Each of the first `n` entries in the array should be swapped with an earlier entry exactly once, and the rest of the array should be left unchanged. Assume you have access to a function `random(int r)` that returns a number between 0 and `r-1`, inclusive. (5 pts)

```c
void shuffle(int* array, int n) {
    for (int i = n - 1; i > 0; i--)
    {
        int newIndex = random(i);
        int temp = array[newIndex];
        *(array + newIndex) = array[i];
        array[i] = temp;
    }
}
```

d) Assume integers are 32 bits. Instead of passing in an integer array as expected, we decide to pass in a string to our shuffle function as shown: (2 pts)

```c
char str[] = "fee fie foh fum ";
shuffle((int*) str, strlen(str)/sizeof(int));
printf("shuffle result: %s",str);
```

From the following choices, circle ONE of the following if it is a possible result of the `printf` statement:

- **Runtime Error** (e.g. seg fault)
- **Compiler Error** (e.g. incompatible pointer types)

```
Runtime Error (e.g. seg fault)  "fum foh fee fie "
Compiler Error (e.g. incompatible pointer types)  "ioe h ef uf fmeif"
```
**Question 3: C Structs and Memory (19 pts)**

A sparse matrix is a matrix in which most of the elements are zero. For matrices of $M$ rows and $N$ columns, instead of storing all $M \times N$ entries in an array, we can save memory for large matrices by instead only storing the nonzero entries in linked lists. Here we store an array of pointers to linked lists (row_ptrs), one entry for each row of the matrix. Each linked list node will contain (1) the column number, (2) the nonzero integer entry, and (3) a pointer to the next node. Each linked list will be *unsorted*. Both rows and columns are zero-indexed.

For example, the diagram below corresponds to the matrix

\[
\begin{bmatrix}
0 & 0 & 1 & 0 \\
-4 & 0 & 5 & 0 \\
0 & 0 & 0 & 0
\end{bmatrix}
\]

where $M = 3$ and $N = 4$:

The struct definition for the nodes is given below on the left. On the right are the declarations for both matrix representations: the usual (array) and our new (sparse) designs.

```c
struct node {
    int col;
    int num;
    struct node *next;
};
```

Array Matrix Storage

```c```
```c
int array[];
```

Sparse Matrix Storage

```c```
```c
struct node **row_ptrs;
```

a) If we have a matrix with $M = 8$, $N = 10$, and 4 nonzero entries, how much memory (in bytes) would each of the following use? Here an integer is 4 bytes and a pointer is 8 bytes. *(3.5 pts)*

<table>
<thead>
<tr>
<th>Array Matrix Storage</th>
<th>Sparse Matrix Storage</th>
</tr>
</thead>
<tbody>
<tr>
<td>array: $M \times N \times \text{sizeof(int)} = 320 \text{ B}$</td>
<td><em>row_ptrs</em>: $M \times \text{sizeof(void *)} = 64 \text{ B}$</td>
</tr>
<tr>
<td></td>
<td>struct node*: $4 \times \text{sizeof(struct node)} = 64 \text{ B}$</td>
</tr>
</tbody>
</table>

b) Complete the following function makeNode(), which creates a new struct node for use in other functions and initializes the col and num fields to the provided arguments. You can ignore running out of memory and you may not need all lines. *(5 pts)*

```c```
```c```
```c
```
c) Complete the following function `setNum()`, which sets a nonzero value in our sparse matrix structure. If `(row, col)` already had a nonzero value, then overwrite the existing value, otherwise add a new `struct node` at the end of the linked list to hold the value.

You should use `makeNode(int column, int integer)` to create any new nodes. You may not need all lines or declared variables. (10.5 pts)

```c
void setNum(struct node **row_ptrs, int row, int col, int num) {
    struct node *prev, *curr; /* short for previous and current */
    curr = row_ptrs[row]; // 1 pt

    /* insert at front of row */
    if (!curr) { // 0.5 pt
        row_ptrs[row] = makeNode(col, num); // 2 pts
        return;
    }

    /* traverse linked list */
    while (!curr) { // 0.5 pt
        if (curr->col == col) { // 1 pt
            curr->num = num; // 1 pt
            return; // 0.5 pt
        }

        prev = curr; // 1 pt
        curr = curr->next; // 1 pt
    }

    /* add to end of list */
    prev->next = makeNode(col, num); // 2 pts
    return;
}
```
Question 4: MIPS Procedures (16 pts)

We wish to write the function `toLowerCase`, which converts a string of letters to lowercase. `toLowerCase` takes in a char pointer, leaves spaces as spaces (assume only letters and spaces), and returns the number of converted characters (including spaces but not including the null terminator). Example: if `strcpy(p,"TeST oNe")`, then `toLowerCase(p)` returns 8 and `*p` now contains “test one”.

a) Complete the table below: (1 pt)

<table>
<thead>
<tr>
<th></th>
<th>‘a’</th>
<th>‘z’</th>
<th>‘A’</th>
<th>‘Z’</th>
<th>Space</th>
</tr>
</thead>
<tbody>
<tr>
<td>Decimal</td>
<td>97</td>
<td>122</td>
<td>65</td>
<td>90</td>
<td>32</td>
</tr>
<tr>
<td>Binary</td>
<td>0b 0110 0001</td>
<td>0b 0111 1010</td>
<td>0b 0100 0001</td>
<td>0b 0101 1010</td>
<td>0b 0010 0000</td>
</tr>
</tbody>
</table>

b) Based on the information above, fill in the C function prototype below and then write out the C assignment that performs the lowercase conversion using bit manipulation on a given variable `char c`: (3 pts)

Function prototype: `int toLowerCase(char* p);`

Lowercase conversion: `c = c | 0x20;`

c) Fill in the recursive MIPS implementation of `toLowerCase` below, following proper MIPS calling conventions. Write labels to the left of the provided lines. You may not need all lines provided. You will be deducted points for using extraneous lines. (12 pts – 9 for function, 3 for calling conventions)

```
toLower:
    addiu $sp, $sp, -4 # prologue
    sw $ra, 0($sp)

                                    # read char using $a0 (1.5 pt)
    lbu $t0, 0($a0)
    bne $t0, $zero, lower           # check for null terminator (1 pt)
    addu $v0, $0, $0                # base case (1 pt)
    j   return

lower:  ori $t0, $t0, 0x20         # recursive case; to lowercase (1.5 pt)
    sb $t0, 0($a0)                  # store char (1.5 pt)
    addiu $a0, $a0, 1              # move to next char (1 pt)
    jal toLower                    # recurse (0.5 pt)
    addiu $v0, $v0, 1              # (1 pt)

return: lw $ra, 0($sp)            # epilogue
        addiu $sp, $sp, 4
        jr $ra # return
```
Question 5: MIPS Instruction Formats (12 pts)

For a new microprocessor, we’re going to use a MIPS-like assembly language but with 16-bit words and instructions. We want all of the same instruction fields as MIPS, but now need to resize them.

a) Can we still support 32 registers (circle one)? Yes // No (2 pts)

Provide a brief explanation.

With 32 registers, rs, rt and rd would be 5 bits. This only leaves 1 bit which is insufficient for opcode, shamt, and funct in R-type instruction format.

b) If we want to keep the J-format instructions (j and jal) but want a target address field of 12 bits, what is the maximum number of I-format instructions we can support? (Hint: don’t forget about R-format) (3 pts)

\[2^4 - 1 - 2 = 13\]

c) If our immediate field is 9 bits wide, what is the maximum jump forward a program could make (relative to the current instruction, not the next instruction) with a single branch instruction? Answer in number of instructions. (3 pts)

\[2^8 = 256\]

d) Using the following arbitrary choices for field sizes, translate the following MIPS-like instruction into machine code for our new microprocessor. Assume the same instruction and register numbering systems as MIPS. (3 pts)

\[srl \; $2, \; $3, \; 2\]

<table>
<thead>
<tr>
<th>Field</th>
<th>bits</th>
</tr>
</thead>
<tbody>
<tr>
<td>opcode (3)</td>
<td>000</td>
</tr>
<tr>
<td>rs (2)</td>
<td>00</td>
</tr>
<tr>
<td>rt (2)</td>
<td>11</td>
</tr>
<tr>
<td>rd (2)</td>
<td>10</td>
</tr>
<tr>
<td>shamt (4)</td>
<td>0010</td>
</tr>
<tr>
<td>funct (3)</td>
<td>010</td>
</tr>
</tbody>
</table>

e) Stanley Stanfurd claims that for 16-bit words, our shamt field must be 4-bits wide, but we counter that we can get away with fewer (e.g. 2 bits). Briefly explain why. (1 pt)

Can perform larger shifts using multiple shift instructions (following RISC principles).
Question 6: Running a Program (9 pts)

The stored-program concept revolutionized computing by allowing machines to be multipurpose (i.e. run many different programs) instead of specialized or hard-coded.

a) Circle all that apply. If I decide to write my program in a compiled language instead of an interpreted language, then I would expect the program to be: (3 pts)

- FASTER
- SLOWER
- LARGER
- SMALLER
- PORTABLE
- NON-PORTABLE

b) Which stage in CALL actually creates the Code section in memory? (2 pts)

- Loader

(c) Which stage in CALL allows the reuse of other people’s code? (2 pts)

- Linker

d) What information in an object file allows for the displacement of instructions in the Code section of memory when multiple files are combined in the executable? (2 pts)

- Relocation Table