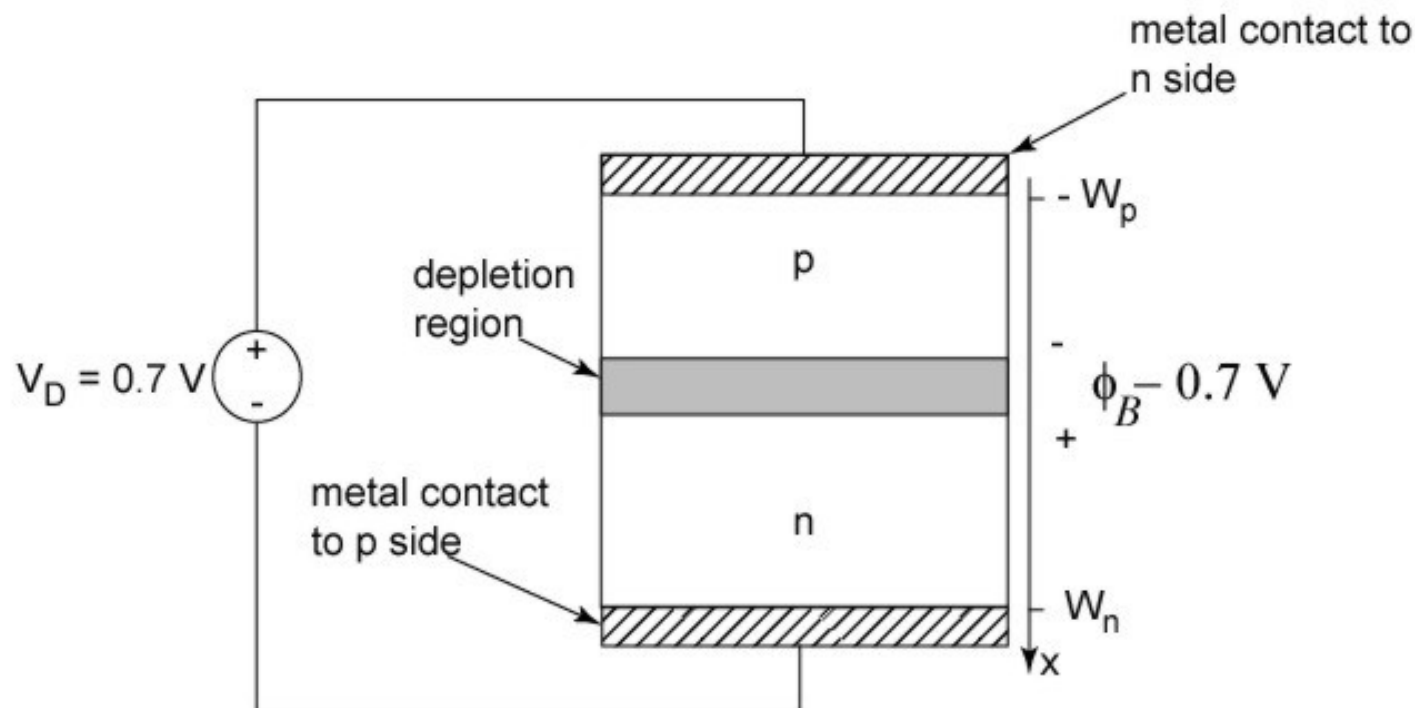


# Lecture 17

- Last time:
  - Complete small-signal model: add capacitors
  - P-channel MOSFET
- Today :
  - pn junctions under *forward* bias (Chapter 6)

# Junction Diode with $V_D = 0.7 \text{ V}$



Barrier is reduced by forward bias  
(what about “ohmic contacts”?)

# What Happens Inside the Junction?

Electric field in the depletion region is reduced →  
 imbalance and net transport of holes from  
 p side into n side and electrons in the other direction

Physical process is called *diffusion* and results in a  
 diffusion current density

$$J_p^{diff} = -qD_p \frac{dp}{dx} \qquad J_n^{diff} = qD_n \frac{dn}{dx}$$

note “downhill” = -  $d(\ )/dx$

# Minority Carriers at Junction Edges

Minority carrier concentration at boundaries of depletion region increase as barrier lowers ... the function is

$$\frac{p_n(x = x_n)}{p_p(x = -x_p)} = \frac{\text{(minority) hole conc. on n-side of barrier}}{\text{(majority) hole conc. on p-side of barrier}}$$

$$= e^{-(\text{Barrier Energy}) / kT}$$

$$\frac{p_n(x = x_n)}{N_A} = e^{-q(\phi_B - V_D) / kT}$$

(Boltzmann's Law)

# The Thermal Voltage

Define  $V_{th} = q / kT$  as the *thermal voltage*

Value:  $q = 1.6 \times 10^{-19}$  C,  $k = 1.38 \times 10^{-23}$  J/K  
 $T = 300$  K

$V_{th} = 26$  mV at room temperature

# “Law of the Junction”

Minority carrier concentrations at the edges of the depletion region are given by:

$$p_n(x = x_n) = N_A e^{-q(\phi_B - V_D)/kT}$$

$$n_p(x = -x_p) = N_D e^{-q(\phi_B - V_D)/kT}$$

Note 1:  $N_A$  and  $N_D$  are the majority carrier concentrations on the *other* side of the junction

Note 2: we can reduce these equations further by substituting  $V_D = 0$  V (thermal equilibrium)

Note 3: assumption that  $p_n \ll N_D$  and  $n_p \ll N_A$

# Thermal Equilibrium Case

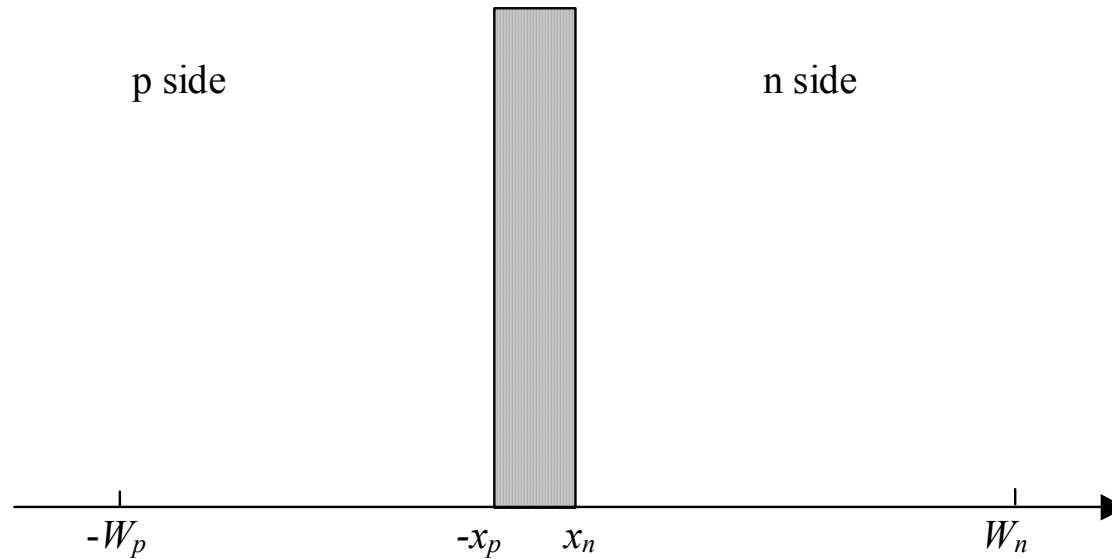
Define  $p_{no}$  as thermal equilibrium hole concentration on the n-side of the junction ...

$$p_{no} = \frac{n_i^2}{N_D} = N_A e^{-(\phi_B - 0)/V_{th}}$$

Solve for the built-in barrier

Alternative form of junction law:

# Boundary Conditions

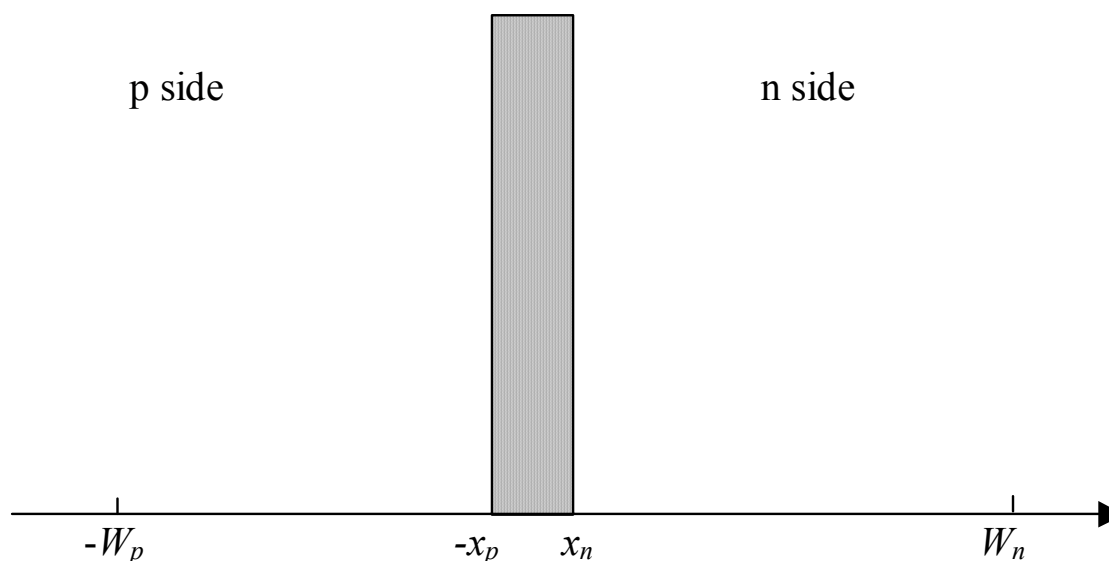


Depletion region edges:  
Ohmic contacts:

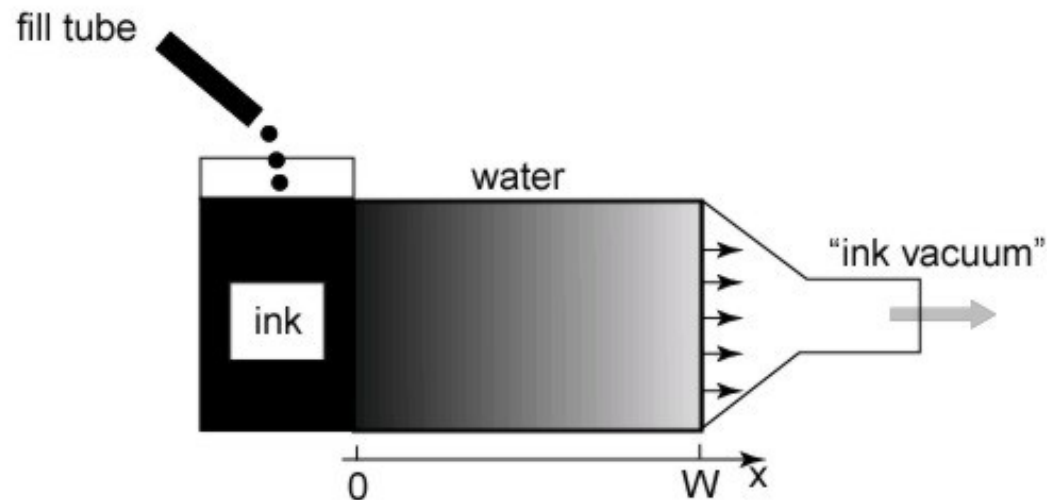
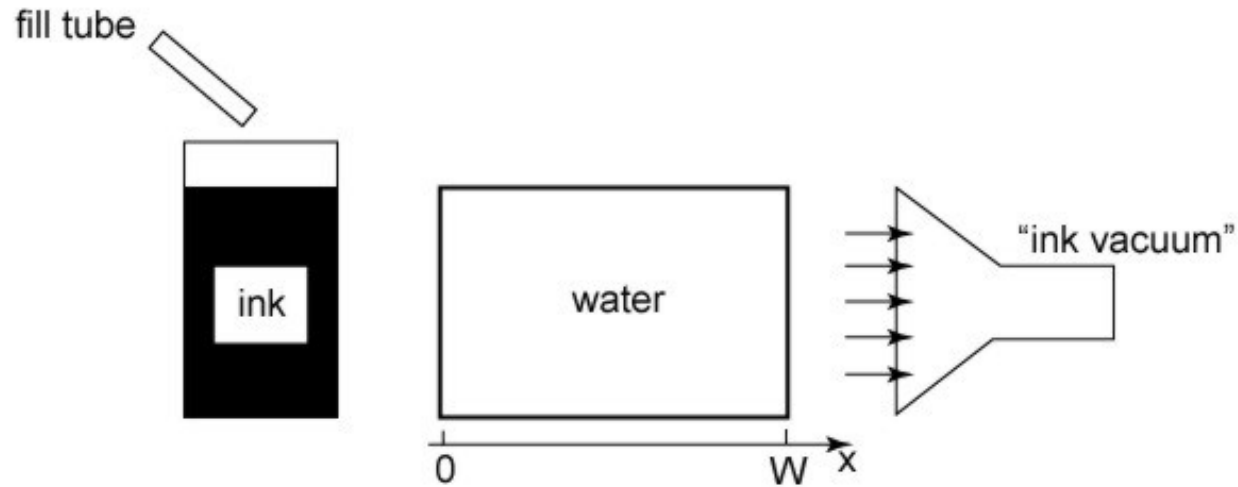


# Steady-State Concentrations

Assume that none of the diffusing holes and electrons recombine  $\rightarrow$  get straight lines ...



# Diffusion Analogy



# Diode Current Densities

$$J_n^{diff} = qD_n \left. \frac{dn_p}{dx} \right|_{x=-x_p}$$

$$J_p^{diff} = -qD_p \left. \frac{dp_n}{dx} \right|_{x=x_n}$$

Total current:

$$J =$$