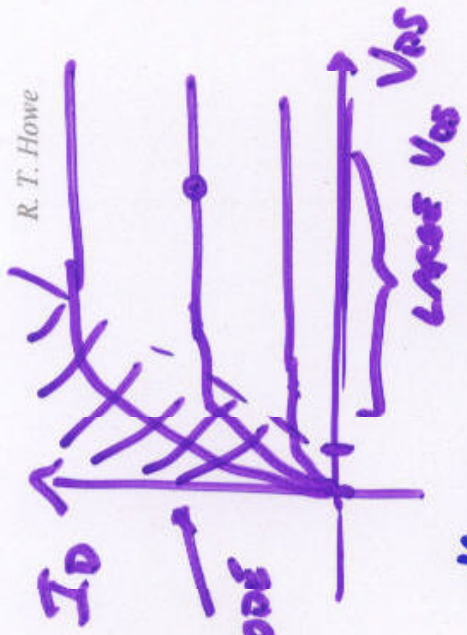


**LAB 4 REPORT IS DUE AT BEGINNING OF YOUR LAB SECTION!**

# Lecture 15

TRIODE



• Last time:

- Square-law MOSFET model
- Linear MOSFET model.

"PARTS ZERO"

$$I_D = -WQ_N(y) \overline{v_{tr}}(y)$$

• Today :

- MOSFET small-signal model, three (four) terminal device  $\rightarrow$  complicated!

CHANGE AVERAGES...  
GOT USEFUL RESULTS

$$i_D = f(\overline{v_{gs}}, \overline{v_{ds}}, \overline{v_{bs}})$$

$$g_m = f(v_{gs})$$



NEXT TIME.

Dep

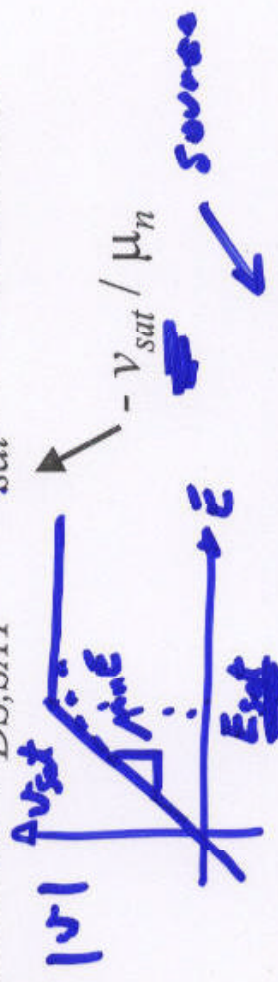
University of California at Berkeley

**WHICH REGION YOU'RE OR IN.**

# Linear MOSFET Model

- Channel (inversion) charge: neglect reduction at drain

Velocity saturation defines  $V_{DS,SAT} = E_{sat} L = \text{constant}$

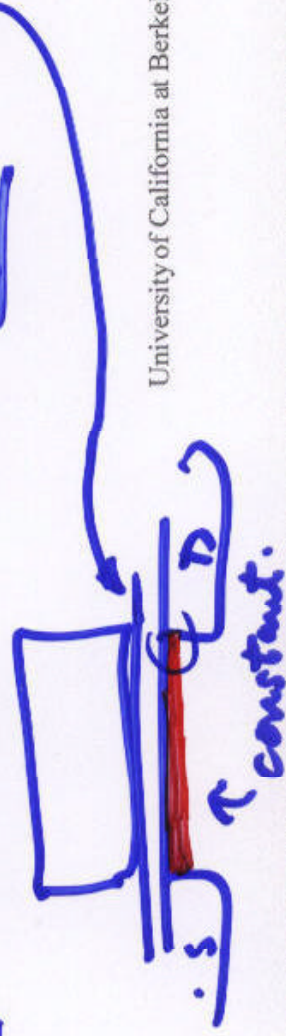


Drain current:  $v_{sat}$

$$I_{D,SAT} = -Wv_{sat}Q_N = -W(v_{sat})[-C_{ox}(V_{GS} - V_{Th})]$$

*Very small.*

$$|E_{sat}| = 10^4 \text{ V/cm}, L = 0.12 \mu\text{m} \rightarrow V_{DS,SAT} = 0.12 \text{ V!}$$

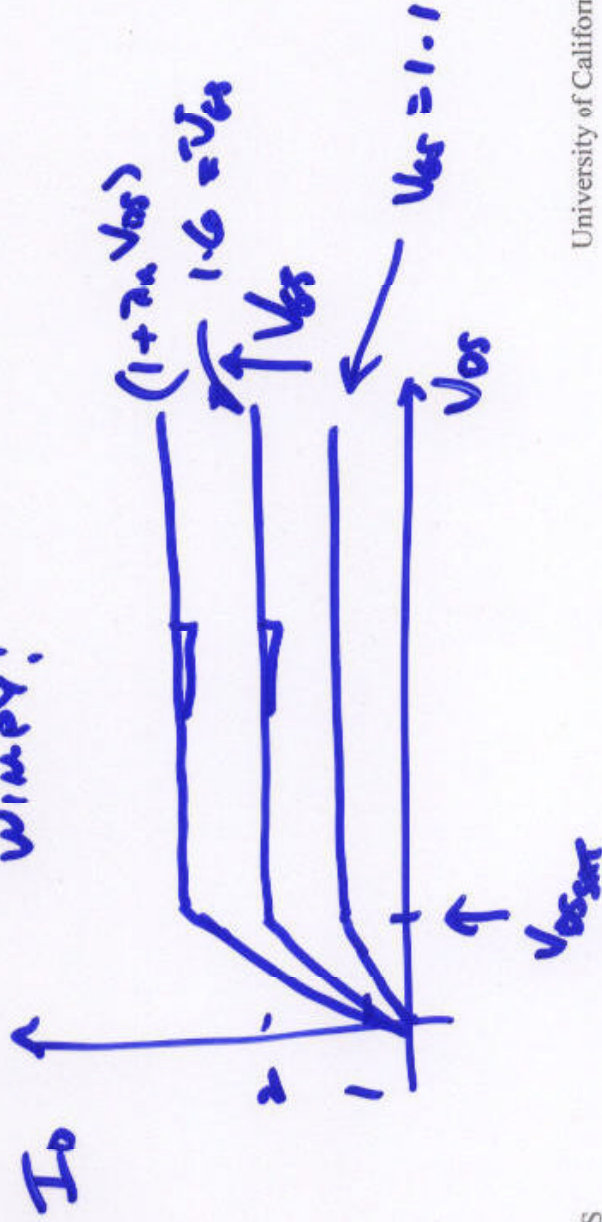


# Linear MOSFET in Saturation

$$I_{D,SAT} = v_{sat} WC_{ox} (V_{GS} - V_{Th}) \underbrace{(1 + \lambda_n V_{DS})}_{\text{EDGE FACTOR}} \quad 0.6V$$

Implication of weaker dependence on  $V_{GS}$ :

wimpy!



$I_D = f(v_{GS}, v_{DS})$   
 ASSUME  $\rightarrow$   
 $i_D(t) = f(v_{GS}(t), v_{DS}(t))$   
 OK.

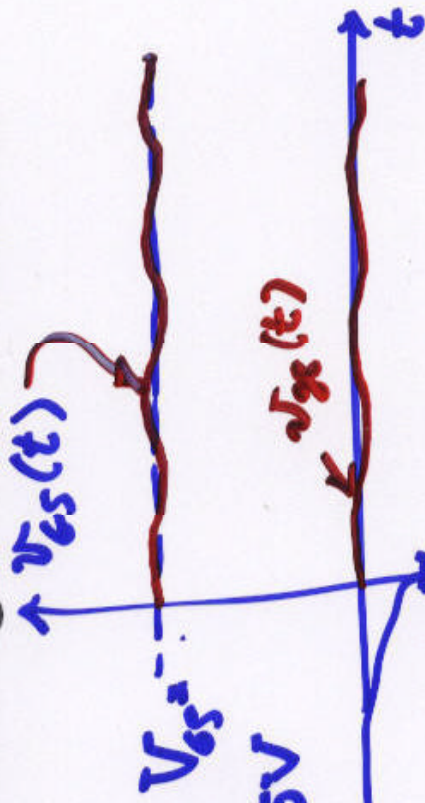
# Why Find an Incremental Model?

- Signals of interest in analog ICs are often of

the form:

$$v_{GS}(t) = V_{GS} + v_{gs}(t)$$

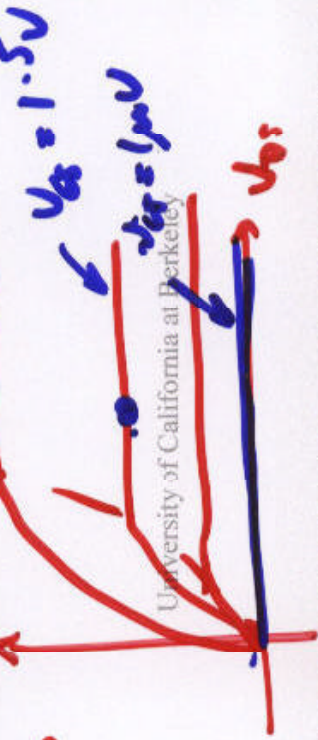
SET UP THE MOSFET



Direct substitution into  $i_D = f(v_{GS}, v_{DS})$  is

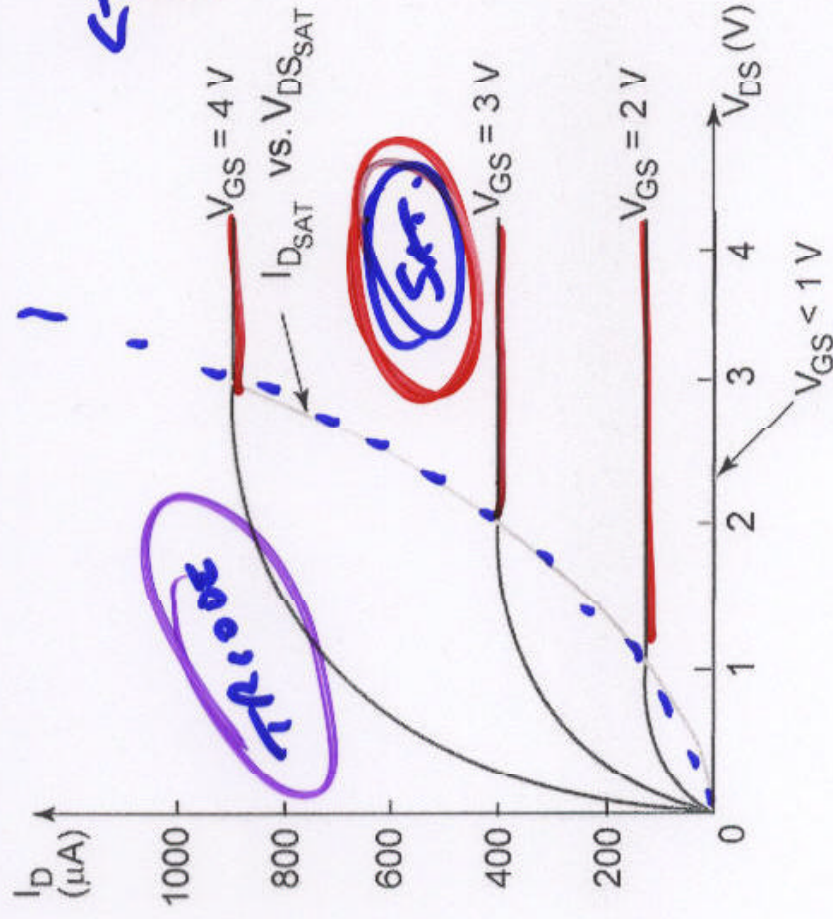
tedious AND doesn't include charge-storage

effects ... pretty rough approximation



# Which Operating Region?

USEFUL



Sat. Low.

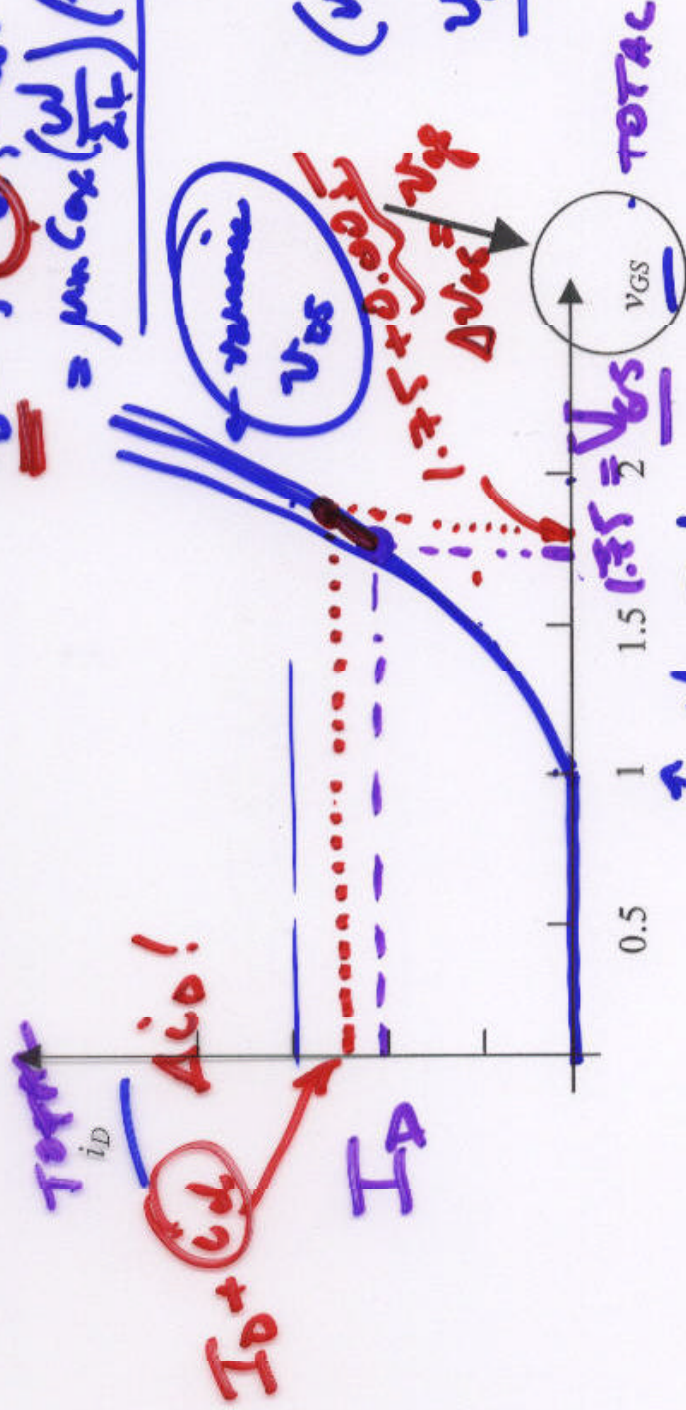
$$\frac{d}{dt} \left( \frac{d}{dt} \right)$$

# Changing One Variable at a Time

$$i_D = f(v_{GS}, v_{DS})$$

$$= \mu_n C_{ox} \left( \frac{W}{L} \right) (v_{GS} - v_{Th})^2$$

$(1 + \lambda v_{DS})$   
 $(v_{DS} \geq V_{DS,SAT})$   
 $v_{GS} \geq v_{Th}$



Assumption:  $V_{DS} > V_{DS,SAT} = V_{GS} - V_{Th}$  (square law)



## The Transconductance $g_m$

Defined as the change in drain current due to a change in the gate-source voltage, with everything else constant.

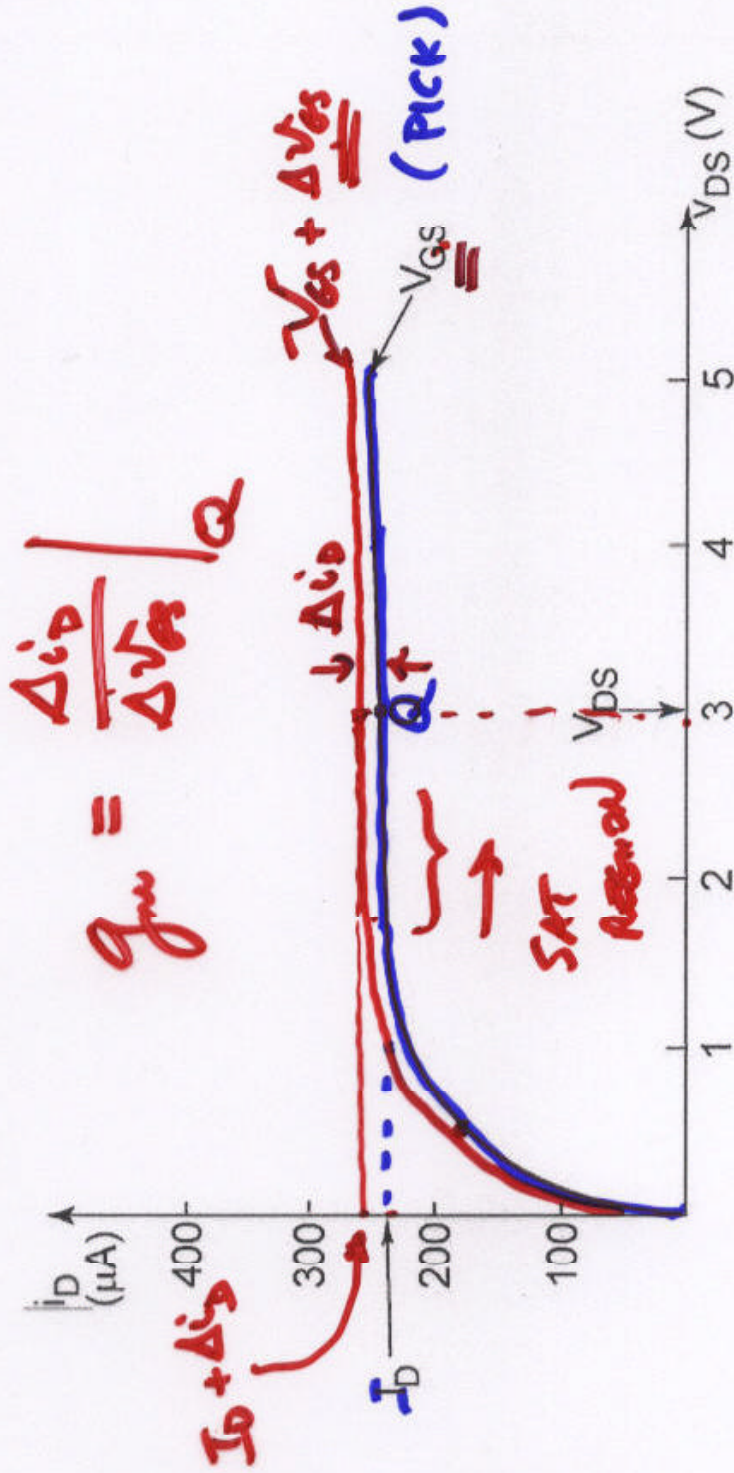
$$g_m = \frac{\Delta i_D}{\Delta v_{GS}} \Big|_{\substack{V_{GS}, V_{DS} \\ \text{bias point}}} = \frac{\partial i_D}{\partial v_{GS}} \Big|_{\substack{V_{GS}, V_{DS} \\ \text{bias point}}} = \left( \frac{W}{2L} \right) \mu_n C_{ox} \cdot 2 (V_{GS} - V_{Tn}) (1 + \lambda_n V_{DS})$$

Square-law: MOSFET saturation region

$$i_D = (W/2L) \mu_n C_{ox} (v_{GS} - V_{Tn})^2 (1 + \lambda_n v_{DS})$$

$$\rightarrow g_m = \mu_n C_{ox} (W/2L) (V_{GS} - V_{Tn}) (1 + \lambda_n V_{DS})$$

# Another Way to Find $g_m$ (Case 5)



$$\underline{Q = (V_{GS}, V_{DS})}$$



# Evaluating $g_m$

Square-law characteristic: H&S 1st Edition

$$g_m = \mu_n C_{ox} (w/l) (V_{GS} - V_{Tn}) \quad \approx \quad \text{WE NEED}$$

$$= \mu_n C_{ox} (w/l) (V_{GS} - V_{Tn}) \quad \text{A SIMPLER}$$

$$\left( \frac{g_m}{I_D} \right) = \sqrt{\frac{I_D \cdot 2 \mu_n C_{ox} (w/l)}{I_D}} \propto \sqrt{I_D} \quad \text{EXPRESSION}$$

Linear characteristic: better for submicron CMOS

$$i_{D,SAT} = v_{sat} W C_{ox} (v_{GS} - V_{Tn}) (1 + \lambda_n v_{DS})$$

$$\left. \begin{aligned} \mu_n C_{ox} &= 100 \mu A/V^2 \\ (w/l) &= 50 \\ I_D &= 100 \mu A \end{aligned} \right\} g_m = \{ 100 \cdot 2 \cdot 50 \cdot 100 \}^{1/2}$$

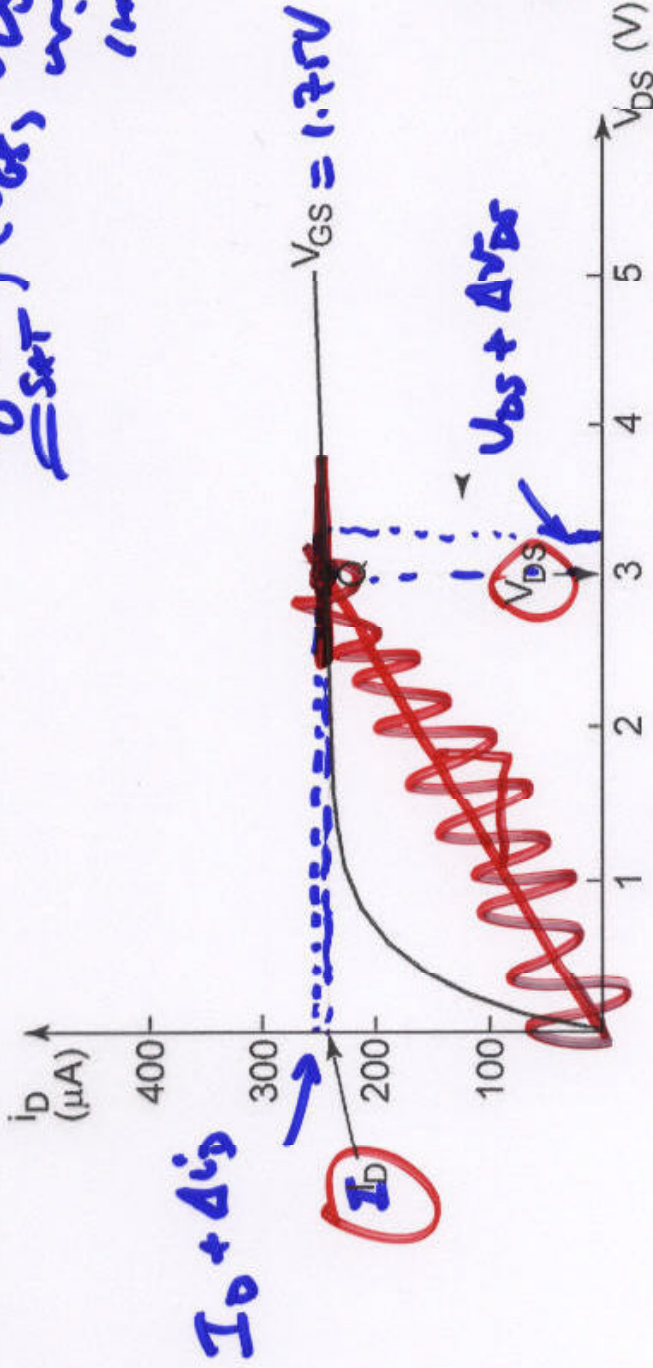
$$= (100^{3/2}) \mu S = 1 mS$$

# • Output Resistance $r_o$

Defined as the inverse of the change in drain current due to a change in the *drain-source* voltage, with everything else constant

$$i_D = f(v_{GS}, v_{DS})$$

(increment)



$$\frac{\Delta i_D}{\Delta v_{DS}} \Big|_{V_{GS}=1.75V, V_{DS}=3V} = \text{small}$$

# Evaluating $r_o$

$$r_o = \left( \frac{\partial i_D}{\partial v_{DS}} \Big|_{V_{GS}, V_{DS}} \right)^{-1} \underbrace{g_o}_{g_o} = \left[ \underbrace{\left\{ \mu_n C_{ox} \left( \frac{W}{L} \right) (V_{GS} - V_{tn})^2 (1 + \lambda v_{DS}) \right\}}_{\lambda I_D} \right]^{-1}$$

$$= \left[ \mu_n C_{ox} \left( \frac{W}{L} \right) (V_{GS} - V_{tn})^2 \cdot \lambda \right]^{-1}$$

$$r_o = \frac{1}{\mu_n C_{ox} (W/L) (V_{GS} - V_{tn})^2 \cdot \lambda} = \frac{1}{\lambda_n I_D}$$

Typical value:  $\approx I_D$  (with no fudge factor)

~~$r_o \neq \frac{V_{GS} - V_{tn}}{I_D}$~~