EECS105 Name
Final
5/12/10 SID

| 1 | $/ 20$ |
| :--- | ---: |
| 2 | $/ 30$ |
| 3 | $/ 20$ |
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| 5 | $/ 30$ |
| 6 | $/ 40$ |
| 7 | $/ 20$ |
| 8 |  |
| Total |  |

1. Give a short answer to each question
a. Your friend from Stanford says that he has designed a three-stage high gain amplifier that works great, but when he puts it in unity-gain feedback he sees a big sine wave at high frequency. He thinks that maybe it's power supply noise that is getting amplified. What do you tell him?
b. Your friend from USC is trying to make an oscillator by using feedback around a single-stage high-gain amplifier. Her circuit doesn't oscillate. Open loop, it works great as an amplifier though, with a phase shift that varies between -180 and -270 degrees from the input to the output over all frequencies. She thinks that maybe she should try to increase the gain to get it to oscillate. What do you tell her?
c. If you measure the reverse leakage current of a diode at room temperature to be 1 nA , and the increase the temperature to 85 C , will the leakage current increase or decrease, and by roughly what factor chosen from this list: \{a lot less than 2 , roughly 2 , roughly 10 , a lot more than 10$\}$
d. Why do circuit designers like to use feedback when they make amplifiers? Give at least two reasons.
2. You have invented a new type of transistor with terminals $A, B$, and $C$. In the "active" region, defined by $\mathrm{V}_{\mathrm{AC}}>0, \mathrm{~V}_{\mathrm{BC}}>1$, you have determined the formulas for the currents into nodes A and B are:
$\mathrm{I}_{\mathrm{A}}=\mathrm{I}_{0} \propto \mathrm{~V}_{\mathrm{AC}}$
$\mathrm{I}_{\mathrm{B}}=\mathrm{I}_{0}\left(\beta \mathrm{~V}_{\mathrm{AC}}\right)^{3} \ln \left(\delta \mathrm{~V}_{\mathrm{BC}}\right)$
Where $\mathrm{I}_{0}, \alpha, \beta$, and $\delta$ are process-related parameters. For simplicity, assume that $\alpha$, $\beta$, and $\delta$ are all equal to $1\left[\mathrm{~V}^{-1}\right]$, and $\mathrm{I}_{0}=1 \mathrm{~mA}$.

How would you wire this device up to make a simple voltage amplifier with a gain of at least 10? Draw your circuit below, using only a resistor $\mathrm{R}_{\mathrm{L}}$ and a 10 V supply. Clearly identify the input and output terminals of your amplifier. What input bias bias point ( $\mathrm{V}_{\text {in }}^{*}$ and $\mathrm{V}^{*}$ out $)$ and resistor value would you pick? Hint: calculate the intrinsic gain as a function of the bias point voltages first.
At this bias point, calculate the input resistance, transconductance, and output resistance of your transistor, and the gain of your amplifier. Draw the DC smallsignal model of your transistor.

3. In the current mirror below, assume that $\mu_{\mathrm{n}} \mathrm{C}_{\mathrm{ox}}=200 \mathrm{uA} / \mathrm{V}^{2}, \lambda=0.1 / \mathrm{V}$, and $\mathrm{V}_{\mathrm{TN}}=1 \mathrm{~V}$. All transistors have $\mathrm{W} / \mathrm{L}=100 \mathrm{u} / 1 \mathrm{u}$. Calculate the gate bias voltage $\mathrm{V}_{\mathrm{GS} 1}$ resulting from the input current. Calculate the currents flowing in the drains of the other transistors. All calculations should be accurate to a few percent.

4. Given the spice input and a portion of the hspice output below, find the bias point $\left(\mathrm{V}^{*}\right.$ in and out), transconductance, input resistance and output resistance of the transistor, and the voltage gain of this circuit. Answers should be accurate to within a few $\%$.
$\mathbf{V}^{*}{ }^{\text {in }}=$

$$
\mathbf{V}_{\text {out }}^{*}=
$$

input resistance $=$

## transconductance=

output resistance $=$

```
[ Hspice input deck]
* Common Emitter test deck
Vcc cc 0 3
Vin in 0 dc 0.6
.model npn npn bf=100 IS=1e-15 vaf=50
Q1 out in 0 npn
Rc cc out 100k
.op
.options post
. end
[Portion of hspice output]
    subckt
    element 0:q1
    model 0:npn
        ib 138.7999n
        ic 14.1533u
        vbe 600.0000m
        vce 1.5847
        vbc -984.6662m
        vs -1.5847
        power 22.5116u
        betad 101.9693
        gm 550.6107u
        rpi 185.0998k
        rx 0.
        ro 3.6023x
        cpi 0.
        cmu 0.
        cbx 0.
        ccs 0.
        betaac 101.9179
        ft 87.6324g
```

5. For the circuit below, find the operating point voltages and currents $\mathrm{I}_{\mathrm{B}}$, and $\mathrm{I}_{\mathrm{C}}$. Calculate the DC gain from point A to point B . Calculate the DC gain from point B to point C . Assume $\mathrm{I}_{\mathrm{S}}=4 \times 10^{-15} \mathrm{~A}, \beta=100$, and $\mathrm{V}_{\mathrm{A}}=100 \mathrm{~V}$. Answers should be accurate to $\mathbf{1 0 \%}$.

| $\mathbf{V}_{\mathrm{B}}^{*}=$ | $\mathbf{V}_{\mathrm{C}}^{*}=$ | $\mathbf{V}_{\mathrm{E}}^{*}=$ |
| :--- | :--- | :--- |
| $\mathbf{I}_{\mathrm{B}}^{*}=$ | $\mathbf{I}_{\mathrm{C}}^{*}=$ | DC gain, $\mathbf{A}->\mathbf{B}$ <br> $=$ |
| DC gain, $\mathbf{B}->\mathbf{C}=$ |  |  |

For what range of frequency does the gain from A->B become approximately one? (for example "X rad/sec and below", or "X to Y rad/sec")

## Frequency range:

What is the frequency at which the gain from $B$ to $C$ is $\mathbf{1 0}$ times greater than the $D C$ value above? What is the maximum gain from A to C ?

max gain:


On the next page, draw a Bode plot of the transfer function from A to C .
6. You have a CMOS inverter with $(\mathrm{W} / \mathrm{L})_{\mathrm{N}}=10 \mathrm{u} / 1 \mathrm{u}$ and $(\mathrm{W} / \mathrm{L})_{\mathrm{P}}=20 \mathrm{u} / 1 \mathrm{u}$ running from a $4 V$ supply. Assume that $\mu_{n} C_{o x}=200 u A / V^{2}, \mu_{p} C_{o x}=100 u A / V^{2}, \lambda_{N}=\lambda_{P}=0.1 / \mathrm{V}$, and $\mathrm{V}_{\mathrm{TN}}=1 \mathrm{~V}, \mathrm{~V}_{\mathrm{TP}}=-1 \mathrm{~V}$. Carefully plot the drain current vs. output voltage for the NMOS device when $\mathrm{V}_{\text {IN }}=2 \mathrm{~V}$. On the same plot, carefully draw the magnitude of the PMOS drain current vs. the output voltage when $\mathrm{V}_{\mathrm{IN}}=2 \mathrm{~V}$. (10pts)


What is the DC output value with this input? At this operating point, what region of operation is each transistor in (off, linear, saturation)?
$\mathbf{V}_{\text {out }}(2 \mathrm{~V})=$

| NMOS region | PMOS region |
| :--- | :--- |

For this region of operation, estimate the gain at this operating point, and the approximate output voltage limits ( $\mathrm{V}_{\text {out,min }}$ and $\mathrm{V}_{\text {out,max }}$ ), and the corresponding input min and max.

| gain $=$ | $\mathbf{V}_{\text {out,min }}=$ | $\mathbf{V}_{\text {out,max }}=$ |
| :--- | :--- | :--- |
|  | $\mathbf{V}_{\text {in,max }}=$ | $\mathbf{V}_{\text {in,min }}=$ |
|  |  |  |

What is the range of input voltages for which the DC output is $\mathrm{V}_{\mathrm{DD}}$ ? What is the range of input voltages for which the DC output is 0 ?

| $V_{\text {in }}$ range for Vout $=V_{D D}$ | $V_{\text {in }}$ range for Vout $=0$ |
| :--- | :--- |

On the next page, plot the DC voltage transfer curve of this inverter (10pts).
LABEL YOUR AXES CLEARLY!


Note: everyone knows roughly what this curve looks like. You get points for showing me that you know *exactly* what it looks like (at least in the regions described on the previous page). Be neat, and label things clearly!
7. The inverter in the previous problem is used to switch a capacitive load. The total output capacitance is 1 pF . Up to time $\mathrm{t}=0$, the input to the amplifier is 0 , and the output is $\mathrm{V}_{\mathrm{DD}}$. At time $\mathrm{t}=0$ the input switches instantaneously to $\mathrm{V}_{\mathrm{DD}}$. What is the initial rate of change of the output voltage just after $\mathrm{t}=0$ ? How long does it take for the output to fall 400 mV (to $\mathrm{V}_{\mathrm{DD}}-400 \mathrm{mV}$ )?

| $\mathbf{d V} V_{\text {out }} / \mathbf{d t}(\mathbf{t}=\mathbf{0})=$ | $\mathbf{t}_{\text {fall } 400 \mathrm{mV}}=$ |
| :--- | :--- |

What is the differential equation that describes the output voltage when $\mathrm{V}_{\text {out }}<\mathrm{V}_{\mathrm{DD}} /$ 10? How long does it take for the output to fall from $\mathrm{V}_{\mathrm{DD}} / 10=400 \mathrm{mV}$ to approximately $\mathrm{V}_{\mathrm{DD}} / 27=400 \mathrm{mV} / 2.7$ ? Your answers should be accurate to $10 \%$.

## Differential equation

Time to fall by a factor of 2.7 from 400 mV :
8. For the circuit below, what condition must be satisfied for the circuit to oscillate when you close the loop (short $\mathrm{V}_{\mathrm{FB}}$ to $\mathrm{V}_{\text {IN }}$ )?

## condition for oscillation

For some value of $\mathrm{C}_{\mathrm{FB}}$ and $\mathrm{R}_{\mathrm{FB}}$, you plot the open-loop transfer function from $\mathrm{V}_{\mathrm{IN}}$ to $\mathrm{V}_{\mathrm{FB}}$. You find that there is a pole at $\omega=1 /\left(\mathrm{R}_{\mathrm{FB}} \mathrm{C}_{\mathrm{FB}}\right)$ that is substantially lower than all of the other poles in the system. You also find that at the frequency where the phase crosses -360 , the gain is about 50 . Will the system oscillate if you close the loop? If yes, how would you change $\mathrm{C}_{\mathrm{FB}}$ to stop it from oscillating, and why would that work?

## Will it oscillate?

## If so, how and why change $\mathrm{C}_{\mathrm{FB}}$ ?

For some different values of $\mathrm{C}_{\mathrm{FB}}$ and $\mathrm{R}_{\mathrm{FB}}$, you plot the open-loop transfer function and find that at the frequency where the phase crosses -360 the gain is about 0.1 . Will the system oscillate if you close the loop? If yes, how would you change $\mathrm{C}_{\mathrm{FB}}$ to stop it from oscillating, and why would that work?

## Will it oscillate?

## If so, how and why change $\mathrm{C}_{\mathrm{FB}}$ ?



