

**Homework 6 : Due by 8 p.m. on Monday October 25**

1. Problem 6. on pg. 444 of LV.
2. Problem 7.29 on pg. 566 of OWN.
3. Problem 7.47 on pg. 577 of OWN.
4. Problem 7.50 on pp. 578 -579 of OWN.
5. This MATLAB problem is aimed at exploring aliasing. First, check that the signal

$$x(t) = \frac{W}{4\pi} \text{sinc}^2\left(\frac{Wt}{4\pi}\right),$$

has Fourier transform

$$X(j\omega) = \begin{cases} 1 - \left| \frac{2\omega}{W} \right| & \text{if } -\frac{W}{2} < \omega < \frac{W}{2} \\ 0 & \text{elsewhere} \end{cases},$$

which is bandlimited with one sided bandwidth  $\omega_M = \frac{W}{2}$ . From the sampling theorem we know that if the signal is sampled with sampling interval  $T$  satisfying  $\frac{2\pi}{T} > W$ , then

$$x_r(t) = \sum_{n=-\infty}^{\infty} x(nT) \text{sinc}\left(\frac{t}{T} - n\right) \quad (1)$$

is a perfect reconstruction of  $x(t)$  (see equation (7.11) on pg. 523 of OWN). If the sampling interval  $T$  is such that  $W > \frac{2\pi}{T}$  then reconstruction using the formula in equation (1) should result in aliasing.

For this problem, pick  $W = 8$ . If the sampling interval is  $T = 0.5$  we would have perfect reconstruction, while with  $T = 2$  we should expect to see aliasing.

- (a) Plot  $x(t)$  over  $-10 < t < 10$  using MATLAB.
- (b) For  $T = 0.5$ , plot  $x_r(t)$ , given by equation (1), over the range  $-10 < t < 10$  using MATLAB. Make sure that you take sample values over the interval  $-200 < nT < 200$  in carrying out the computation in equation (1).
- (c) For  $T = 2.0$ , plot  $x_r(t)$ , given by equation (1), over the range  $-10 < t < 10$  using MATLAB. Make sure that you take sample values over the interval  $-200 < nT < 200$  in carrying out the computation in equation (1).

Do NOT submit any M-files. You simply need to submit three plots.