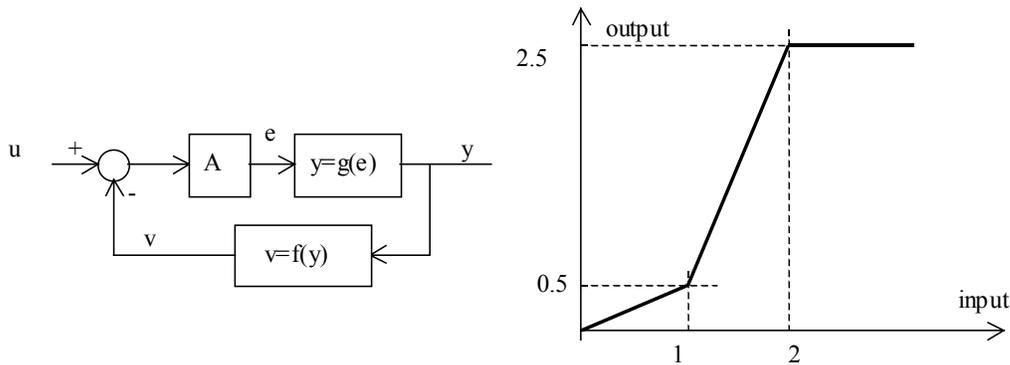


Due on 9/15/04 (before the Wednesday lab session)

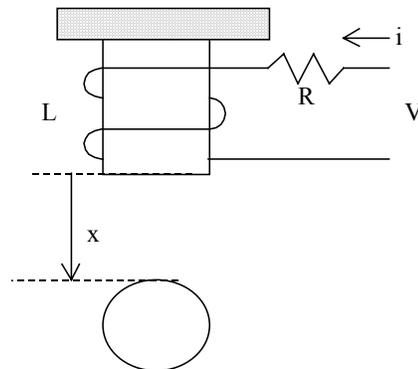
Consider the following feedback system where  $u$  is the input and  $y$  is the output.

- (1) Assume  $v=y$  (i.e.,  $f(\cdot)$  is the identity function),  $A=20$ , and the graph of the function  $g$  is shown below. Sketchy the  $y$  vs.  $u$  graph. The  $y$  variable in your graph must cover the interval  $[0\ 3]$  and you must specify the coordinate of any 'break point' of the graph.
- (2) Assume  $y=e$  (i.e.,  $g(\cdot)$  is the identity function),  $A=20$ , and the graph of the function  $f$  is shown below. Sketchy the  $y$  vs.  $u$  graph. The  $y$  variable in your graph must cover the interval  $[0\ 3]$  and you must specify the coordinate of any 'break point' of the graph.
- (3) Repeat the (1) and (2) but assume  $A \rightarrow \infty$ .
- (4) The function  $g(\cdot)$  can be thought of as the 'plant' and  $f(\cdot)$  as the sensor. Draw some conclusions from the above analysis on the magnitude of  $A$  and the effect of  $f(\cdot)$  on the transfer function (i.e., graph) of  $y$  vs.  $u$ .



- (2) The figure on the right shows a ball suspension system. The steel ball is suspended in the air by the electromagnetic force generated by the electromagnet.

The magnetic force acting on the ball is  $F=(k \cdot i^2)/x^2$ , the mass of the ball is  $m$ . Gravitational constant is  $g$ . The inductance of the magnet is  $L$  and the resistance of the magnet winding is  $R$  (as represented by a resistor in the figure). Using the state vector  $x$  defined below, write a nonlinear state equation ( $V$  is the input and  $x$  is the output variable).



$X=[i, x, v]$  where  $v$  is the speed of ball.

- (3) Problem 2.23 in the textbook.
- (4) Draw a block diagram of the motor system in Problem 2.23.
- (5) If the armature circuit of a DC motor is driven by a controlled current source, the effects of armature winding resistance ( $R_a$ ), armature inductance ( $L_a$ ), and the back emf ( $K_e$ ) are completely nullified. In such a case, the armature current  $i_a$  should be considered as the input variable. Assume the motor in Problem 2.23 is driven by a controlled current source ( $i_a$ ). Find the transfer function between  $i_a$  and  $\theta_2$ . (Hint: This is a 4<sup>th</sup> order transfer function.)