

**Due at 1700, Fri. Mar. 3 in homework box under stairs, first floor Cory .**

Note: up to 2 students may turn in a single writeup. Reading Nise 8, 9  
Midterm: Thurs. Mar. 9, Location: 277 Cory, 0810-0930 am.

1. (22 pts) Root locus (Nise 8.7)

Given the unity gain feedback system in Fig. 1, where

$$G(s) = \frac{K(s+15)(s+40)}{(s+30)(s^2-20s+200)}$$

[11 pts] a) Find and approximately hand sketch the root locus using RL rules 1-8.

[4 pts] b) Find the range of  $K$  which makes the system stable.

[5 pts] c) Using the second order approximation (assuming dominant 2nd order poles) find the value of  $K$  that gives  $\zeta = 0.5$  and  $T_s \approx 0.2$  for the system's dominant closed-loop poles.

[2 pts] e) Use MATLAB to plot the step response for c) and compare to approximation estimate.

2. (25 pts) Root locus (Nise 8.6, 8.9)

Consider the unity gain feedback system in Fig. 1 with  $G(s) = \frac{k(s-10)(s-5)}{(s+20)(s+10)(s+2)}$ . Here  $-\infty < k < \infty$

[13 pts] a) Apply root locus rules: specify real axis segments, break-away and break-in locations on real axis, and angle of departure from complex poles.

[6 pts] b) Find the  $j\omega$  crossing using Routh-Hurwitz.

[4 pts] c) Hand sketch the closed-loop root locus for positive and negative  $k$ .

[2 pts] d) Find the range of  $k$  for stability.

3. (26 pts) PI compensation (Nise 9.2)

Consider open loop plant

$$G(s) = \frac{2000K}{(s+10)^2(s+20)}$$

and unity feedback.

[5 pts] a) find  $K$  such that overshoot is 20%.

[11 pts] b) Design a PI controller with the same 20% overshoot such that steady state error is 0, with  $T_s \leq 1$  sec. (Hint: PS4-1)

[6 pts] c) Hand sketch the root locus for the original system and the system with a **PI** compensator, and verify with Matlab.

[2 pts] d) Use Matlab to compare the step response for the closed-loop compensated and uncompensated systems, transient and steady state response.

[2 pts] e) Find the steady state error for a step for both systems.

4. (27 pts) PD compensation (Nise 9.3)

Consider open loop plant

$$G(s) = \frac{144K}{s(s+4)(s+12)^2}$$

and unity feedback.

[5 pts] a) find  $K$  such that overshoot is 20%.

[12 pts] b) Design a PD controller (i.e. find zero location) such that  $T_p \approx 0.8$  sec, with the same 20% overshoot.

[6 pts] c) Hand sketch the root locus for the original system and the system with a **PD** compensator, and verify with Matlab.

[2 pts] d) Use Matlab to compare the step response for the closed-loop compensated and uncompensated systems, transient and steady state response.

[2 pts] e) Find the steady state error for a step for both systems.



Fig. 1. Unity Gain Feedback.