## PROBLEM SET \#6

Issued: Thursday, Feb.28, 2013
Due (at 8 a.m.): Friday, Mar. 8, 2013, in the EE 140/240A HW box near 125 Cory.

1. Consider the circuit of Fig. PS6.1, assuming $(W / L)_{1-3}=40 / 0.5, I_{\text {REF }}=0.3 \mathrm{~mA}, \lambda=0.02 \mathrm{~V}^{-1}$, $K^{\prime}=138 \mu \mathrm{~A} / \mathrm{V}^{2}, L_{D}=80 \mathrm{~nm}, \mathrm{~V}_{\mathrm{TH} 0}=0.7 \mathrm{~V}$, and $\gamma=0$.
a. Determine $V_{b}$ such that $V_{X}=V_{Y}$.
b. If $V_{b}$ deviates from the value calculated in part (a) by 100 mV , what is the ratio of $I_{\text {OUT }}$ to $I_{\text {REF }}$ ?
c. If the circuit fed by the current source of Fig. PS6.1 changes $V_{P}$ by 1V, how much do $V_{Y}$ and $I_{\text {OUT }}$ change.
d. Add a transistor to this circuit that will generate $V_{b}$ to the gate of transistor $M_{3}$, while still ensuring that $V_{X}=V_{Y}$. Estimate the minimum output voltage $V_{P}$ of this design.


Figure PS6. 1
2. The circuit of Fig. PS6.2 is designed with $(W / L)_{1,2}=20 / 0.5,(W / L)_{3,4}=60 / 0.5, I_{R E F}=100 \mu \mathrm{~A}$, $K^{\prime}=138 \mu \mathrm{~A} / \mathrm{V}^{2}, L_{D}=80 \mathrm{~nm}, \mathrm{~V}_{\text {тно }}=0.7 \mathrm{~V}, \lambda=0.02 \mathrm{~V}^{-1}, 2 \Phi=0.7 \mathrm{~V}$, and $\gamma=0.4 \mathrm{~V}^{1 / 2}$.
a. Determine $V_{X}$ and the acceptable range of $V_{b}$ that guarantees $\mathrm{M}_{3}$ is biased in saturation.
b. Estimate the deviation of $I_{\text {OUT }}$ from its nominal value if the drain voltage of $M_{4}$ is higher than $V_{X}$ by 1 V .


Figure PS6. 2
3. Fig. PS6.3 shows a two-stage differential amplifier.
a. Calculate the DC operating points including the current flowing through each branch and DC voltage at each node. The DC value of the input nodes is set at zero. Calculate transistor small-signal parameters (i.e. $g_{m}, r_{o}, C_{\pi}$ ).
b. Draw the differential-mode and common-mode half-circuits for the amplifier and provide expressions and calculate the numerical values for the output resistance, $R_{\text {out }}$; gain, $v_{\text {out }} / v_{i n}$; and high-frequency cut-off $f_{H}$.

## BJT parameters:

$$
V_{B E(o n)}=0.7 \mathrm{~V}, \beta=100, V_{A}=50 \mathrm{~V}, V_{C C}=6 \mathrm{~V}, V_{T}=25 \mathrm{mV},
$$

$$
f_{T}=600 \mathrm{MHz} \text { at } I_{C}=1 \mathrm{~mA}, C_{\mu}=0.2 \mathrm{pF}, C_{j e}=2 \mathrm{pF}, C_{c s}=1 \mathrm{pF} ;
$$



Fig. PS6. 3
4. For the amplifiers shown in Fig. PS6.4, provide expressions for the gain, output resistance and high-frequency cut-off $f_{H}$, in terms of transistors small-signal parameters (i.e. $g_{m}, g_{m b}, r_{o}$, $\left.C_{\pi}, C_{\mu}, C_{c s}, C_{g s}, C_{g d}, C_{d b}, C_{s b}\right)$ for common-mode and differential-mode input.


Fig. PS6. 4

