## Homework 2

Due: Friday, 7 February 2014 at 1pm

## This is an individual assignment!

PROBLEM 1 (10pts):
Derive the expressions for input resistance $R_{\text {in }}$, output resistance $R_{\text {out }}$, voltage gain $A_{v}=v_{\text {out }} / v_{\text {in }}$ as a function of small-signal parameters (i.e. gm, rpi, ro, etc.) and given circuit elements for circuits in Figure 1a,b. Assume that all capacitors have infinite values.


Figure 1

## PROBLEM 2 (10pts):

An NMOS transistor has parameters $W=10 \mu \mathrm{~m}, L=1 \mu \mathrm{~m}, k^{\prime}=190 \mu \mathrm{~A} / \mathrm{V}^{2}, \lambda=0.02 \mathrm{~V}^{-1}, t_{o x}=80 \AA, \phi_{f}=0.3 \mathrm{~V}$, $V_{t 0}=0.6 \mathrm{~V}$ and $N_{A}=5 \times 10^{15} \mathrm{~cm}^{-3}$. Ignore velocity saturation effects.
(a) Sketch the $I_{D s}-V_{D S}$ characteristics for $V_{D S}$ from 0 to 2 V and $\mathrm{V}_{G S}=1 \mathrm{~V}$.
(b) Sketch the Ids $-V_{G S}$ characteristics for $V_{D S}=2 \mathrm{~V}$ as $V_{G}$ varies from 0 to 2 V with $V_{S B}=0$ and 1 V .
(c) Derive and sketch the complete small-signal equivalent circuit for the device with $\mathrm{V}_{\mathrm{GS}}=1 \mathrm{~V}$, $\mathrm{V}_{\mathrm{DS}}=2 \mathrm{~V}$, and $\mathrm{V}_{\mathrm{SB}}=1 \mathrm{~V}$. Use $\psi_{0}=0.7 \mathrm{~V}, C_{s b 0}=C_{d b}=20 \mathrm{fF}$, and $C_{g b}=5 \mathrm{fF}$. Overlap capacitance from gate to source and gate to drain is 2 fF .

## PROBLEM 3 (10pts):

For circuit in Figure 2 sketch the $V o\left(V_{I}\right)$ output characteristic as $V_{I}$ goes from 0 V to $\mathrm{VDD}=2 \mathrm{~V}$. Mark the regions and type of operation for both M1 and M2. Assume $V_{t 1}=V_{t 2}=0.5 \mathrm{~V}$ and $k_{l}=$ $10 k_{2}$. Find $V_{I}$ for which the small-signal gain is the largest.


Figure 2

PROBLEM 4 (10pts):
Derive the expressions for input resistance $R_{\text {in }}$, output resistance $R_{\text {out }}$, voltage gain $A_{v}=v_{\text {out }} / v_{\text {in }}$ as a function of small-signal parameters and given circuit elements for MOS circuit in Figure 3. Assume that all capacitors have infinite values.


Figure 3
PROBLEM 5 (10pts):
Derive the expressions for input resistances $R_{\text {in } 1,2}$, output resistances $R_{\text {out } 1,2,}$, voltage gains $A_{v 1}=$ $v_{\text {out }} / v_{\text {in }}, A_{v 2}=v_{\text {out } 2} / v_{\text {in }}$ as a function of small-signal parameters and given circuit elements for BiC MOS circuit in Figure 4. Assume that all capacitors have infinite values.


Figure 4

## EXTRA PROBLEMS FOR EE 240A STUDENTS:

## PROBLEM 5 (10pts):

Derive the expressions for input resistance $R_{\text {in }}$, output resistance $R_{\text {out }}$, voltage gain $A_{v}=v_{\text {out }} / v_{\text {in }}$ as a function of small-signal parameters and given circuit elements for circuit in Figure 5. Assume that all capacitors have infinite values. Determine the biasing resistor values RE, RB, RC to maximize the output swing and voltage gain. Assume $\beta_{F}=100, I_{C}=1 \mathrm{~mA}, \mathrm{~V}_{\mathrm{A}}=\infty$ and $R_{S}=10 \Omega$.


Figure 5

## PROBLEM 6 (10pts):

Derive the expressions for input resistances $R_{\text {inl } 1,2 \text {, output resistances } R_{o u t l, 2,} \text {, voltage gains } A_{v l}=}=$ $v_{\text {out }} / v_{\text {in }}, A_{v 2}=v_{\text {out }} / v_{\text {in }}$ as a function of small-signal parameters and given circuit elements for circuit in Figure 6. Assume that all capacitors have infinite values.


Figure 6

PROBLEM 7 (10pts):
Determine the small-signal transconductance $i_{3} /\left(v_{2}-v_{1}\right)$ for circuits in Figure 7a,b, as a function of small-signal transistor parameters.

(a)

(b)

Figure 7

