## Homework 5

Due: Friday, 28 February 2014 at 1pm

## This is an individual assignment!

## PROBLEM 1 (10pts):

Fig. 1(A) shows a common source amplifier that is biased using a current mirror. Assume that $R_{B}$ and $\mathrm{C}_{\mathrm{B}}$ have very large values, and that the transistors have the following parameters: $\mathrm{L}=120 \mathrm{~nm}, \mathrm{~V}_{\mathrm{th} 0}=$ $0.5 \mathrm{~V}, \mathrm{k}_{\mathrm{n}}{ }^{\prime}=200 \mu \mathrm{~A} / \mathrm{V}^{2}, \gamma=0$.
Given $\mathrm{V}_{\mathrm{DD}}=1.5 \mathrm{~V}, \mathrm{~W}_{1}=1.92 \mu \mathrm{~m}, \mathrm{I}_{\mathrm{REF}}=100 \mu \mathrm{~A}$, and $\mathrm{R}_{\mathrm{L}}=1 \mathrm{k} \Omega$ :
(a) Assuming $\lambda=0$, size $\mathrm{M}_{2}$ (i.e. find $\mathrm{W}_{2}$ ) so that the amplifier has a mid-band, small-signal voltage gain $v_{d} / v_{i}=5$. What is the bias current $\mathrm{I}_{\mathrm{D} 2}$ in this case?
(b) Keep the same size for M2 that you found in part (a), but now let $\lambda=0.4 \mathrm{~V}^{-1}$. What is the new bias current $\mathrm{I}_{\mathrm{D} 2}$ ? What is the new small-signal voltage gain? Explain the source of mismatch with your results from part (a).
(c) In order to more accurately control the bias current, we could add a cascode device to the amplifier, as shown in Fig. 1(B). Find the bias voltage $\mathrm{V}_{\mathrm{B}}$ that will make the bias current $\mathrm{I}_{\mathrm{D} 2}$ match what was found in part (a) exactly. Assume $(\mathrm{W} / \mathrm{L})_{3}=(\mathrm{W} / \mathrm{L})_{2}$, and $\lambda=0.4 \mathrm{~V}^{-1}$ still.


Figure 1

## PROBLEM 2 (10pts):

Determine the output resistance of the current mirror in Figure 2 as a function of transistor parameters. Neglect the body-effect. Assume that the amplifier in Figure 2 has finite gain $\mathrm{A}=100$ and infinite input resistance. For small-signal analysis assume $\mathrm{v}_{\mathrm{o}}=\mathrm{A}\left(\mathrm{v}_{+}-\mathrm{v}_{-}\right)$. Since gain A is high, for DC analysis assume that $v_{+}=v_{\text {.. If }}$ If the size of transistors $\mathrm{M}_{1-4}$ is $\mathrm{W} / \mathrm{L}$, find the size of $\mathrm{M}_{5}$ that minimizes the systematic gain error. What is the resulting gain error?


Figure 2
PROBLEM 3 (10pts):
Figure 3 depicts a self-biasing $V_{t}$ reference circuit which is capable of providing a current reference independent of biasing voltage.
(a) Provide expressions for the DC output current Iovt and biasing currents IBIASI and IBIAS2 in terms of circuit elements and transistor parameters and calculate numerical values. Ignore body effect and channel length modulation.
(b) Calculate the ratio of small-signal variations in Iout to small-signal variations in $V_{D D}$ at low frequencies. Ignore the body effect but include finite transistor $r_{o}$ in this calculation.
MOS parameters: $\left|V_{t h}\right|=0.5 \mathrm{~V}, k_{n}{ }^{\prime}=200 \mu \mathrm{~A} / \mathrm{V}_{2}, k_{p}{ }^{\prime}=100 \mu \mathrm{~A} / \mathrm{V}_{2}, \lambda=0.05 \mathrm{~V}_{-1}, V_{D D}=3 \mathrm{~V}, R=1.75 \mathrm{k} \Omega$,
$(W / L) \_=12.5 \mu \mathrm{~m} / 0.25 \mu \mathrm{~m},(W / L) 2=6.25 \mu \mathrm{~m} / 0.25 \mu \mathrm{~m},(W / L) 3=31.25 \mu \mathrm{~m} / 0.25 \mu \mathrm{~m}$,
$(W / L) 4=6.25 \mu \mathrm{~m} / 0.25 \mu \mathrm{~m},(W / L) 5=12.5 \mu \mathrm{~m} / 0.25 \mu \mathrm{~m},(W / L) 6=15.5 \mu \mathrm{~m} / 0.25 \mu \mathrm{~m}$.


Figure 3

## EXTRA PROBLEMS FOR EE 240A STUDENTS: <br> PROBLEM 4 (10pts):

A band-gap reference circuit is shown in Fig. 4. Assume that $\beta_{\mathrm{F}} \rightarrow \infty$, VA $\rightarrow \infty, \mathrm{I}_{\mathrm{S} 1}=1 \times 10^{-15} \mathrm{~A}$, and $\mathrm{I}_{\mathrm{S} 2}=8 \times 10^{-15} \mathrm{~A}$. Assume the op-amp is ideal except for a possibly nonzero offset voltage $\mathrm{V}_{\mathrm{OS}}$, which is modeled by a voltage source in Fig. 4.
(a) Suppose that $\mathrm{R}_{2}$ is trimmed to set Vout equal to the target voltage for which dV out $/ \mathrm{dT}=0$ at $\mathrm{T}=25^{\circ} \mathrm{C}$ when $\mathrm{V}_{\text {OS }}=0$. Find dV Out $/ \mathrm{dT}$ at $\mathrm{T}=25^{\circ} \mathrm{C}$ when $\mathrm{V}_{\mathrm{OS}}=30 \mathrm{mV}$.
(b) Under the conditions in part (a), is $\mathrm{d}^{\mathrm{OUUT}} / \mathrm{dT}$ positive or negative? Explain.


Figure 4

## PROBLEM 5 (10pts):

For the bias circuit shown in Figure 5:
a) Determine the bias current. Assume $\left|V_{t h}\right|=0.5 \mathrm{~V}, \mathrm{k}_{\mathrm{n}}{ }^{\prime}=200 \mu \mathrm{~A} / \mathrm{V}^{2}, \mathrm{k}_{\mathrm{p}}{ }^{\prime}=200 \mu \mathrm{~A} / \mathrm{V}^{2}$. Neglect base currents and the body effect.
b) Derive the expression for the temperature dependence of the bias current.
c) Derive the expression for the supply sensitivity of the bias current. Assume $\lambda=0.05 \mathrm{~V}^{-1}$.


Figure 5

