Homework Assignment \#1
Due by online submission very very late Monday night 1/22/2018 (Tuesday at 9am)

1. In the figure below, there are four identical three terminal devices. These devices all have the property that the current from $C$ to $A$ is a strong function of the voltage from $B$ to $A$, and a weak function of the voltage from $C$ to $A$. There is negligible current into node $B$. If the voltage from $B$ to $A$ is less than $V_{X}$, that the current is zero. If the voltage from $B$ to $A$ is more than $V_{X}=$ $\mathrm{V}_{\mathrm{big}} / 10$, the current goes up really fast. The voltage from C to A doesn't have much effect, as long as it is greater than 0 , but if it is 0 or less, the current is 0 . (note: seen from far away, this describes JFETs, BJTs, Darlingtons, MOSFETs, MESFETs, vacuum tubes, IGBTs, HEMTs, and virtually every other three terminal electronic device ever made)

a. sketch the voltage on out1 as the voltage on in varies from 0 to $\mathrm{V}_{\text {big. }}$
b. when the voltage on out1 is Vbig/2, write an expression for the voltage gain using the derivative of the current with respect to Vin.
c. sketch the voltage on out2 as the voltage on in2 varies from 0 to $\mathrm{V}_{\text {big. }}$.
d. sketch the voltage on tail as the voltage on in3 varies from 0 to $\mathrm{V}_{\mathrm{big}}$.
2. You're standing on a big smooth hillside. Directly North the hill climbs up quite steeply, rising 10 cm for every step you take. Directly East the hill climbs gently, rising only 1 mm for every step you take. You put a stake in the ground where you are standing and call it ( 0,0 ). You measure the elevation to be E. If you want to be 10 steps further north than you currently are, but don't want to change your altitude (current source!)
a. if you walk 10 steps east and put a stake in the ground labeled $(10,0)$, what is your elevation?
b. if you walk 10 steps north from $(0,0)$ and put a stake in the ground labeled $(0,10)$, what is your elevation.
c. how far east do you have to walk in order to stay at the same altitude? (trick question the answer is negative)
d. (note: altitude is current. East/west is drain/source voltage. North/south is gate/source voltage. The first stake is the DC operating point, the origin of the local coordinate systems. Step counts are small signal voltage changes. What is the intrinsic gain?)
e. Do any of the previous answers depend on E, or the GPS location of the stake that you labeled (the specific values of the DC operating point) ?
3. You live in an area with a lot of gold mines. Everyone knows that the amount of gold $G$ that has been extracted from a mine as a function of the total time worked $H$ is given by
$G(H)=G_{\text {total }}(1-\cos (\pi H / T)) / 2$
from the time that people first start excavating the mine (when $\mathrm{H}=0$ ) until the time that all of the gold is gone, $H=T$. If you only get to work for one hour in the mine, does it matter if you work at the beginning, vs. the middle or the end? When should you work to mine the most gold? How much will you get? If $T=100 y e a r s$, and you start working at $H=T / 4$ and work for a year, does your gold mining rate change much from month to month?
(This is about linearization. You get more bang for your buck (more $g_{m}$ per $\mu \mathrm{A}$ ) with transistors that are biased just right. There's a low bias where you get nothing, a high bias where everything is maxed out, and a sweet spot somewhere in the middle.)
4. Graph the magnitude of the impedance of the following elements and circuits by hand. Use a $\log / \log$ scale, with the frequency axis varying from 1 to $10^{11} \mathrm{rad} / \mathrm{sec}$, and impedance axis varying from $1 \Omega$ to $10 \mathrm{G} \Omega$.
a. Resistors of magnitude $1 \mathrm{k} \Omega, 1 \mathrm{M} \Omega, 1 \mathrm{G} \Omega$ and capacitors of $1 \mathrm{nF}, 1 \mathrm{pF}$, and 1 fF ; and inductors of magnitude $1 \mathrm{mH}, 1 \mathrm{uH}, 1 \mathrm{nH}$ (all 9 of these components should be on the same plot; the next three should be together on a separate plot)
b. The series combination of $1 \mathrm{M} \Omega$ and 100 fF
c. The parallel combination of $1 \mathrm{M} \Omega$ and 100 fF
d. The series combination of $10 \Omega$ and 10 nH (real inductors always have series resistance)
5. [ee240A] Use matlab or something equivalent to plot some 3D surfaces of current vs. control and output voltages for several of the types of 3 terminal devices listed above, preferably showing constant-current projections onto the XY plane. Comment on the gain vs. bias point.
