

EE16 A Gireeja Ranade

Discussion Poll + Rebalancing.

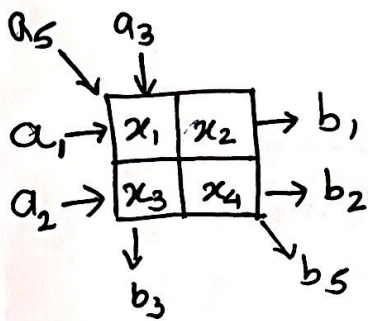
HWO due yesterday.

Self-grades due tonight

HW1 due Friday midnight

HW Party tomorrow.

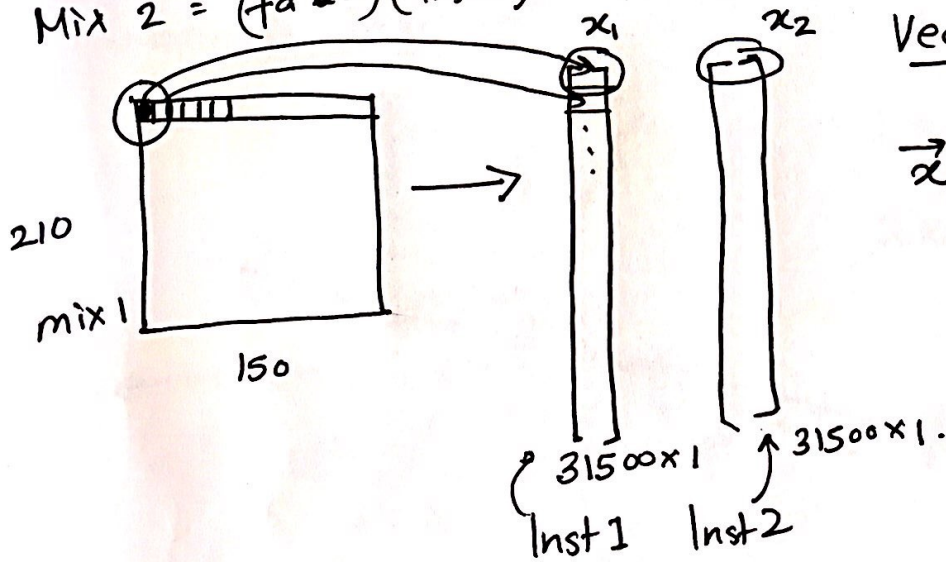
Today: Gaussian Elimination & Systems of Linear Equations.



$$\begin{aligned} a_1 x_1 + a_2 x_2 &= b_1 \\ a_3 x_1 + a_4 x_2 &= b_2 \\ a_5 x_1 &= b_3 \end{aligned}$$

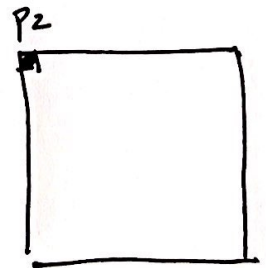
$$\text{Mix 1} = (f_{1a})(\text{Inst 1}) + (f_{2a})(\text{Inst 2})$$

$$\text{Mix 2} = (f_{1b})(\text{Inst 1}) + (f_{2b})(\text{Inst 2})$$



Vector: Ordered list of numbers.

$$\vec{x} = \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix}$$



$$P_1 = (f_{1a}) \cdot x_1 + (f_{2a}) \cdot x_2$$

$$P_2 = (f_{1b}) \cdot x_1 + (f_{2b}) \cdot x_2$$

Gaussian Elimination.

$$\begin{aligned}x + 4y &= 6 & (E1) \\2x - y &= 3 & (E2).\end{aligned}$$

$$(E2) - 2 \cdot (E1)$$

$$2x - y - 2x - 8y = 3 - 12 = -9$$

$$-9y = -9$$

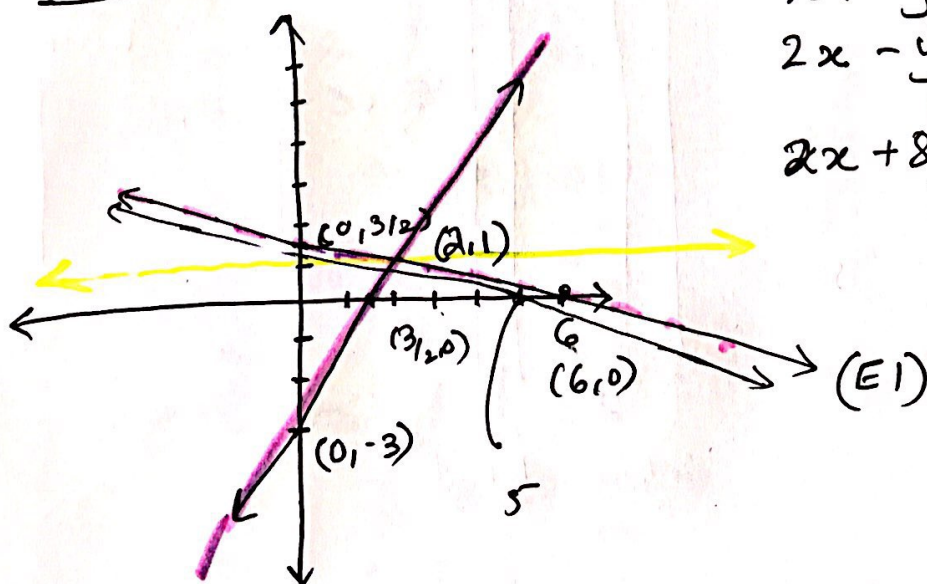
$$\boxed{y = 1}$$

Gaussian Elimination.

$$\begin{bmatrix} 1 & 4 \\ 2 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 6 \\ 3 \end{bmatrix}$$

matrix vector vector.

Geometric Perspective



$$\begin{aligned}x + 4y &= 6 & (E1) \\2x - y &= 3 & (E2) \\2x + 8y &= 12 & (E3)\end{aligned}$$

$$\left[\begin{array}{cc|c} 1 & 4 & 6 \\ 2 & -1 & 3 \end{array} \right]$$

'Augmented matrix'

↓ R2 - 2(R1)

$$\left[\begin{array}{cc|c} 1 & 4 & 6 \\ 0 & -9 & -9 \end{array} \right]$$

Upper triangular matrix.

$$2y + z = 1 \quad (E1)$$

$$2x + 6y + 4z = 10 \quad (E2)$$

$$x - 3y + 3z = 14 \quad (E3).$$

Goal! Make UT.

$$\left[\begin{array}{ccc|c} 0 & 2 & 1 & 1 \\ 2 & 6 & 4 & 10 \\ 1 & -3 & 3 & 14 \end{array} \right]$$

Strategy: Use (E1) to eliminate variables from (E2), (E3).

↕ SWAP (R2) ↔ (R1).

$$\left[\begin{array}{ccc|c} 2 & 6 & 4 & 10 \\ 0 & 2 & 1 & 1 \\ 1 & -3 & 3 & 14 \end{array} \right]$$

↕ Divide (R1) by 2.

$$\left[\begin{array}{ccc|c} 1 & 3 & 2 & 5 \\ 0 & 2 & 1 & 1 \\ 1 & -3 & 3 & 14 \end{array} \right]$$

↕ (R3) - (R1)

$$\left[\begin{array}{ccc|c} 1 & 3 & 2 & 5 \\ 0 & 2 & 1 & 1 \\ 0 & -6 & 1 & 9 \end{array} \right]$$

↕ $3 \cdot (R2) + (R3)$

$$\left[\begin{array}{ccc|c} 1 & 3 & 2 & 5 \\ 0 & 2 & 1 & 1 \\ 0 & 0 & 4 & 12 \end{array} \right]$$

$$x = 2$$

$$2y + 3 = 1, \quad y = -1$$

$$z = 3.$$

① Multiply by scalar

② Swapping

③ Adding a scalar multiple of one row to another.

$$x + 4y = 6 \quad (E1)$$
$$2x + 8y = 12 \quad (E3).$$

$$\left[\begin{array}{cc|c} 1 & 4 & 6 \\ 2 & 8 & 12 \end{array} \right]$$

↓

$$\left[\begin{array}{cc|c} 1 & 4 & 6 \\ \blacksquare & 0 & 0 \end{array} \right]$$

↑ Pivot

WARNING.

$$x + 4y = 6 \quad (E1)$$
$$2x + 8y = 10 \quad (E4).$$

$$\left[\begin{array}{cc|c} 1 & 4 & 6 \\ 2 & 8 & 10 \end{array} \right]$$

↓

$$\left[\begin{array}{cc|c} 1 & 4 & 6 \\ \hline 0 & 0 & -2 \end{array} \right]$$