

Principles of MRI

EE225E / BIO265

Lecture 17

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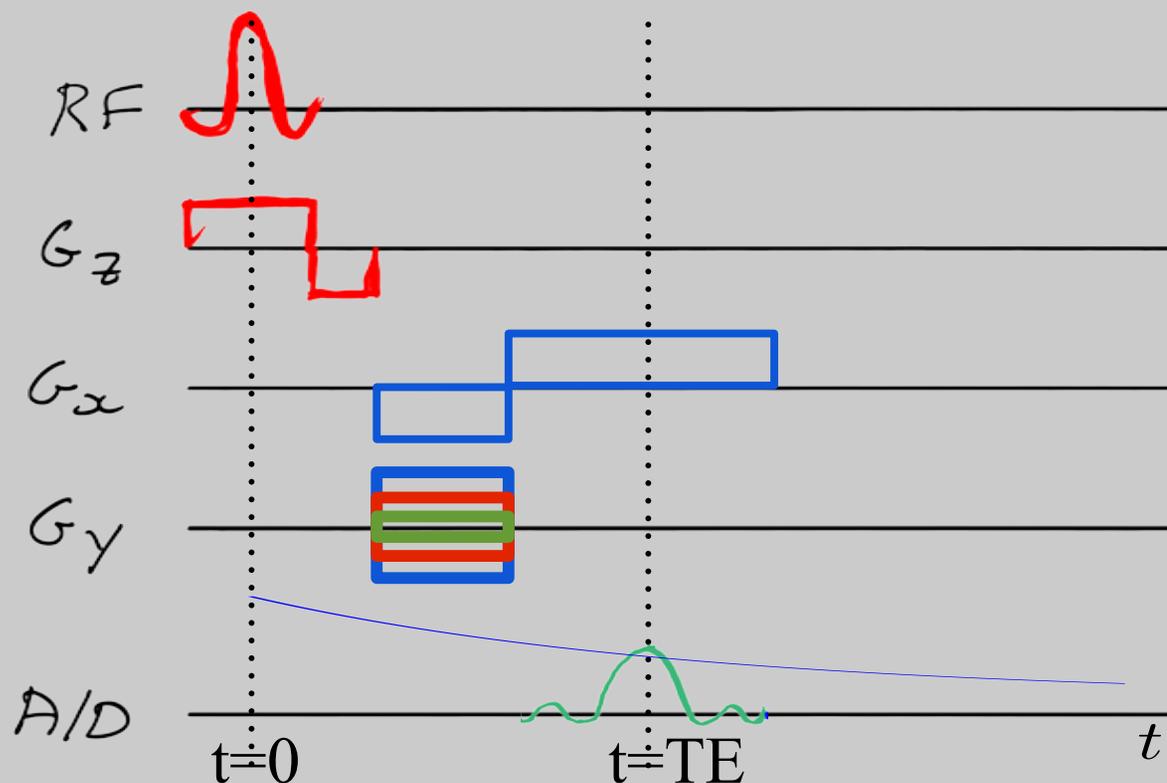
Next:

- Practical Issues in MRI
- T_2 decay
 - Map decay to k-space
 - result in artifacts
 - Image weighting
 - blurring in the readout
- Off-resonance

Effect of T2 Decay on Imaging

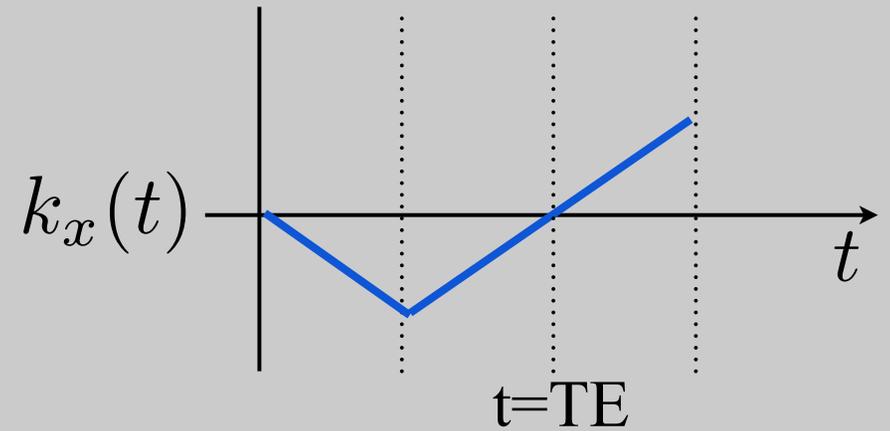
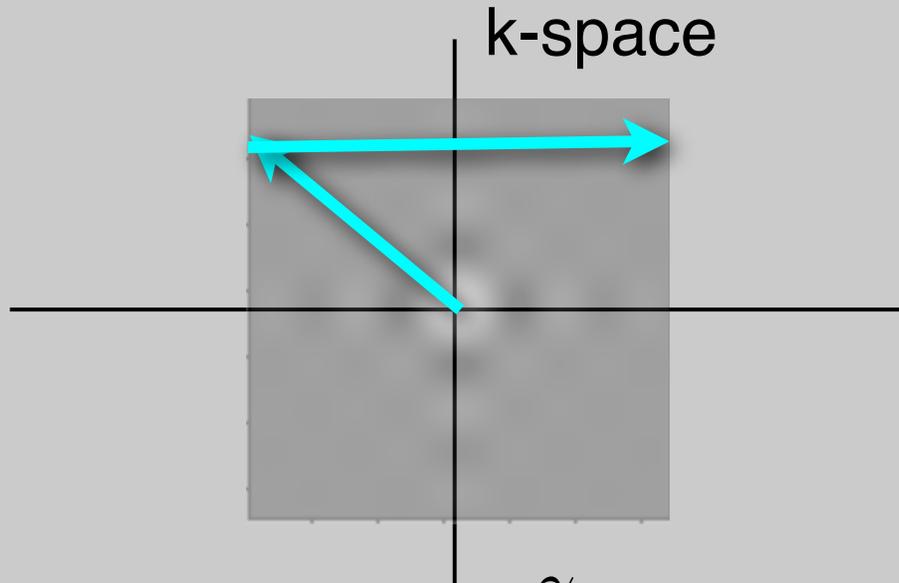
$$s(t) = \int_{\vec{R}} M_{xy}(\vec{r}, 0) e^{-\frac{t}{T_2}} e^{-i2\pi\vec{k}(t)\cdot\vec{r}} d\vec{r}$$

- Signal decays along k-space trajectory



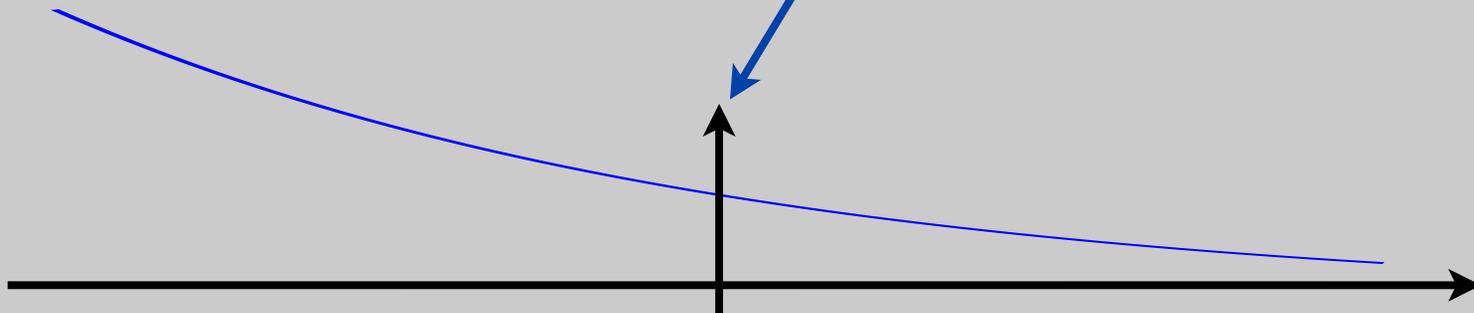
Approximation:
Mxy created mid-RF
Decays with T_2 after

Effect of T2 Decay on Imaging



$$k_x = \frac{\gamma}{2\pi} G_x (t - TE) \Rightarrow t = \frac{k_x}{\frac{\gamma}{2\pi} G_x} + TE$$

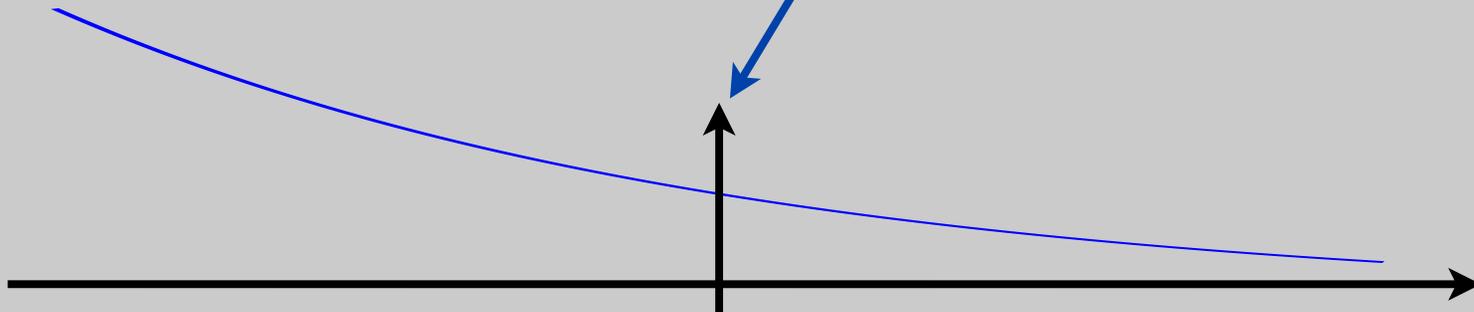
$$e^{-\frac{t}{T_2}} = e^{-\frac{TE}{T_2}} e^{-\frac{k_x}{\frac{\gamma}{2\pi} G_x T_2}}$$



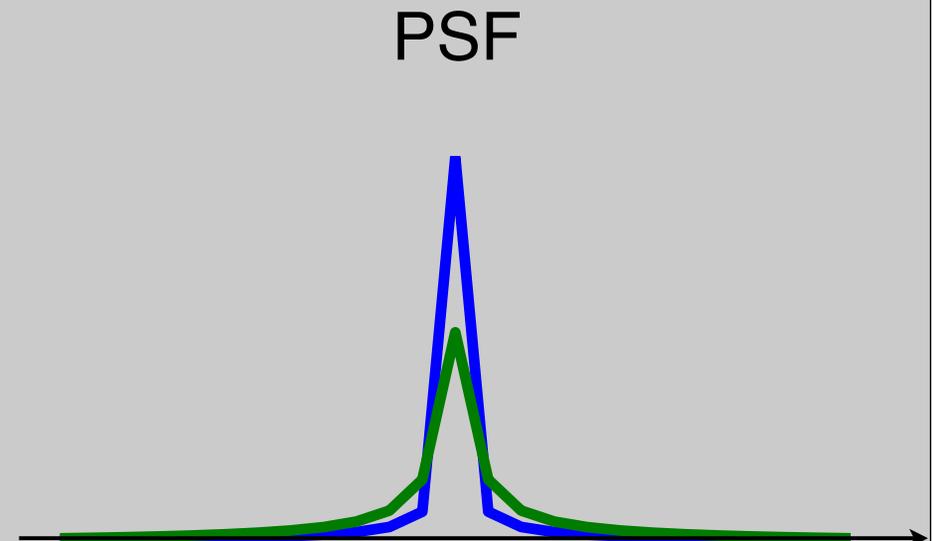
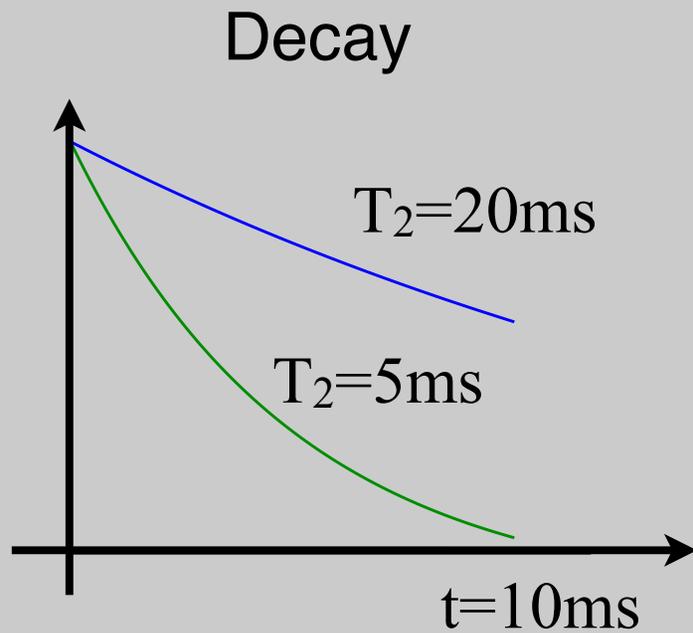
Effect of T2 Decay on Imaging

- Two Effects:
 - Signal Loss by e^{-TE/T_2} (T_2 Weighting)
 - Apodization by $e^{-\frac{k_x}{\frac{\gamma}{2\pi} G_x T_2}}$
 - Blurring in Image Domain (readout direction)
 - Usually minor effect
 - Reduced by increasing G_x

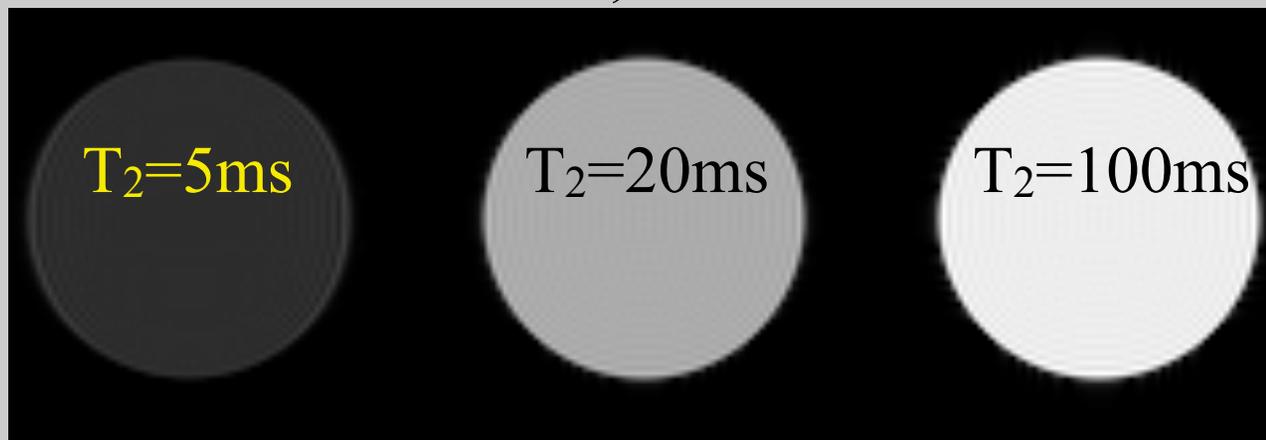
$$e^{-\frac{t}{T_2}} = e^{-\frac{TE}{T_2}} e^{-\frac{k_x}{\frac{\gamma}{2\pi} G_x T_2}}$$



Point Spread Function



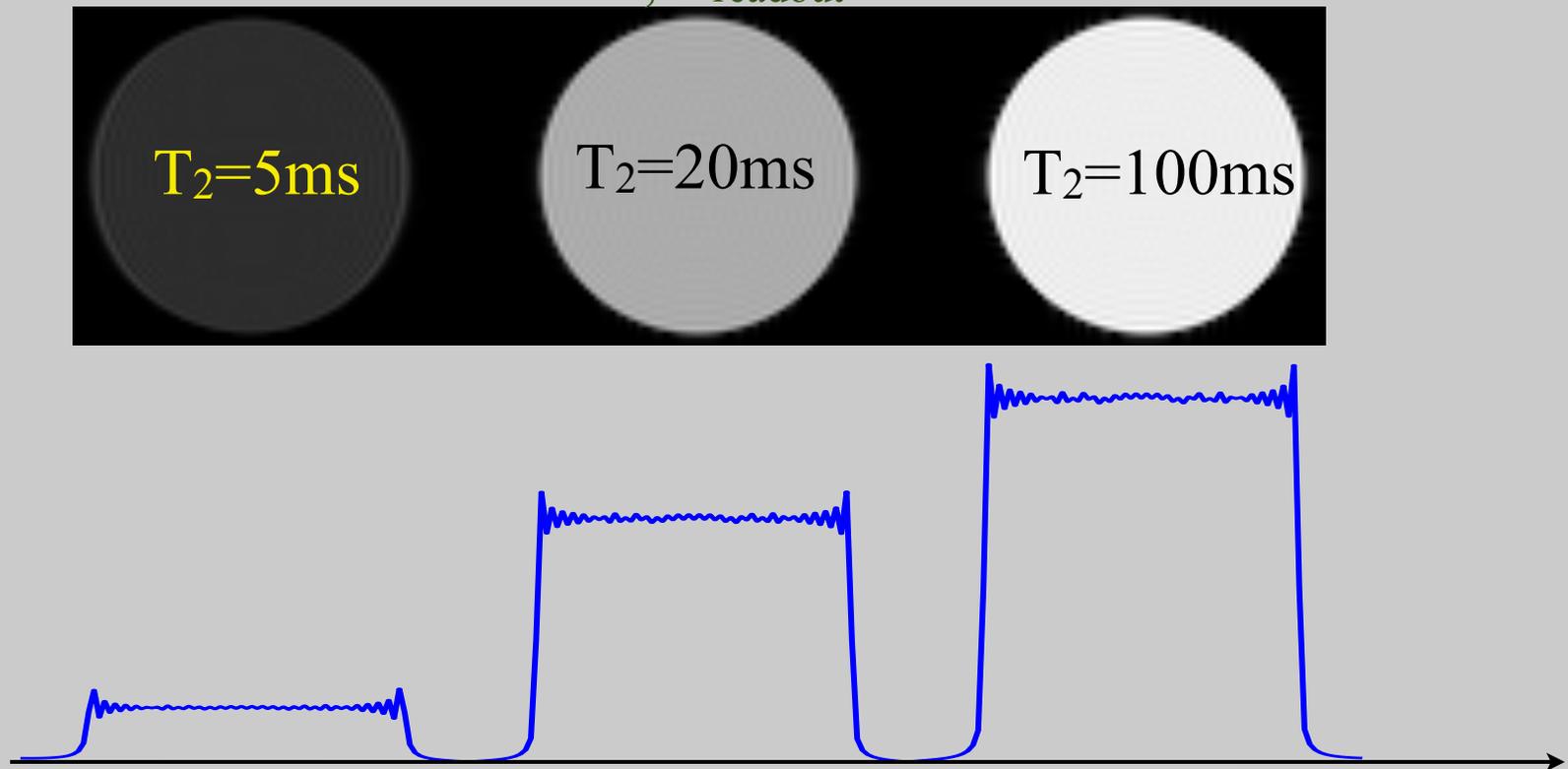
$TE=10\text{ms}$, $T_{\text{readout}}=20\text{ms}$



Effect of T2 Decay on Imaging

- Two effects:
 - Signal loss by $\exp(-TE/T_2)$ (T2 weighting)
 - Apodization - causes blurring in readout

TE=10ms, $T_{\text{readout}}=20\text{ms}$



Off - Resonance

- So far, assumed B_0 constant. But B_0 varies due to:
 - Main field inhomogeneity (~ 1 ppm)
 - Object magnetic susceptibility
 - Chemical shift

Main Field Inhomogeneity

- Magnet is designed to be homogeneous over a (spherical) volume
- Typical numbers:
 - Bare magnet ~10-100 ppm
 - Shimmed magnet ~1 ppm
@3T 1ppm is 127Hz
- Generally, main magnet inhomogeneity is not a limitation

Object Susceptibility

- Most biological objects perturb the field

$$\Delta B_{z,\text{tissue}} \approx \chi B_{0,\text{freespace}}$$

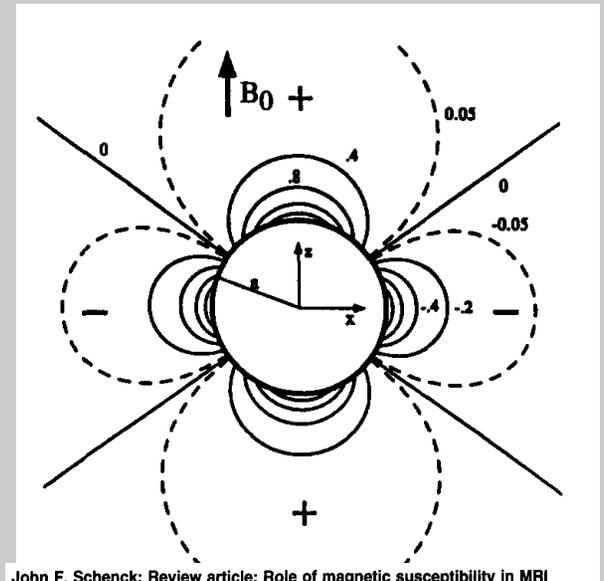
- χ is the magnetic susceptibility
- Larmor frequency lower in tissue than air

$\chi_{\text{water}} = -9.05\text{ppm}$ w.r.t free-space

$\chi_{\text{air}} = 0.36\text{ ppm}$ w.r.t free-space

for a sphere:

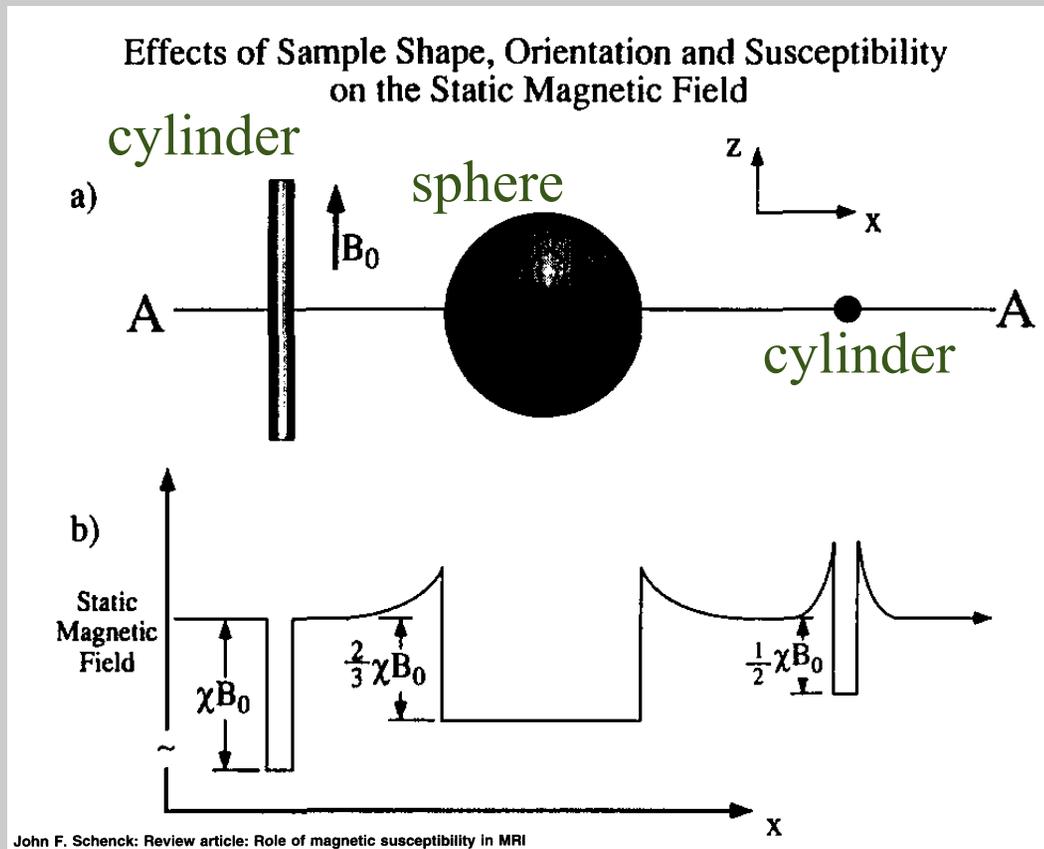
$$\Delta B_z = \frac{\Delta\chi B_0}{3} \left(\frac{a}{r}\right)^3 (3 \cos^2 \theta - 1)$$



John F. Schenck: Review article: Role of magnetic susceptibility in MRI

Object Susceptibility

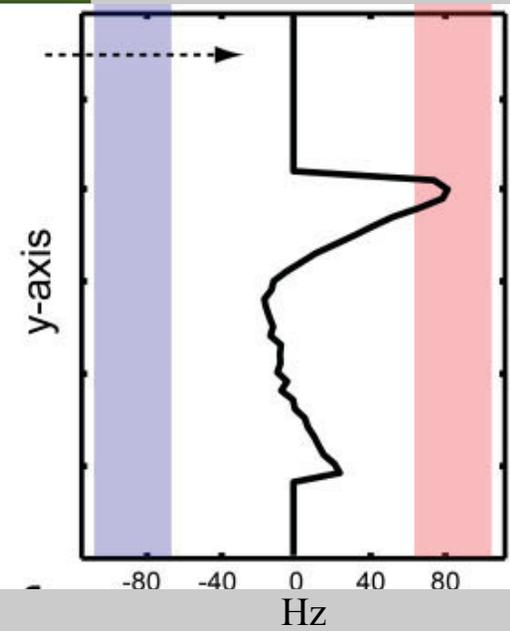
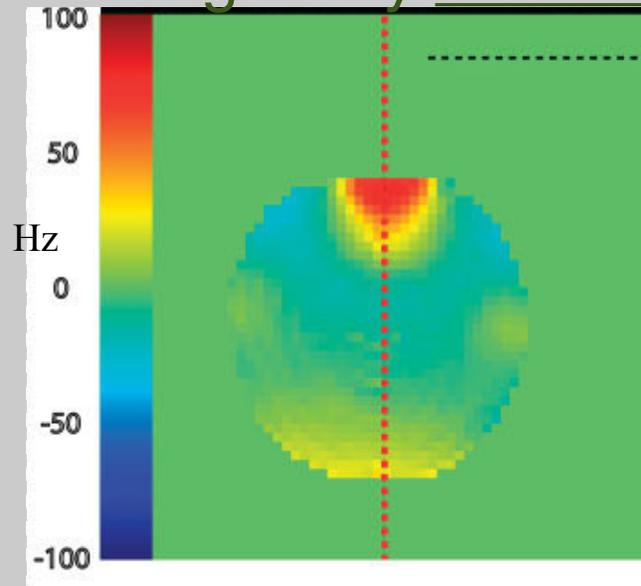
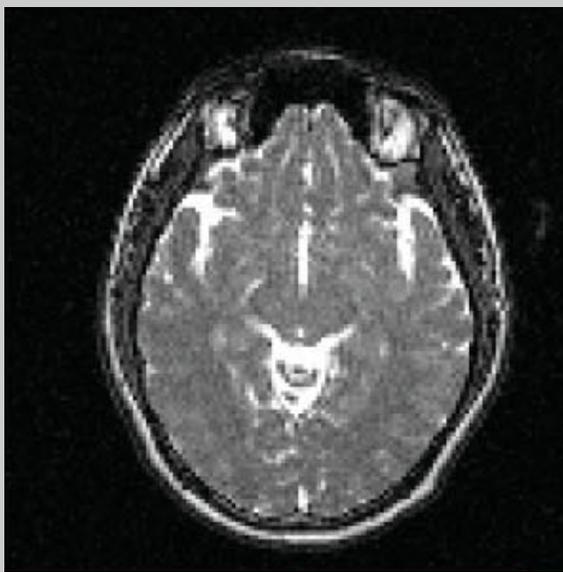
- Complex behavior at boundaries.
 - Depends on $\Delta\chi$ and geometry
 - Typical $\Delta B_0 \pm 3$ ppm ($-12 < \chi < -6$)



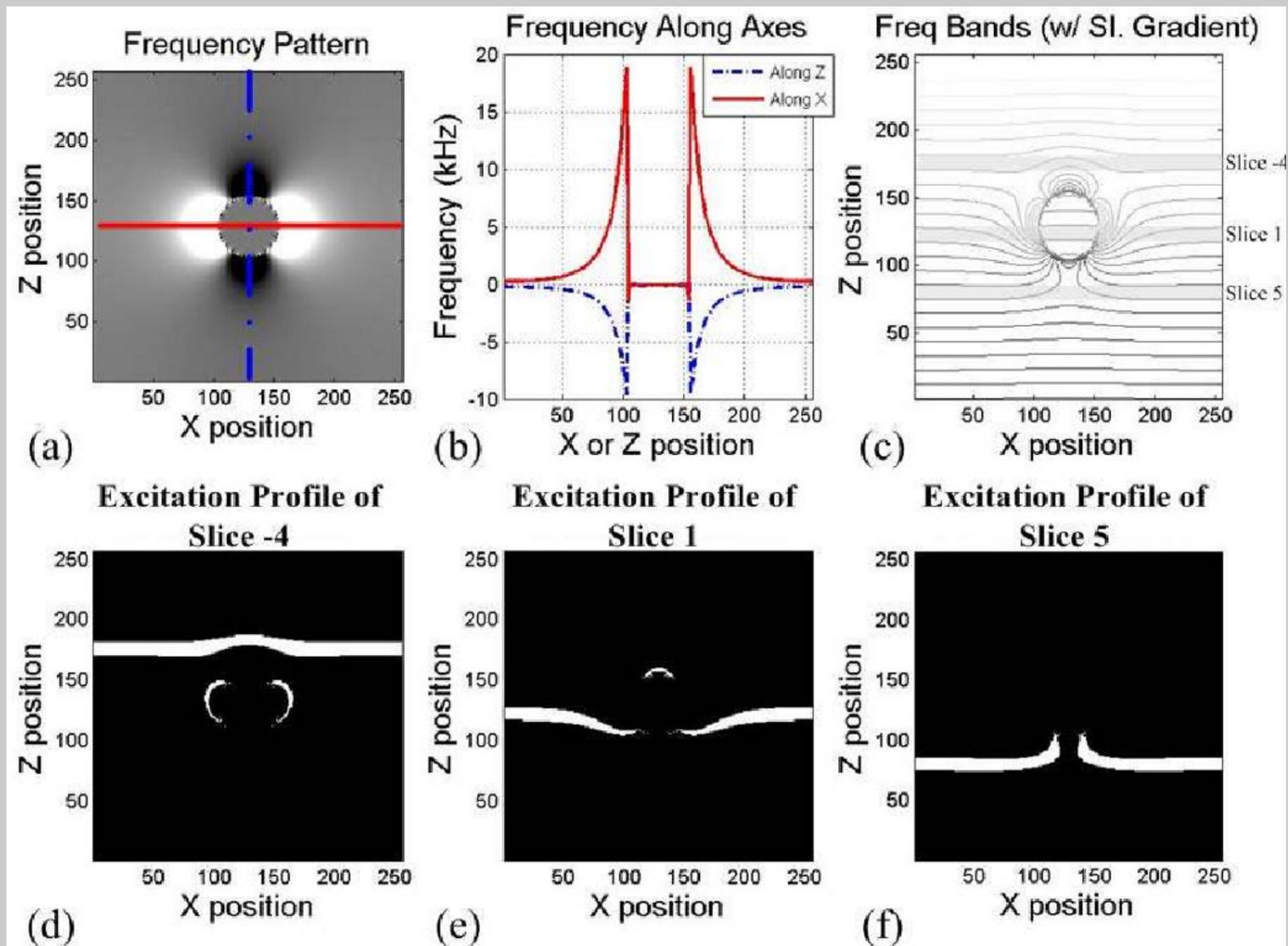
Macroscopic Effect

- Problem areas:
 - Brain above sinuses, auditory canals
 - Heart surrounded by lungs
 - Abdomen

Field inhomogeneity brain@1.5T



Macroscopic Effects - Metal Artifacts



Magn Reson Med. 2009 July ; 62(1): 66–76. doi:10.1002/mrm.21967.

Macroscopic Effects - Metal Artifacts

metal artifact



corrected (SEMAC)



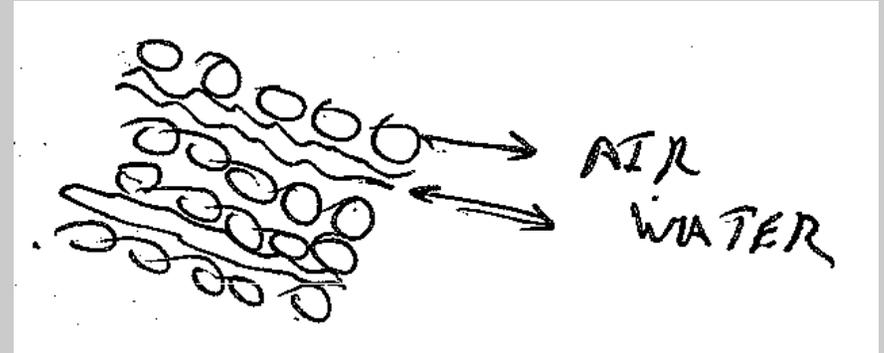
- $\chi_{\text{titanium}} = 182$
- $\chi_{\text{stainless steel (nonmagnetic)}} = 3520-6700$

could be a project...

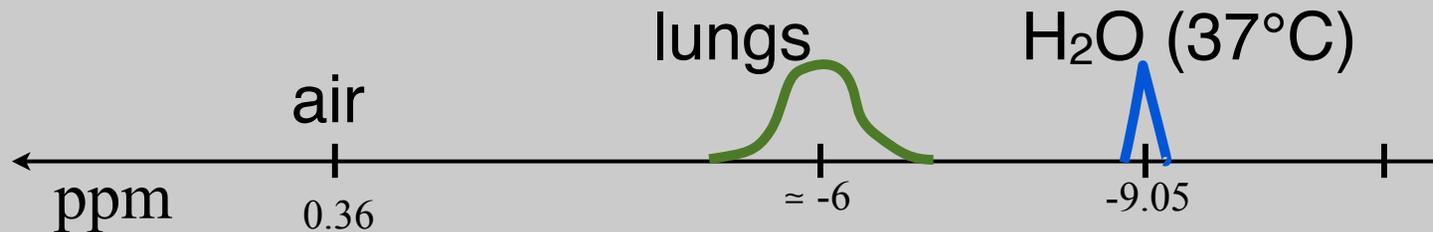
Magn Reson Med. 2009 July ; 62(1): 66–76. doi:10.1002/mrm.21967.

Microscopic Effects

- Lungs:
 - Approx: 1/6 tissue, 5/6 air



- Result:
 - Distribution of field/frequencies



- Tells a lot about microstructure of tissue

Blood

- +Water $\chi=-9.05$
- +Hemoglobin molecule (deoxy) $\chi=0.15$
- +Red Blood cells (deoxy) $\chi=-6.52$
- *Deoxy blood $\chi=-8.77$
- *Oxy blood $\chi=-9.05$

*Magnetic Resonance in Medicine 68:863–867 (2012)

+ **John F. Schenck: Review article: Role of magnetic susceptibility in MRI**

Chemical Shift

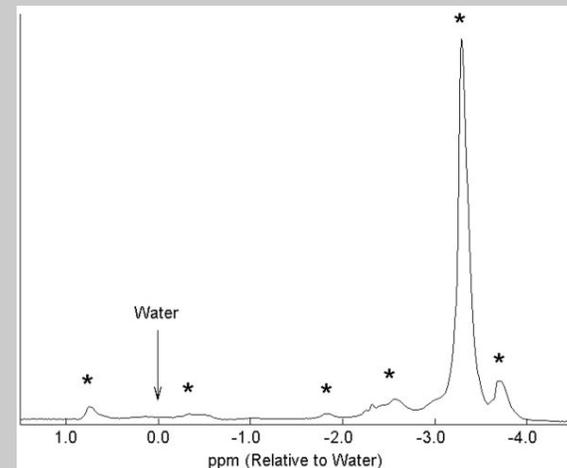
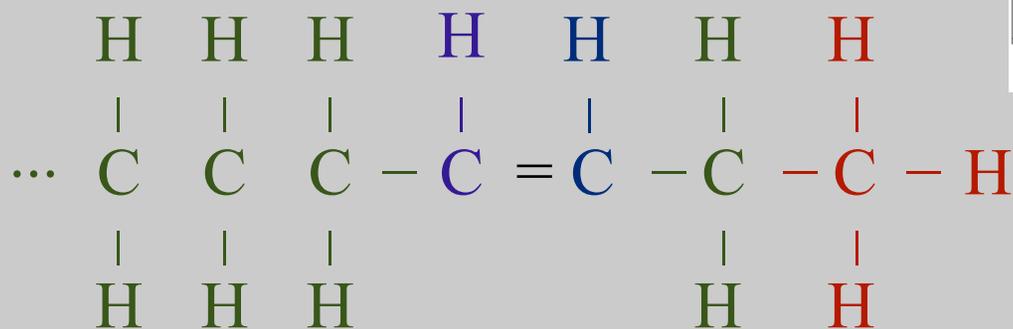
- Protons in complex molecules are “shimmed” by adjacent spins and electrons

$$B_{\text{CS}} = B_0(1 - \sigma)$$

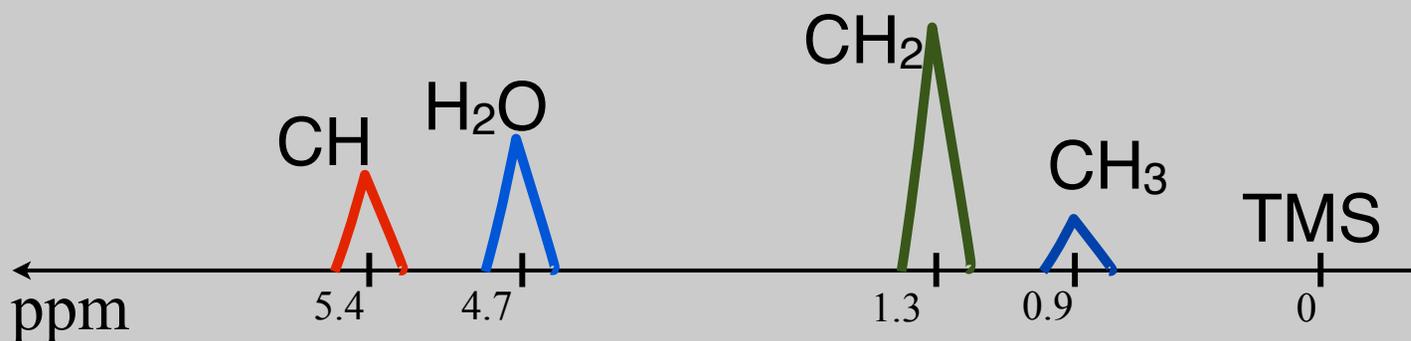
- σ is a shielding constant - depends on molecular structure
- Example: Lipids

Chemical Shift

- Example: Lipids



[J Magn Reson Imaging. 2009 June; 29\(6\): 1332-1339.](#)



Lipids from CH₂ is 3.4ppm below water
@3T \approx 440 Hz

Heterogeneous Tissue

- Tissue is a combination of
 - Chemical shift
 - Susceptibility
 - Geometry
- Results are complex
 - Interesting cases:
 - Blood (fMRI)
 - Lungs
 - Trabecular bone
 - Iron in brain / liver

Effect on Imaging

- Magnitude
 - Phase
 - Geometric
 - Blurring
-
- All depend on spatial scale we look at and acquisition strategy