

(a)

(1) $L = 100 \mu\text{m}$, $W = 1 \mu\text{m}$, $\Gamma = 1\%$, $\lambda = 1 \mu\text{m}$
 $t = 10 \text{ nm}$
 $R_1 = 100\%$, $R_2 = 50\%$, $n_{\text{eff}} = 3$
 $\alpha_i = 10 \text{ cm}^{-1}$

$$\alpha_m = \frac{1}{2L} \ln \frac{1}{R_1 R_2} = 34.6 \text{ cm}^{-1}$$

$$g_{\text{th}} = \frac{1}{\Gamma} (\alpha_i + \alpha_m) = 4460 \text{ cm}^{-1}$$

(b)

$$\tau_p = \frac{1}{v_g \alpha}$$

$$v_g = \frac{c}{n_{\text{eff}}} = 10^{10} \text{ cm/sec}$$

$$\alpha = \alpha_i + \alpha_m$$

$$\tau_p = 2.2 \text{ ps}$$

(c) $Q = \omega \tau = \left(2\pi \frac{c}{\lambda} \right) \left(\frac{n_{\text{eff}}}{c \cdot \alpha} \right) = \frac{2\pi n_{\text{eff}}}{\lambda \alpha}$
 $= 4224$

(d) $\eta = \frac{\alpha_m}{\alpha_i + \alpha_m} = \frac{34.6}{44.6} = 77.6\%$

$$R = \eta \frac{h\nu}{q} = 0.96 \text{ W/A}$$

$$h\nu \cong E_g = \frac{1.24}{\lambda} = 1.24 \text{ eV}$$

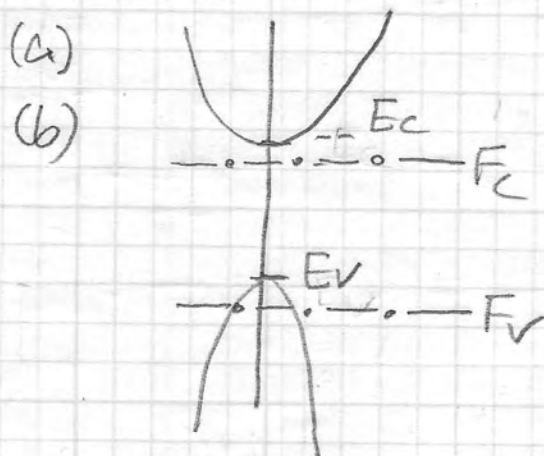
(e) $g(N) = g_0 \ln \left(\frac{N}{N_{\text{tr}}} \right)$, $g_0 = 5000 \text{ cm}^{-1}$

$$N = N_{\text{tr}} e^{\frac{g_{\text{th}}}{g_0}} = 10^{18} \times 2.4 = 2.4 \times 10^{18} \text{ cm}^{-3}$$

$$I_{\text{th}} = \frac{qN}{L} \cdot t \cdot L \cdot W = 0.38 \text{ mA}$$

$$2. m_e^* = 0.2 m_0 \quad L_z = 10 \text{ nm}$$

$$m_h^* = 0.1 m_0$$



(c) Let $\Delta = \frac{E_c - F_c}{k_B T}$

$$N_c^{2d} e^{-\Delta} = N_v^{2d} \Delta$$

$$e^{-\Delta} \approx 1 - \Delta = \frac{m_h^*}{m_e^*} \Delta = \frac{1}{2} \Delta$$

$$\Rightarrow \Delta = \frac{2}{3}$$

$$\Rightarrow E_c - F_c = \frac{2}{3} \times 26 \text{ meV} = 17.3 \text{ meV}$$

(d)
$$N_{tr} = N_v^{2d} \Delta = \frac{m_h^* k_B T}{\pi \hbar^2 L_z} \Delta$$

$$= 0.1 N_0^{2d} \Delta$$

$$= 0.1 \times 10^{19} \times 0.67 = 6.7 \times 10^{17} \text{ cm}^{-3}$$

$$3. (a) E_{e1} = \frac{\hbar^2}{2m_e^*} \left(\frac{\pi}{L_z}\right)^2 = \left(\frac{m_0}{m_e^*}\right) \cdot E_0, \quad E_0 = \frac{\hbar^2}{2m_0} \left(\frac{\pi}{L_z}\right)^2 = 3.7 \text{ meV}$$

$$E_{e2} = 4E_{e1}$$

$$\Delta E_e = E_{e2} - E_{e1} = 3E_{e1} = 3 \times 10 \times 3.7 \text{ meV} = 111 \text{ meV}$$

$$\lambda = \frac{1.24}{0.111} = 11.2 \text{ } \mu\text{m}$$

$$(b) N_{\min} = \rho_e^{2d} \cdot \Delta E_c = \frac{m_e^*}{\pi \hbar^2 L_z} \cdot \frac{\hbar^2}{2m_e^*} \cdot \frac{\pi^2}{L_z^2} \cdot 3 = \frac{3\pi}{2L_z^3} = 4.7 \times 10^{18} \text{ cm}^{-3}$$

$$(c) \Delta E_h = \frac{m_e^*}{m_h^*} \cdot \Delta E_e = \frac{1}{5} \times 111 \text{ meV} = 22.2 \text{ meV}$$

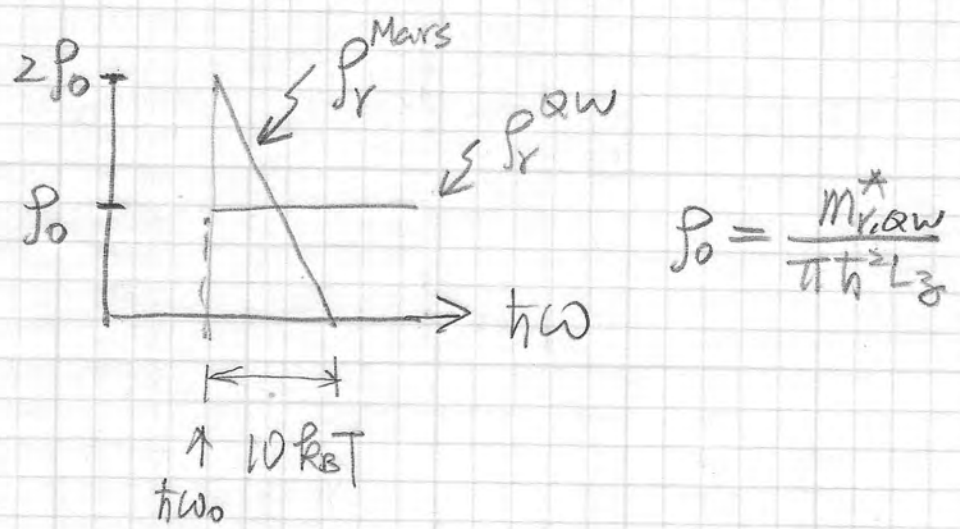
$$\lambda = \frac{1.24}{0.022} = 56 \text{ } \mu\text{m}$$

(d) Peak absorption $\alpha_N \propto \omega_N N_{\min}$
 $\alpha_p \propto \omega_p P_{\min}$

$$N_{\min} = P_{\min} = \frac{3\pi}{2L_z^3}$$

$$\frac{\alpha_N}{\alpha_p} = \frac{\omega_N}{\omega_p} = \frac{\lambda_p}{\lambda_N} = 5 \neq$$

4.



(a)
$$g_{\text{max}}^{qw} = C_0 |\hat{e} \cdot \vec{P}_{qw}|^2 \underset{\substack{\parallel \\ P_0}}{P_r^{qw}}(\hbar\omega_0) \underset{\substack{\parallel \\ 1}}{f_g(\hbar\omega_0)}$$

$$g_{\text{max}}^{Mars} = C_0 |\hat{e} \cdot \vec{P}_{Mars}|^2 \underset{\substack{\parallel \\ 2P_0}}{P_r^{Mars}}(\hbar\omega_0) \underset{\substack{\parallel \\ 1}}{f_g(\hbar\omega_0)}$$

⇒ Mars semiconductor has higher maximum gain.

(b) The peak optical gain always happen at $\hbar\omega = \hbar\omega_0$. For $\Delta F = \hbar\omega_0 + k_B T$, the Fermi Inversion functions above have the same value. Therefore

$$\frac{g_p^{Mars}}{g_p^{qw}} = \frac{P_r^{Mars}(\hbar\omega_0)}{P_r^{qw}(\hbar\omega_0)} = \frac{2P_0}{P_0} = 2 \#$$