

EE C245 - ME C218 Introduction to MEMS Design Fall 2010

Prof. Clark T.-C. Nguyen

Dept. of Electrical Engineering & Computer Sciences
University of California at Berkeley
Berkeley, CA 94720

Lecture Module 8: Microstructural Elements

EE C245: Introduction to MEMS Design

LecM 8

C. Nguyei

9/28/07

UGBerkeley

Outline

- Reading: Senturia, Chpt. 9
- Lecture Topics:
 - ♦ Bending of beams
 - ♥ Cantilever beam under small deflections
 - Combining cantilevers in series and parallel

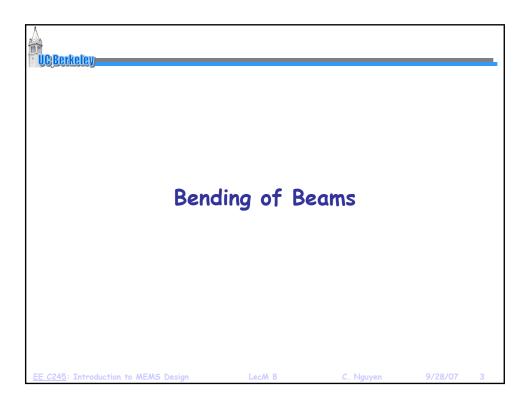
 - ♦ Design implications of residual stress and stress gradients

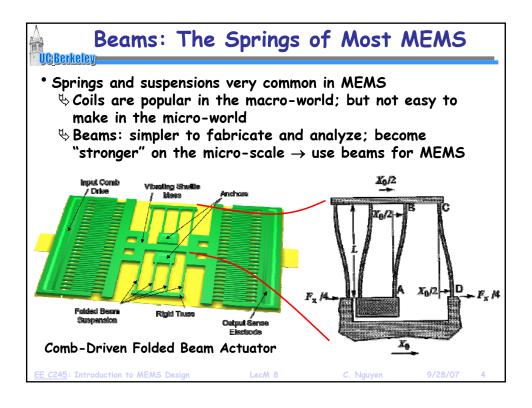
E C245: Introduction to MEMS Design

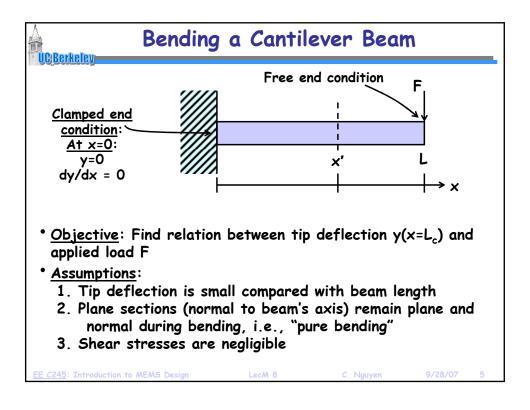
LecM 8

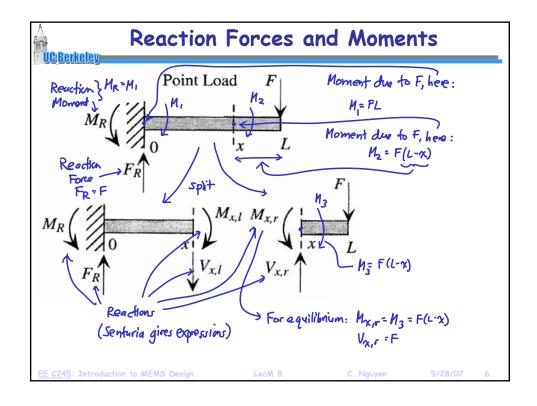
C. Nguyen

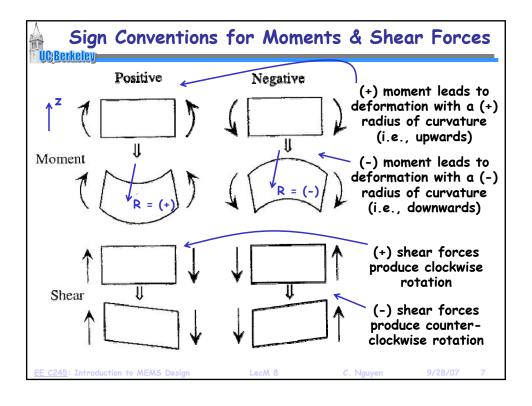
9/28/07

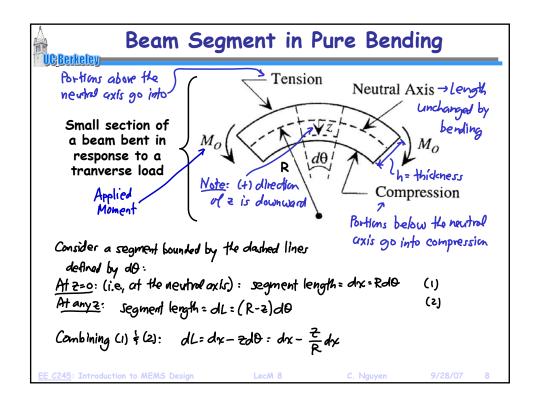


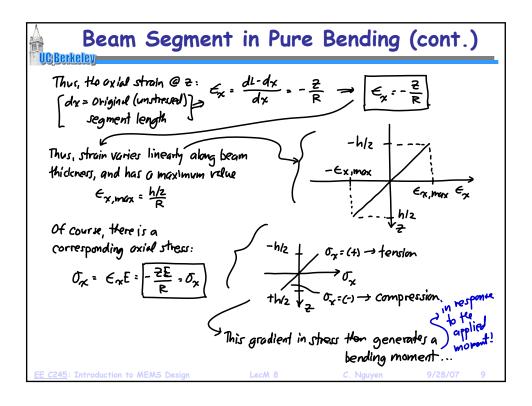


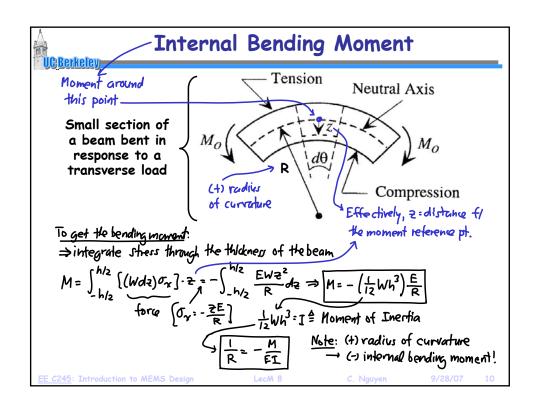


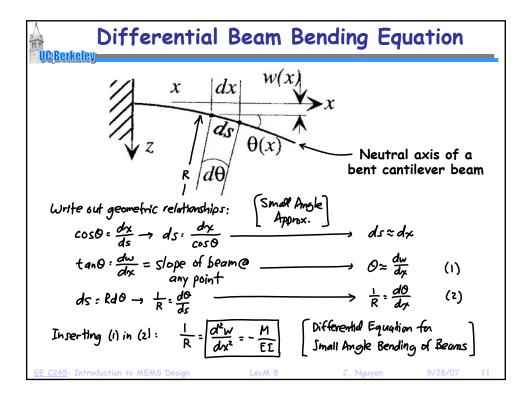


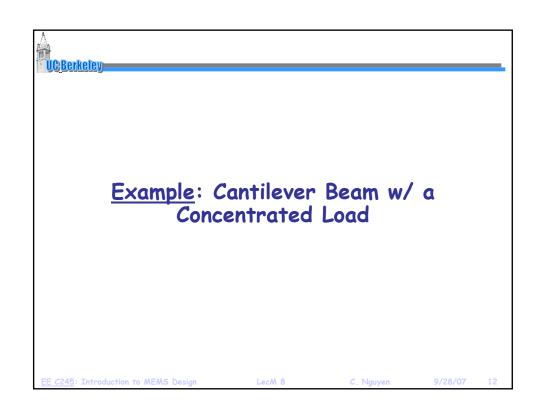


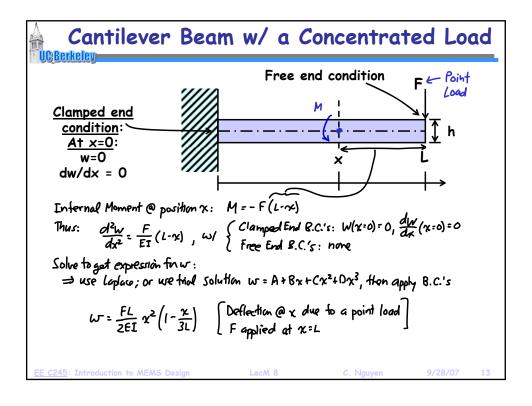


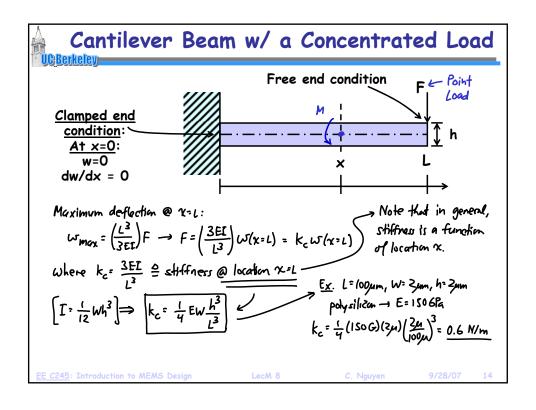


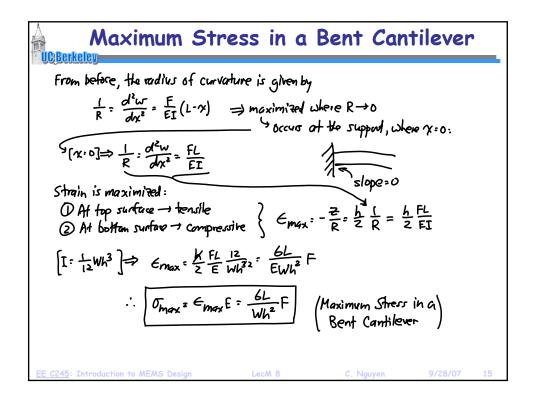


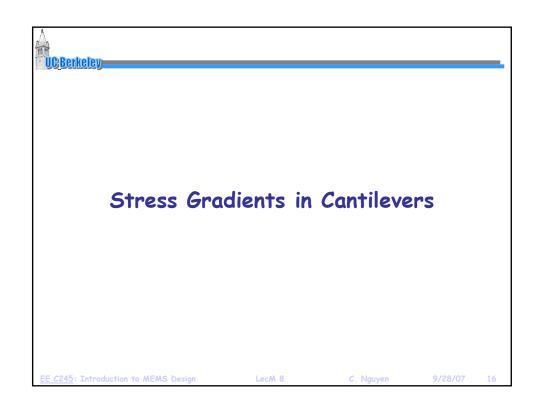


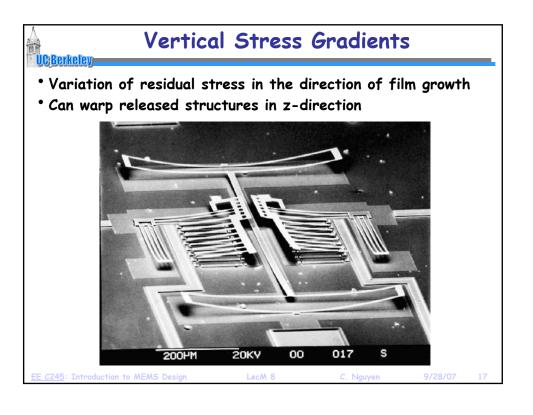


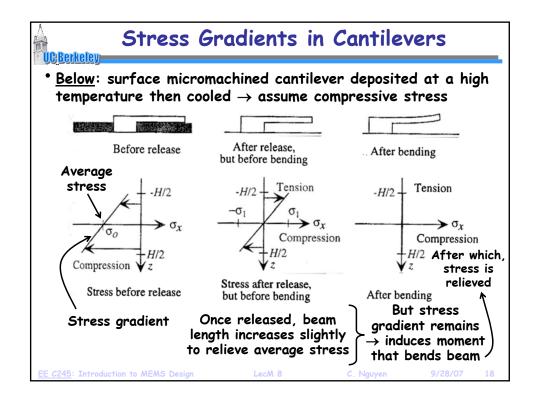


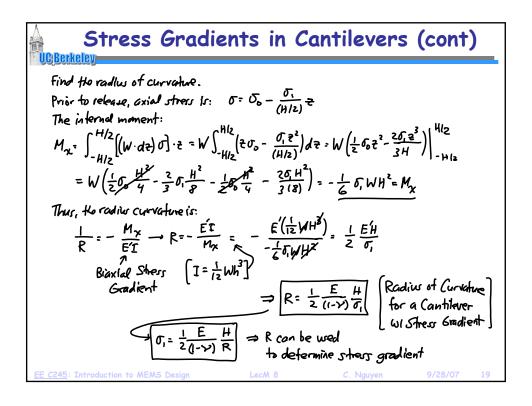


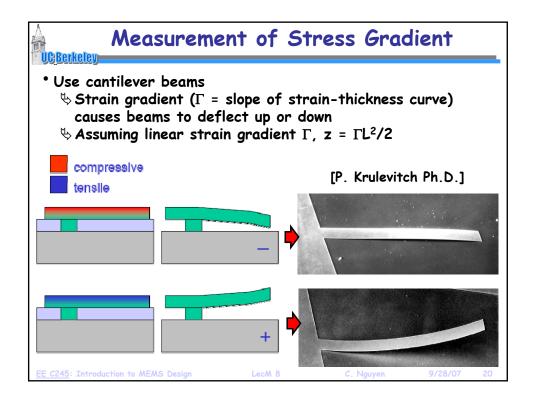


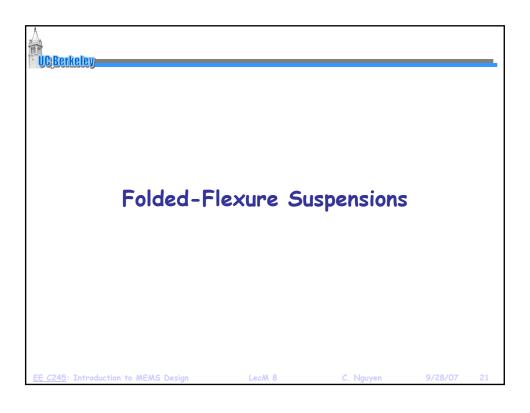


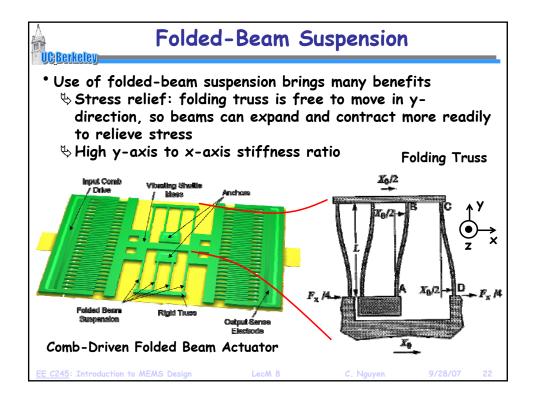


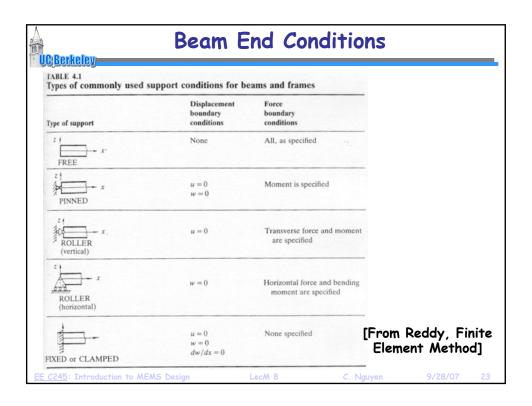


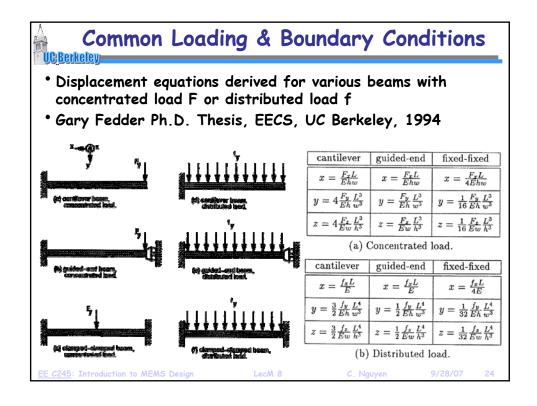


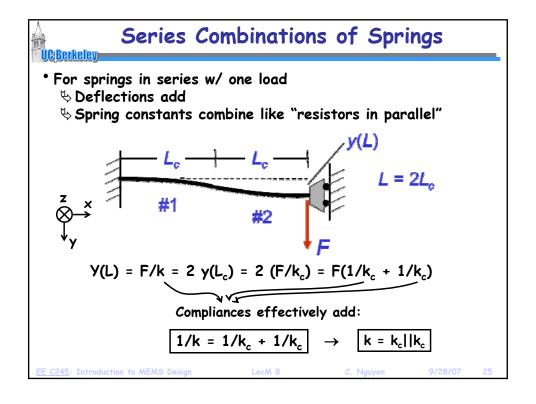


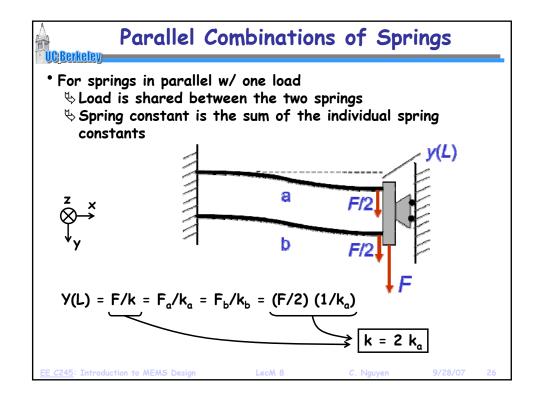


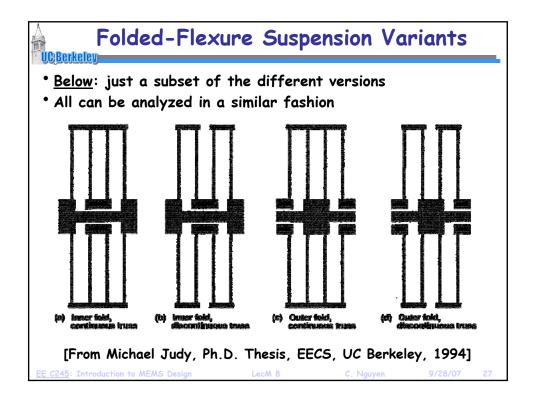


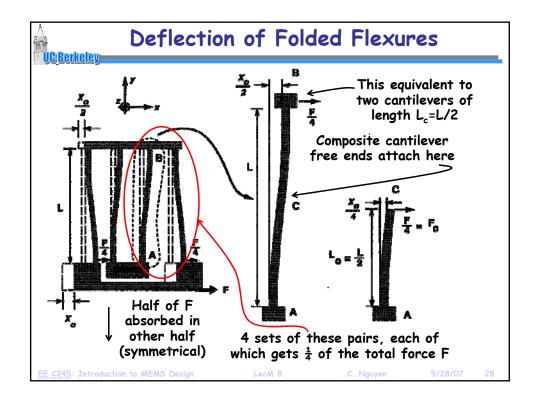


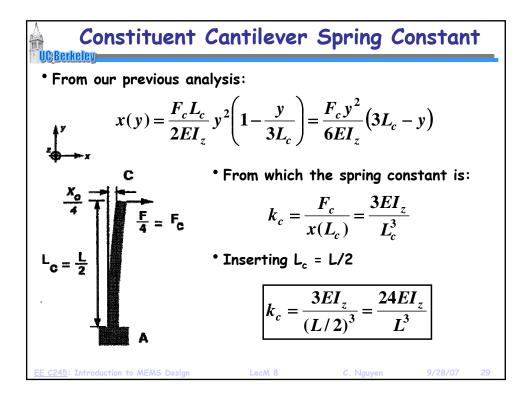


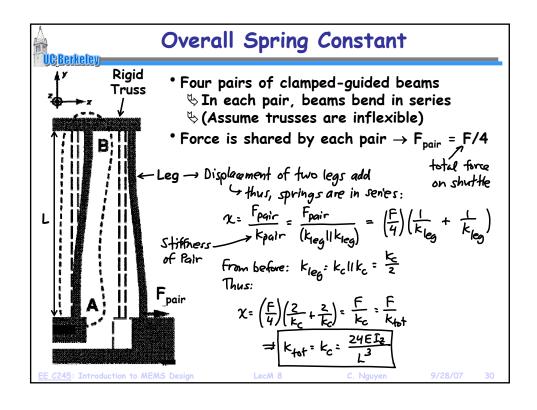


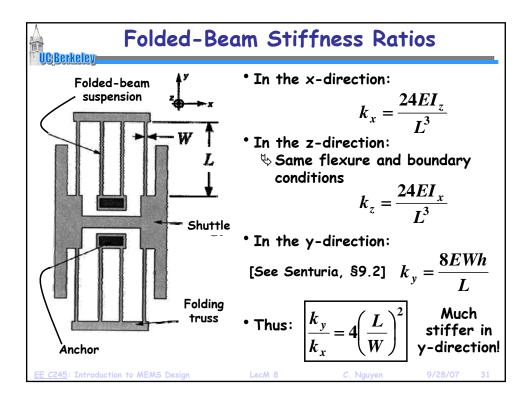


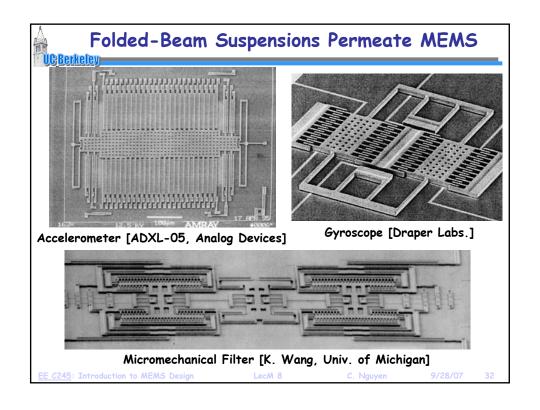


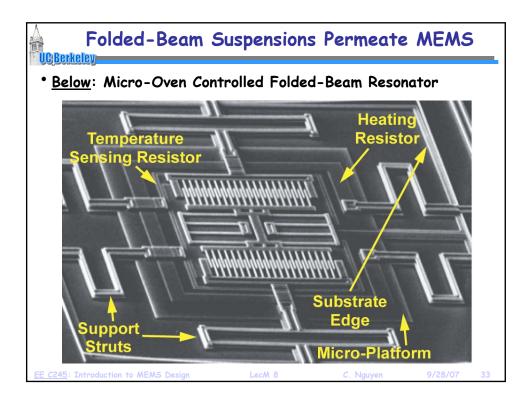


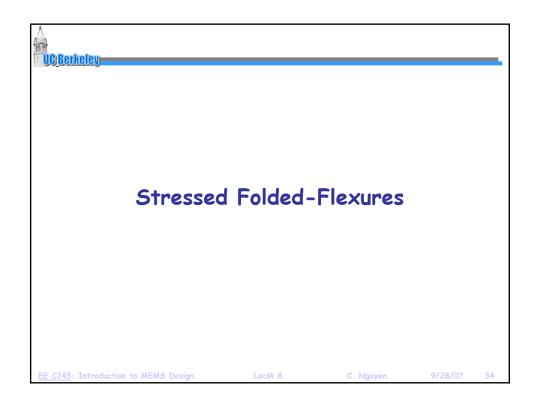


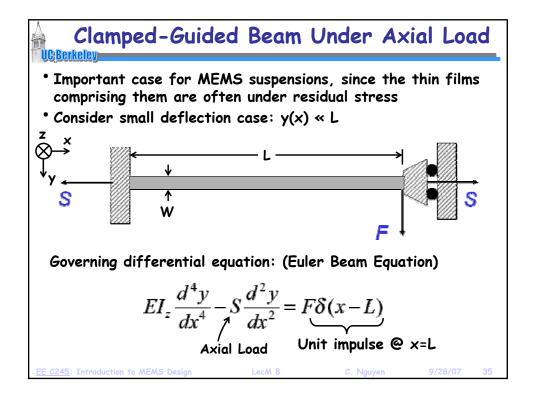


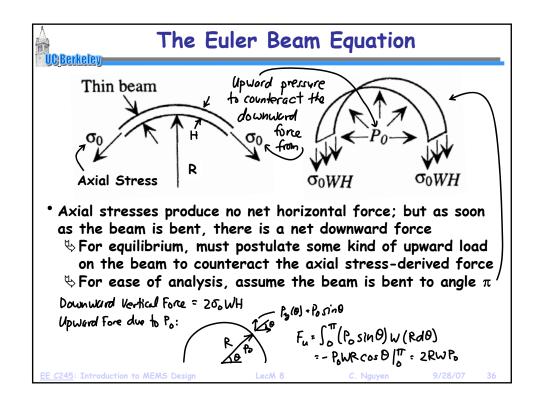


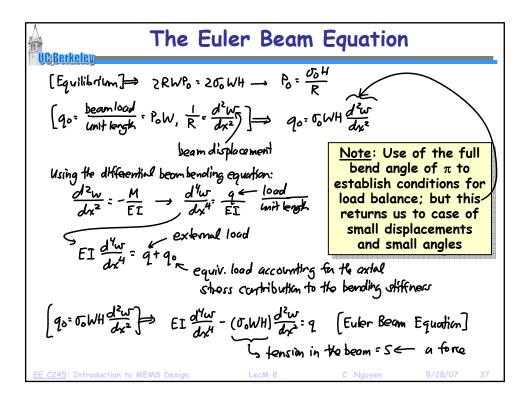


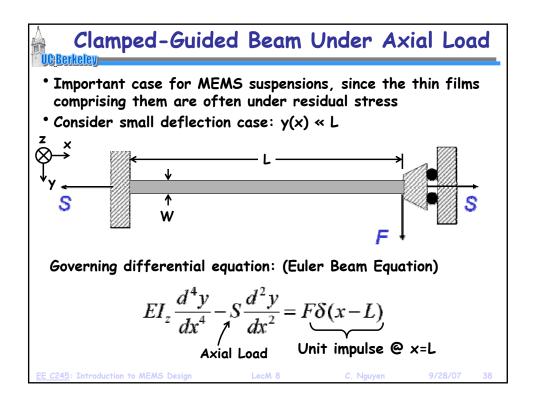












Solving the ODE

- UC Berkeley
- Can solve the ODE using standard methods
 - Senturia, pp. 232-235: solves ODE for case of point load on a clamped-clamped beam (which defines B.C.'s)
 - ♦ For solution to the clamped-guided case: see S. Timoshenko, Strength of Materials II: Advanced Theory and Problems, McGraw-Hill, New York, 3rd Ed., 1955
- Result from Timoshenko:

$$S > 0$$
 (tension) $k^{-1} = \frac{pL - 2\tanh(pL/2)}{p|S|} = \frac{y(x = L)}{F}$

S < 0 (compression)

$$k^{-1} = \frac{-pL + 2\tan(pL/2)}{p|S|} = \frac{y(x=L)}{F}$$

where $p = \sqrt{\frac{|S|}{EI_z}}$

<u>EE C245</u>: Introduction to MEMS Design

LecM 8

C. Nguyen

9/28/07

Design Implications UCBerkeley Straight flexures \$ Large tensile S means flexure behaves like a tensioned wire (for which $k^{-1} = L/S$) $\$ Large compressive S can lead to buckling $(k^{-1} \rightarrow \infty)$ 1) If polysi shall is Er, then Folded flexures should expand by SLs=Erls-♦ Residual stress Outer 2 This than applier a load to the only partially beams, who AL SLs. released Tension to shuttle's centerline differs Compression by L_s for inner Compressive and outer legs offset expand 3 Beam Strain: $\epsilon_b = \frac{\Delta L}{L} = \frac{\Delta l_s}{L} = \epsilon_F \frac{L_s}{L}$

